

University of Anbar  
College of Engineering

# ***Soil Mechanics***

Prepared  
by  
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RAMADI – IRAQ



**College of Engineering**

**COURSE SYLLABUS**

**Course Title**

**SOIL MECHANICS**

**Course Code**

**CE 3321**

**2<sup>nd</sup> (Spring) Semester, 2018 / 2019**

**Course description:**

This course introduces the students to the Fundamental engineering properties of soil and their applications in geotechnical engineering This course covers the following topics:-

Soil composition, physical and chemical properties, and classifications; water movement and seepage problems; effective stress concept, stress distribution in soil mass, consolidation, shear strength, compaction and soil improvement.

## **Course Objectives/Goals:**

The goals of this course are to enable students:

- 1.** To develop an appreciation soil as a vital construction material, and of soil mechanics in the engineering of civil infrastructure;
- 2.** To develop an understanding of the relationships between physical characteristics and mechanical properties of soils;
- 3.** To understand the concepts governing the mechanical and fluid transport properties of soils
- 4.** To understand and be able to apply the modeling and analysis techniques used in soil mechanics: (a) Darcy's Law and flow-nets for seepage; (b) consolidation models for load-time-deformation responses of soils; (c) Mohr-Coulomb models for shear strength behavior of soils.



## **Course Learning Outcomes:**

By the end of successful completion of this course, the student will be able to:

- 1.** understand the origin, formation, parameters and basic fundamental behavior of soils and have the knowledge of soil classification and be able to classify the soil using Unified Soil Classification System
- 2.** understand the principles of soil compaction and the factors affecting soil compaction
- 3.** understand soil permeability and seepage theory and be able to analyze a seepage problem by flow net
- 4.** understand the effective stress concept and be able to calculate effective stress in non-seepage and seepage problems and be able to calculate the vertical stress in soils caused by various types of loading
- 5.** apply one-dimensional consolidation theory to calculate settlement and pore pressure as a function of time during consolidation
- 6.** apply the principles of shear strength of soils to various laboratory tests

## Distribution of Course Topics/Contents

Topics Covered	Chapter in Textbook	CLO
<b>ORIGIN OF SOIL AND GRAIN SIZE</b>	<b>Chapter 2</b>	<b>1</b>
<b>WEIGHT-VOLUME RELATIONSHIPS, PLASTICITY, AND STRUCTURE OF SOIL</b>	<b>Chapter 3</b>	<b>1</b>
<b>ENGINEERING CLASSIFICATION OF SOIL</b>	<b>Chapter 3</b>	<b>1</b>
<b>PERMEABILITY AND SEEPAGE PERMEABILITY</b>	<b>Chapter 5</b>	<b>3</b>
<b>IN SITU STRESSES</b>	<b>Chapter 6</b>	<b>4</b>
<b>STRESSES IN SOIL MASS</b>	<b>Chapter 6</b>	<b>4</b>
<b>CONSOLIDATION OF SOIL</b>	<b>Chapter 7</b>	<b>5</b>
<b>SHEAR STRENGTH OF SOIL</b>	<b>Chapter 8</b>	<b>6</b>
<b>SOIL COMPACTION</b>	<b>Chapter 4</b>	<b>2</b>

## Teaching and Learning Resources:

### Text Book(s):

**Braja M. Das, Fundamentals of Geotechnical Engineering, Cengage Learning, 3rd ed., 2008**

### Recommended Readings:

- 1. Principles of geotechnical engineering, Braja M. Das, 8th edition**
- 2. Soil mechanics, R.F. Craig, 8th ed.**
- 3. Solving problems in soil mechanics, B.H.C. Sutton, 2nd ed.**

### Students' Assessment:

Students are assessed as follows:

<b>Assessment Tool(s)**</b>	<b>Date</b>	<b>Weight (%)</b>
Semester activities: These include, Homeworks	At the end of each major topic	<b>15%</b>
Mid semester exam <b>or</b> Progress Exams	According to department schedule	<b>25%</b>
Final Exam	Week-16	<b>60%</b>
<b>Total</b>		<b>100%</b>

**Estimated Content 3 credit**

**Math. 20%**

**Engineering Science 80%**

**Engineering Design 0%**



## *Soil Mechanics*

*Assistant Professor Dr. Khalid R. Mahmood, Instructor*

### **Catalogue Description**

- *Origin of Soil and Grain Size*
- *Weight-Volume Relationships, Plasticity, and Structure of Soil*
- *Engineering Classification of Soil*
- *Permeability*
- *Seepage*
- *In Situ Stresses (Effective Stress Concept)*
- *Stresses in a Soil Mass*
- *Compressibility of Soil*
- *Shear Strength of Soil*
- *Soil Compaction*




## Textbook and Reference Books

*Textbook- Fundamentals of Geotechnical Engineering*, Braja M. Das, 3<sup>rd</sup> ed., 2008

1. *Principles of geotechnical engineering*, Braja M. Das, 8<sup>th</sup> edition
2. *Soil mechanics*, R.F. Craig, 8<sup>th</sup> ed.
3. *Solving problems in soil mechanics*, B.H.C. Sutton, 2<sup>nd</sup> ed.
4. *Soil mechanics laboratory manual*, Braja M. Das, 6<sup>th</sup> ed., 2002

## Types of Civil Engineering

- Structural Engineering
- Transportation Engineering
- Environmental Engineering
- Coastal Engineering
- **Geotechnical Engineering** 
  - **Soil Mechanics**
  - **Foundation Engineering**

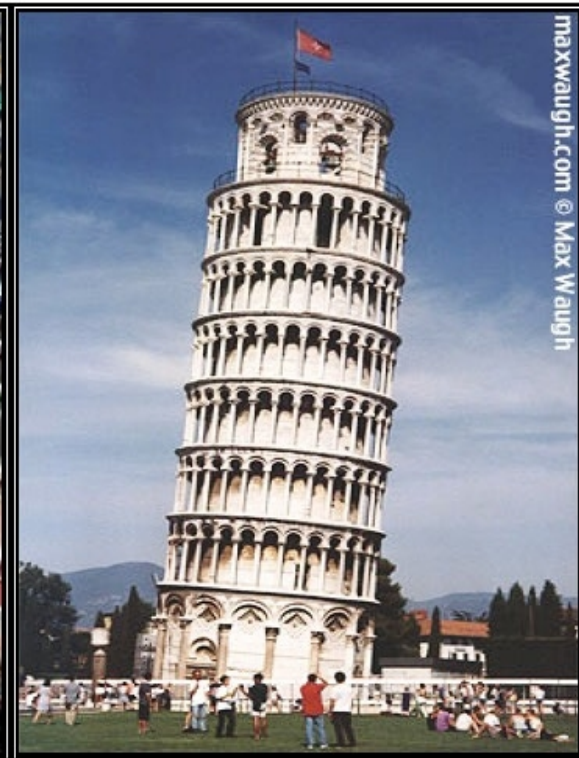
## Problems in Geotechnical Engineering

- Shear Failure-Loads have exceeded shear strength capacity of soil!



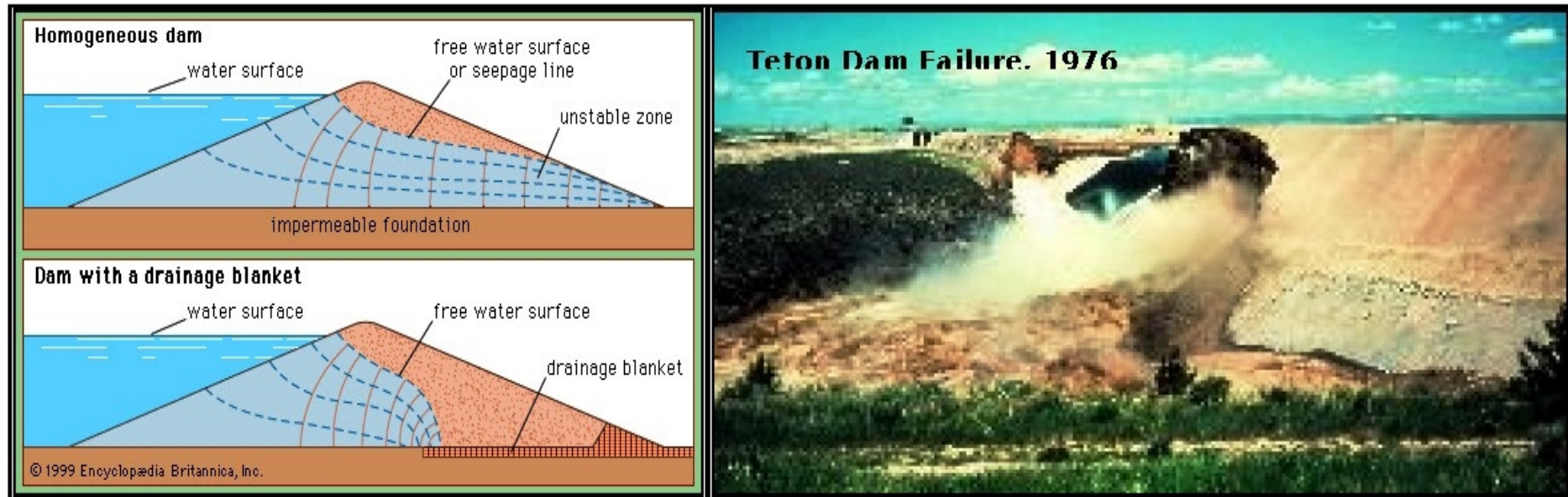


- Settlement



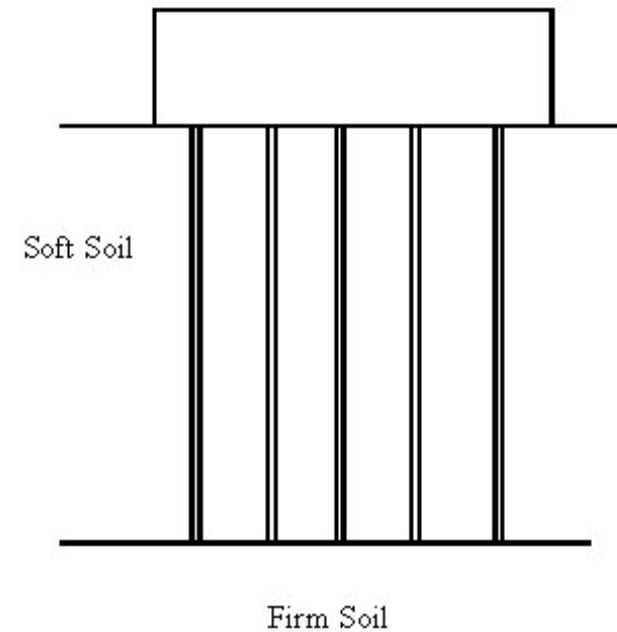
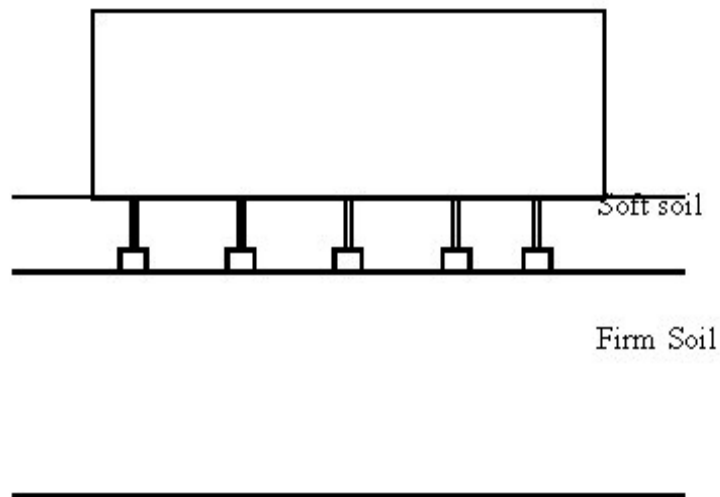


## • Seepage Problems



## Engineering problems related to Soil Mechanics

### 1- Soil as a foundation



For difficult soil condition such as **expansive soil, collapsible soil (gypseous soil)** special precautions must be taken in designing and construction of foundations on such soils.



## **2- Soil as a construction material**

It can be used in works such as:

- Pavement works (Flexible and Rigid pavements works)
- Earth dams and embankments
- Earth filling.

Here we must take into consideration the following factors

- Type of soil to be selected.
- Quality control of compacting soil.
- Proper methods are used for replacement and compaction of the soil.
- The availability of the required type of soil near the site.



## The Unique Nature of Soil

The soils are often highly variable, even within a distance of few millimeters. Another way of saying this is that soils are-

- **Heterogeneous** rather than **homogenous** materials.
- **Anisotropic** instead of being **Isotropic**
- The stress-strain relationships did not obey linear stress- strain laws.
- their behavior depends on pressure, time, and the environment.

Most of the theories we have for the mechanical behavior of engineering materials assume that the materials are Homogenous, Isotropic and obey linear stress- strain laws, so most of the relations used in Soil Mechanics are empirical relationships.



## The solution of soil engineering problems

It includes the basic principles of-

### Soil mechanics

Geology, Exploration

Experience

Economics



+ Engineering  
Judgment

=

Solutions



## Origin of Soil and Grain Size

### Soils and Rocks

#### Definition of “Soil” and “Rock”

- **Soil**

Naturally occurring mineral particles which are readily separated into relatively small pieces, and in which the mass may contain air, water, or organic materials (derived from the decay of vegetation).

- **Rock**

Naturally occurring material composed of mineral particles so firmly bonded together that relatively great effort is required to separate the particles (i.e., blasting or heavy crushing forces).

#### Types of Rocks

- Igneous rocks (**Intrusive** and **extrusive**) such as Granite, Basalt, ....etc.
- Sedimentary rocks such as sandstone, limestone, shales,...etc.
- Metamorphic rocks such as gneiss, marble, slate



## Methods of Classifying Rocks

- Visual Classification
- Weathering Classification
- Discontinuity Classification
- Colour and Grain Size
- Hardness Classification
- Geological Classification
- Classification by Field Measurements and Strength Tests
- Strength
- Rock Quality Designation and Velocity Index Rock

### Rock Quality Designation (RQD)

- Based on a modified core recovery procedure

$L_i$  = length of a given recovered piece  $\geq 4"$

$L_t$  = total length of core sample

$$RQD = \frac{\sum L_i}{L_t}$$





- Velocity index

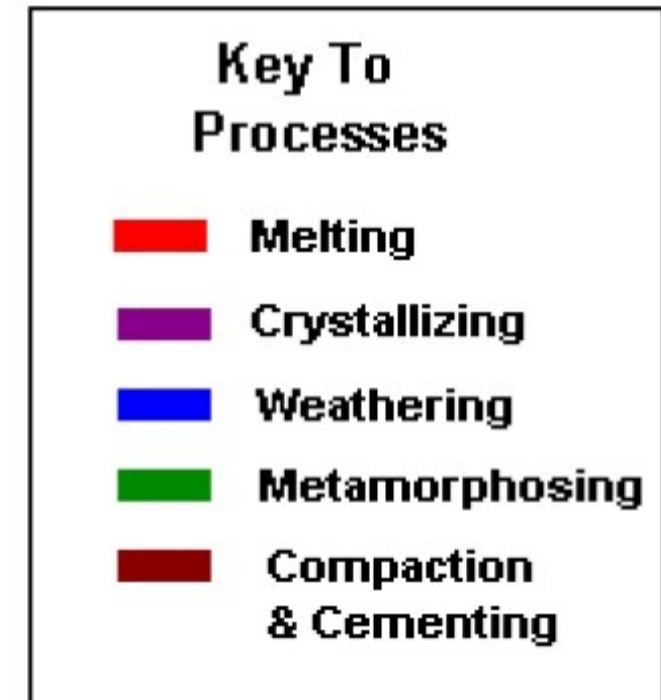
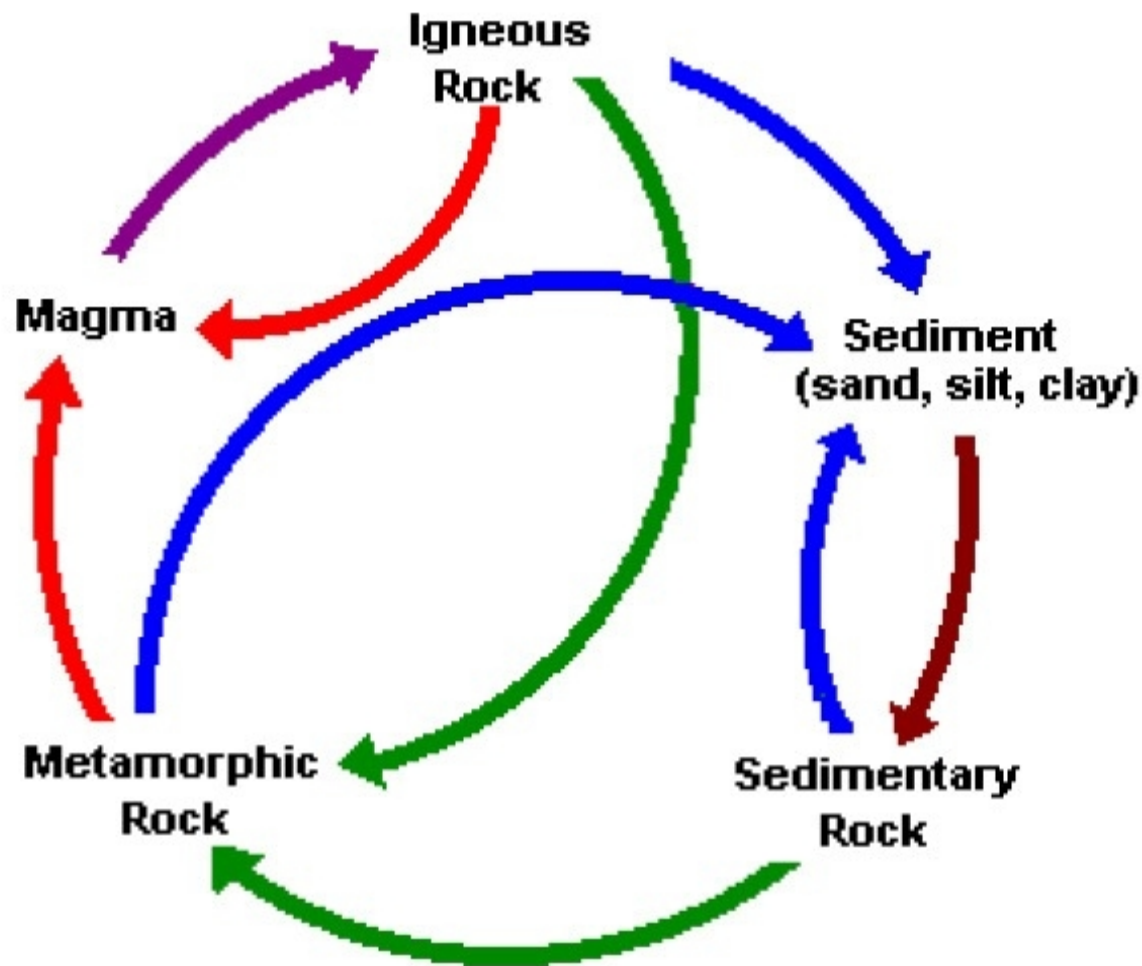
- Square of the ratio of the field compression wave velocity to the laboratory compression wave velocity
- Typically used to determine rock quality using geophysical surveys

### Rock Quality Designation (RQD)

RQD%	VELOCITY INDEX	ROCK MASS QUALITY
90 - 100	0.80 - 1.00	Excellent
75 - 90	0.60 - 0.80	Good
50 - 75	0.40 - 0.60	Fair
25 - 50	0.20 - 0.40	Poor
0 - 25	0 - 0.20	Very Poor



## Soil – Rock Cycle





## Weathering

*Physical or Mechanical weathering* causes disintegration of the rocks into smaller particle sizes, the processes that cause physical weathering are-

- **Freezing and thawing**
- **Temperature changes**
- **Erosion (Abrasion)**
- **Activity of plants and animals including man**

*Chemical weathering* causes decomposition in rocks by –

- **Oxidation** – union of oxygen with minerals in rocks forming another mineral
- **Hydration** – water will enter the crystalline structure of minerals forming another group of minerals
- **Hydrolysis** – the release Hydrogen from water will union with minerals forming another mineral
- **Carbonation** – when  $\text{CO}_2$  is available with the existence of water the minerals changed to Carbonates



## Basic Soil Types

<b>Parent Rocks</b>	
<b>Sedimentary Soils</b>	<b>Transported Soils</b>
	<b>transported and deposited by</b>
<ul style="list-style-type: none"> <li>• Residual</li> <li>• Organic</li> </ul>	<ul style="list-style-type: none"> <li>• Alluvial      running water</li> <li>• Aeolian      wind</li> <li>• Glacial      glaciers, or by melt water from the glacier</li> <li>• Marine      ocean waves and currents in shore and offshore</li> <li>• Colluvial    gravity</li> <li>• Pyroclastic   Material-propelled lava</li> </ul>



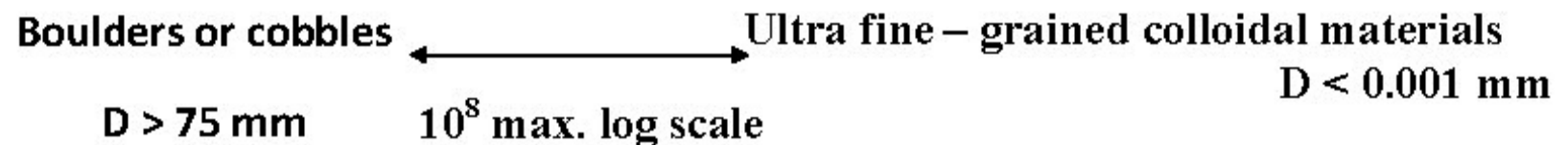
## Special Soils (problematic soil)

- Expansive Soils
- Collapsing Soils
- Permafrost and Frost Penetration
- Man-made and Hydraulic Fills
- Limestone and Related Soils
- Karst Topography
- Calcareous Soils
- Quick Clays
- Dispersive Clays
- Submarine Soils

## Soil-Particle Size or Grain Sizes

We are often interested in the particle or grain sizes present in a particular soil as well as the distribution of those sizes.

Its range





**Table 2.1** Soil-separate-size limits

Name of organization	<i>Cohesionless soils</i>		<i>Cohesive soils</i>	
	Grain size (mm)			
	Gravel	Sand	Silt	Clay
Massachusetts Institute of Technology (MIT)	>2	2 to 0.06	0.06 to 0.002	<0.002
U.S. Department of Agriculture (USDA)	>2	2 to 0.05	0.05 to 0.002	<0.002
American Association of State Highway and Transportation Officials (AASHTO)	76.2 to 2	2 to 0.075	0.075 to 0.002	<0.002
Unified Soil Classification System (U.S. Army Corps of Engineers; U.S. Bureau of Reclamation; American Society for Testing and Materials)	76.2 to 4.75	4.75 to 0.075	Fines (i.e., silts and clays) <0.075	





## *Soil Cohesion*

<i>Coarse-grained, Granular or Cohesionless Soils</i>	<i>Fine-Grained or Cohesive Soils</i>
<ul style="list-style-type: none"><li>● Generally are granular or coarse-grained</li><li>● Particles do not naturally adhere to each other</li><li>● Have higher permeability</li><li>● Excellent foundation material for supporting structures and roads.</li><li>● The best embankment material.</li><li>● The best backfill material for retaining walls.</li><li>● Might settle under vibratory loads or blasts.</li><li>● Dewatering can be difficult due to high permeability.</li><li>● If free draining does not frost susceptible</li></ul>	<ul style="list-style-type: none"><li>● Generally are fine grained</li><li>● Particles have natural adhesion to each other</li><li>● due to the presence of clay minerals</li><li>● Have low permeability</li><li>● Very often, possess low shear strength.</li><li>● Plastic and compressible.</li><li>● Loses part of shear strength upon wetting.</li><li>● Loses part of shear strength upon disturbance.</li><li>● Shrinks upon drying and expands upon wetting.</li><li>● Very poor material for backfill.</li><li>● Poor material for embankments.</li><li>● Practically impervious.</li><li>● Clay slopes are prone to landslides.</li></ul>



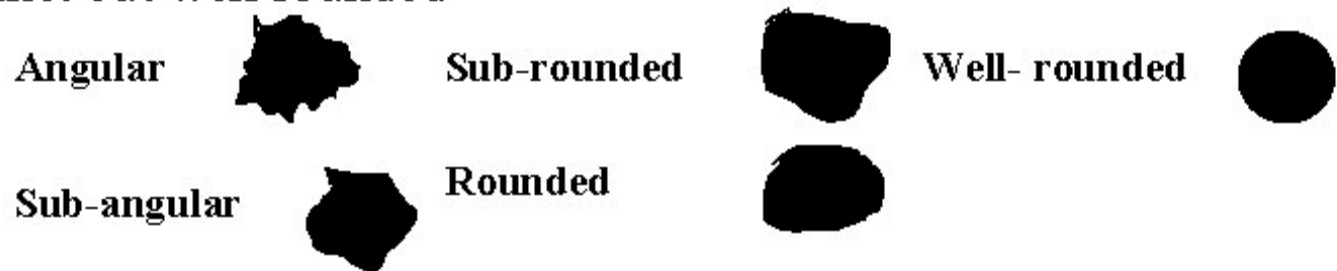
## Silts

<ul style="list-style-type: none"> <li>● Characteristics                     <ul style="list-style-type: none"> <li>● Relatively low shear strength</li> <li>● High Capillarity and frost susceptibility</li> <li>● Relatively low permeability</li> <li>● Difficult to compact</li> </ul> </li> </ul>	<p>Compared to Clays</p> <ul style="list-style-type: none"> <li>● Better load sustaining qualities</li> <li>● Less compressible</li> <li>● More permeable</li> <li>● Exhibit less volume change</li> </ul>
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## Aspects of Cohesionless Soils

### Angularity

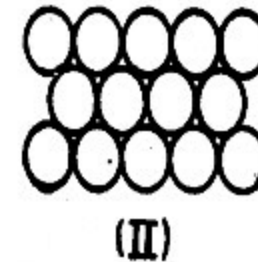
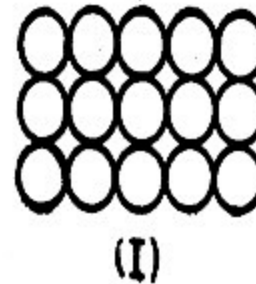
- Angular – Sharp Edges
- Subangular – Edges distinct but well rounded
- Subrounded
- Rounded
- Well Rounded



## Density

- Both unit weight and strength of soil can vary with particle arrangement
- Denser soils have both higher load carrying capacity and lower settlement

$$e_{\max} = 0.91 \quad n_{\max} = 48\%$$
$$e_{\min} = 0.35 \quad n_{\min} = 26\%$$



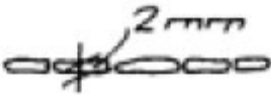



## Relative Density

$$D_r = \frac{e_{\max} - e_o}{e_{\max} - e_{\min}} \times 100$$

- $e_{\max}$  = void ratio of the soil in its loosest condition
- $e_{\min}$  = void ratio of the soil in its densest condition
- $e_o$  = void ratio in the natural or condition of interest of the soil
- Convenient measure for the strength of a cohesionless soil



## Properties of Fine Soils

<u>Plasticity</u>	<u>Silt</u>	<u>Clay</u>
	Low	High
<u>Settlement rate</u>		
	Settles within 20 min	Suspension after 24h.
<u>Dilatancy</u>		
	High	Low
<u>Dry strength</u>		
	Low	High



## *Aspects of Cohesive and Fine-Grained Soils*

- Structure of Clay Minerals
- Types of Clay Minerals
- Clay Minerals and Water
- Particle Orientation of Clay Soils
- Thixotropy



## *Structure of Clay Minerals*

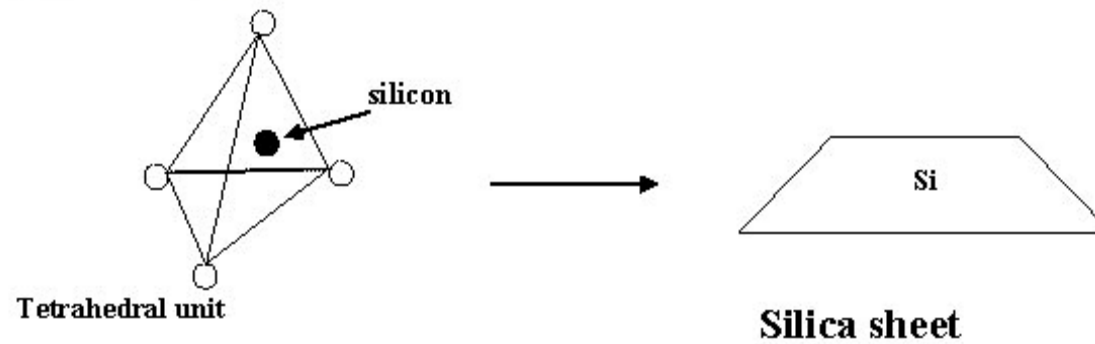
Clay minerals are very tiny crystalline substances evolved primarily from chemical weathering of certain rock forming minerals, they are *complex alumino – silicates plus other metallic ions*.

All clay minerals are very small with colloidal – sized ( $D < 1\mu\text{m}$ ). Because of their small size and flat shape, they have very large specific surfaces.

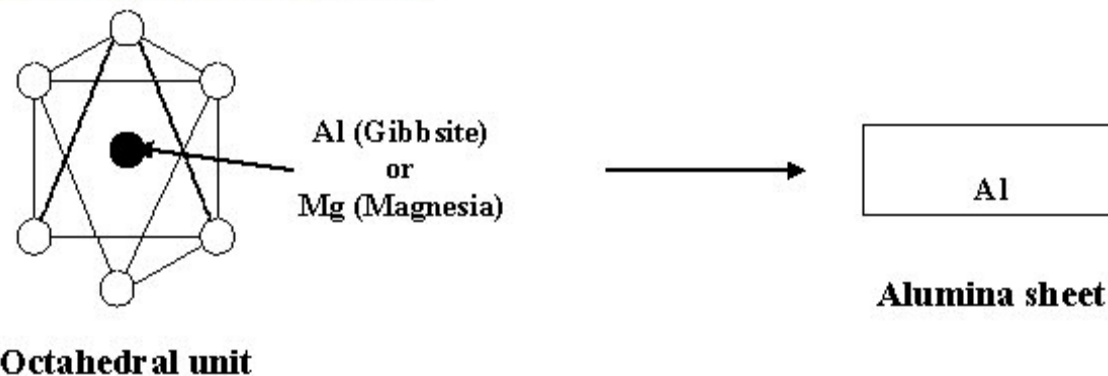
There is usually a negative electric charge on the crystal surfaces and electro – chemical forces on these surfaces are therefore predominant in determining their engineering properties.

In order to understand why these materials behave as they do, it will be necessary to examine their crystal structure in some detail.

- Atoms of clay minerals form sheets
  - **Silica tetrahedral sheets**



- **Alumina octahedral sheets**



- Sheets can layer in different ways, forming different types of clay minerals
- Clay minerals tend to form flat, platelike, and niddle shapes



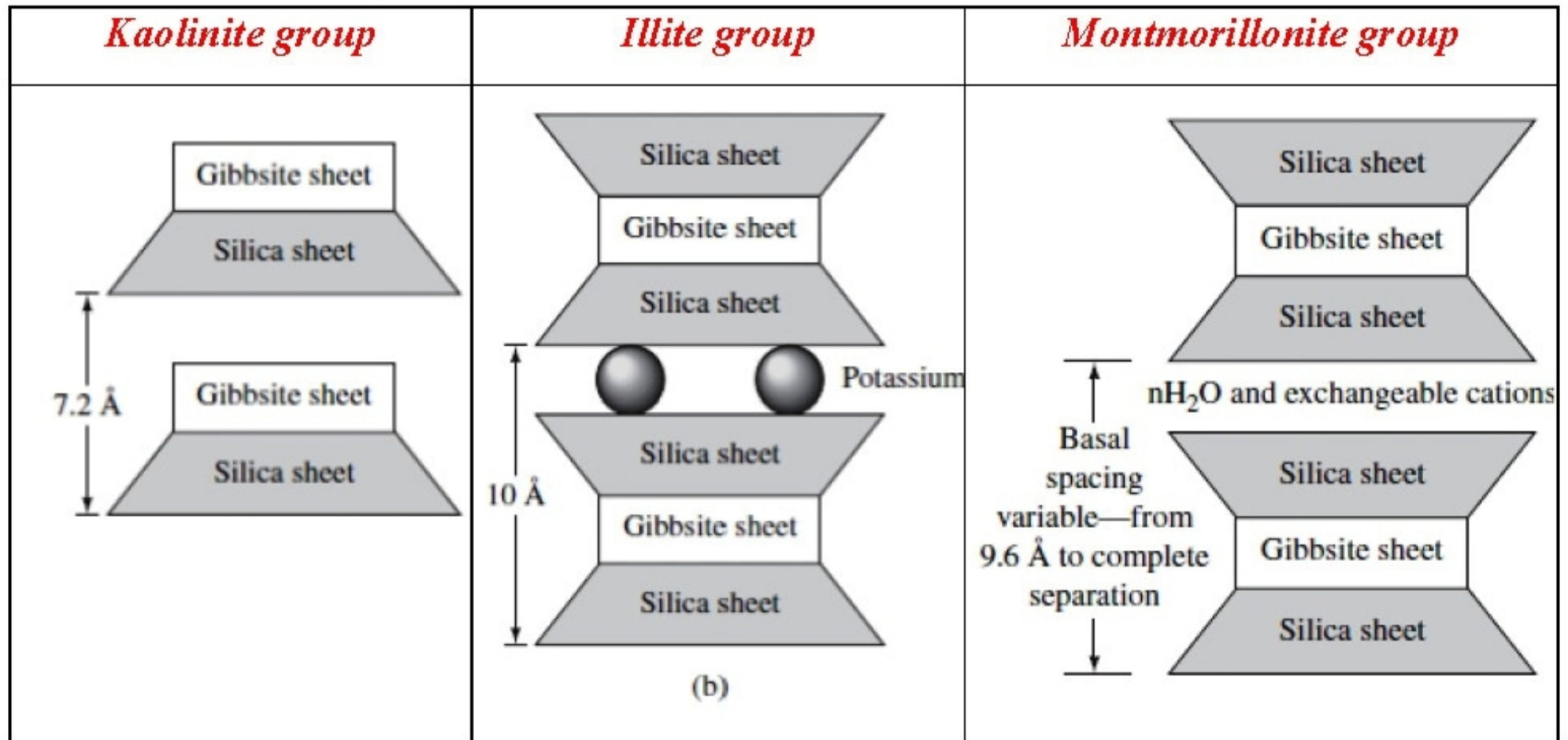
- **Electro – Chemical Forces**

- Primary valency bonds
- Van der Waals forces or molecular bonds
- Polar forces
- Hydrogen bonds

- **Isomorphic substitutions and absorbed ions**

It is the replacement of the silicon and aluminum ions in the crystal by other elements, with no change in the crystalline structure

## Types of Clay Minerals





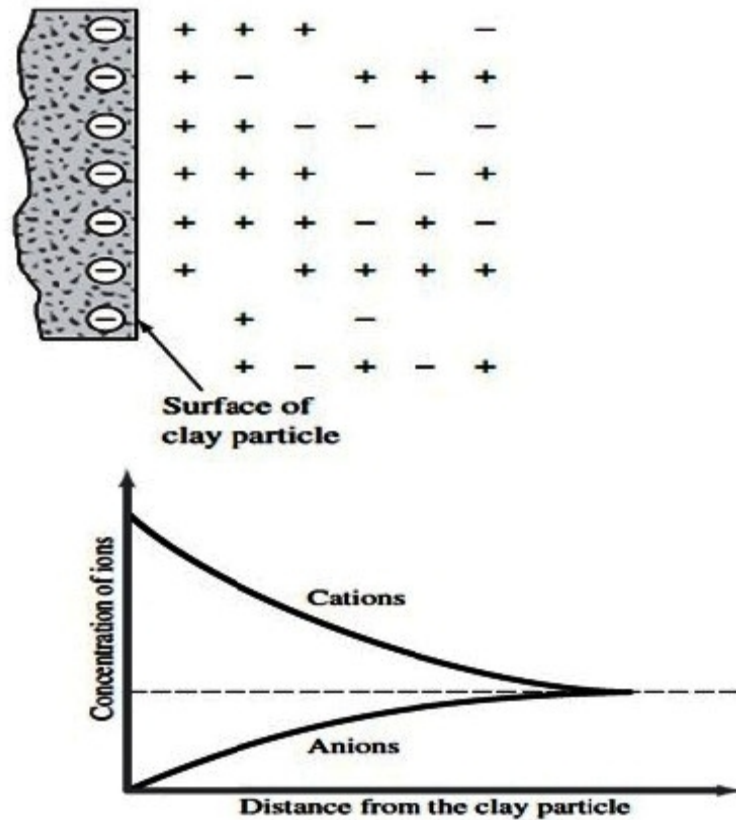
### *Specific surface*

$$S.S = \frac{As}{V} \left( \frac{1}{length} \right) ; S.S = \frac{As}{m} \left( \frac{length^2}{mass} \right)$$

Cube	S.S
$1 \times 1 \times 1 \text{ cm}^3$	$\frac{6(1\text{cm}^2)}{1\text{cm}^3} = 6 / \text{cm} = 0.6 / \text{mm}$
$1 \times 1 \times 1 \text{ mm}^3$	$\frac{6(1\text{mm}^2)}{1\text{mm}^3} = 6 / \text{mm}$
$1 \times 1 \times 1 \text{ }\mu\text{m}^3$	$\frac{6(1\mu\text{m}^2)}{1\mu\text{m}^3} = 6 / \mu\text{m} = 6000 / \text{mm}$



## How is water absorbed on the surface of a clay particle?



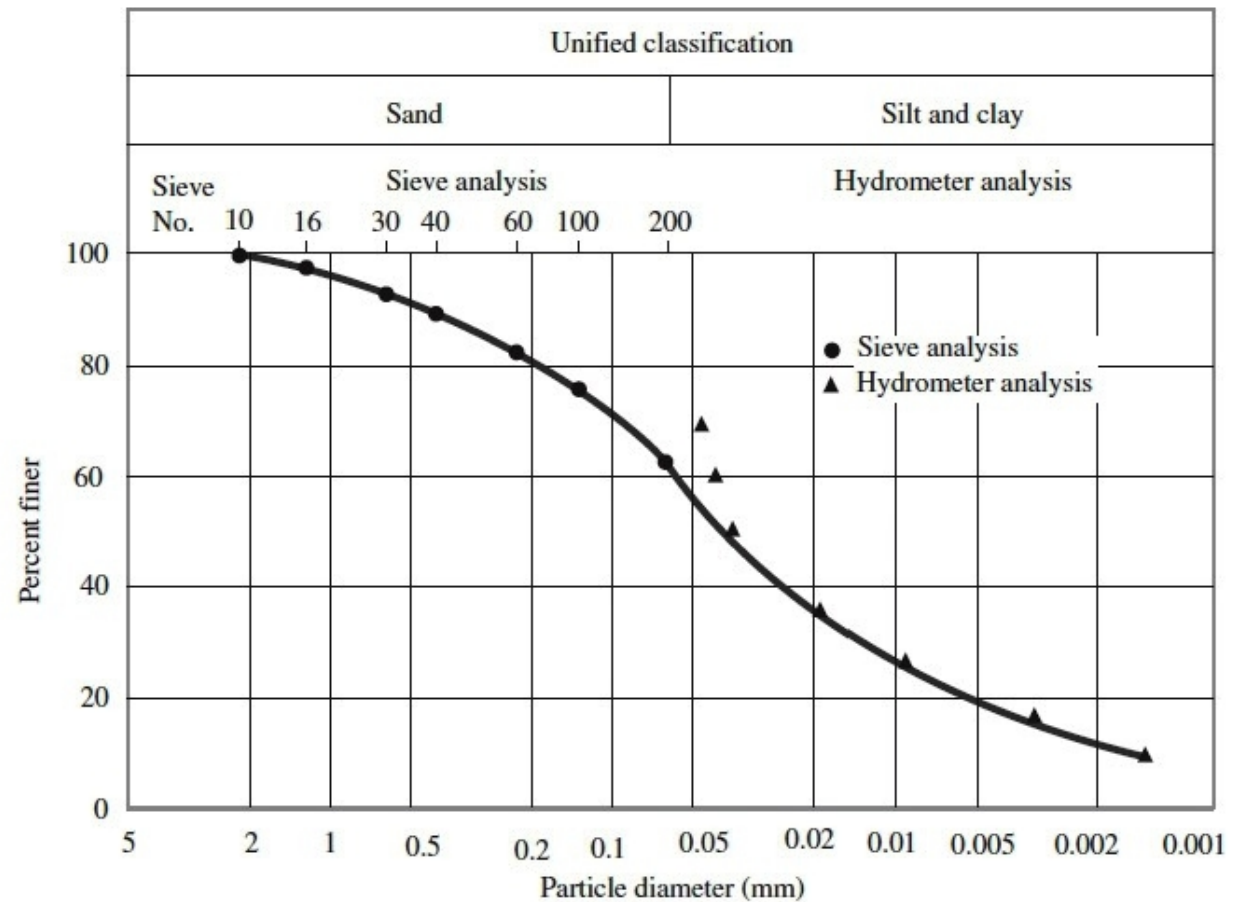


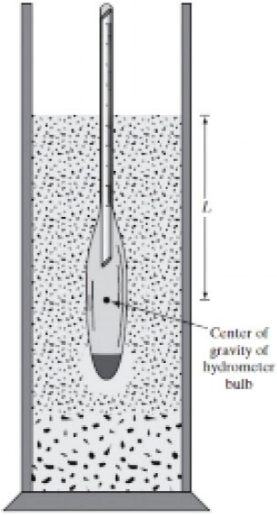


## Gradation of Particle Size

### Sieve Analysis

### Hydrometer Analysis







*D<sub>x</sub>* – designates particle size for which *x* percent of sample has passed

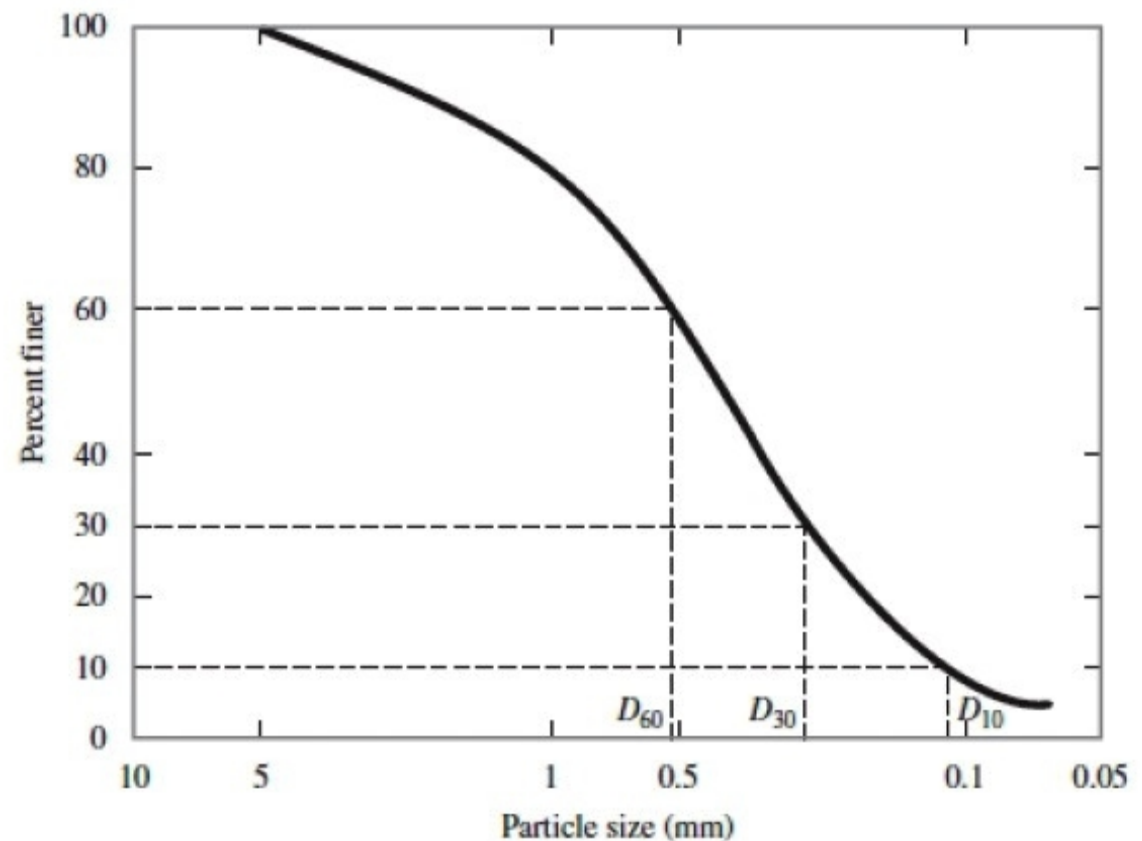
- *D*<sub>10</sub> – effective size – particle size at which 10% of the sample has passed. It is useful to determine permeability

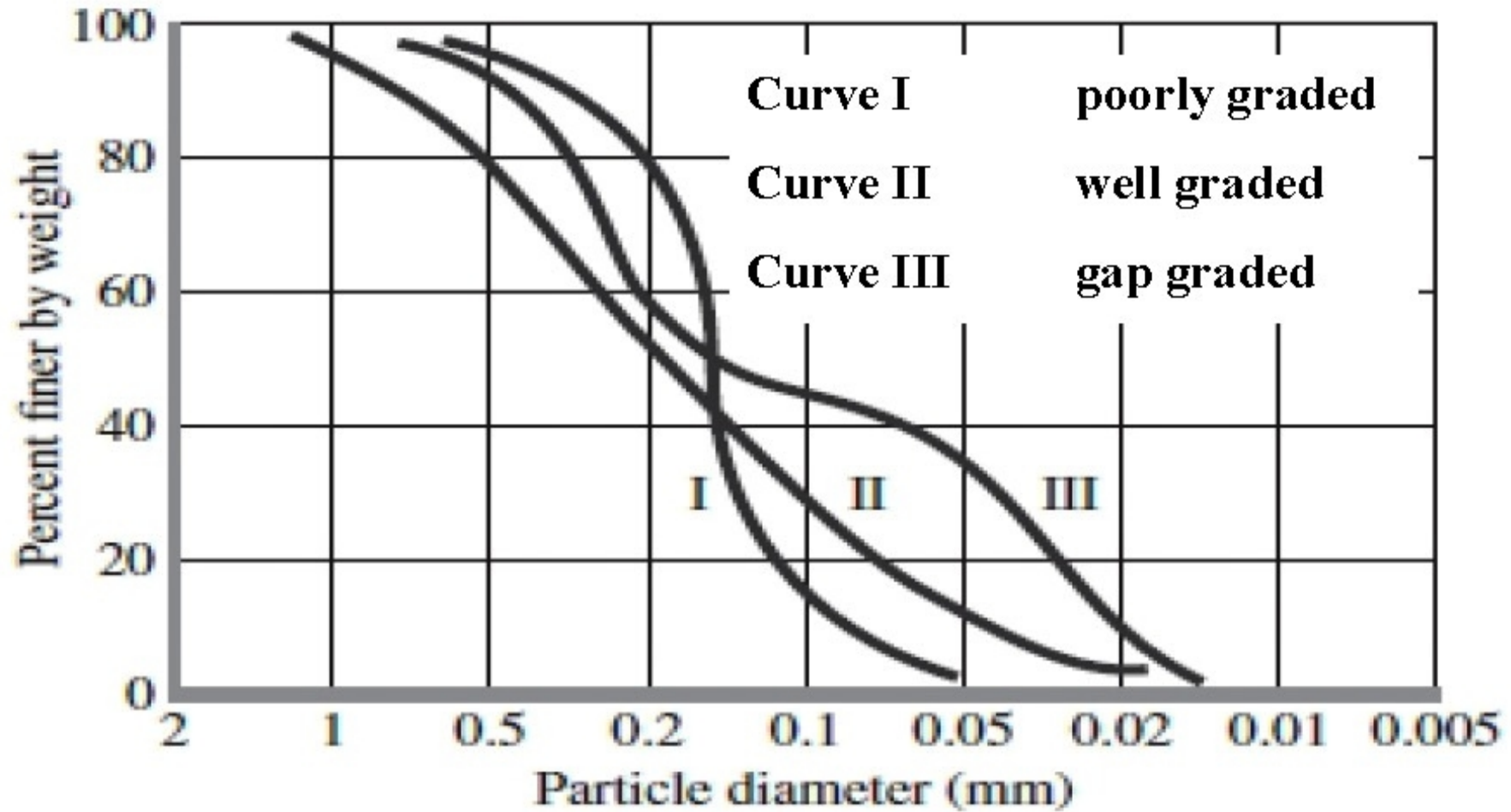
*Uniformity Coefficient C<sub>u</sub>*

$$C_u = \frac{D_{60}}{D_{10}}$$

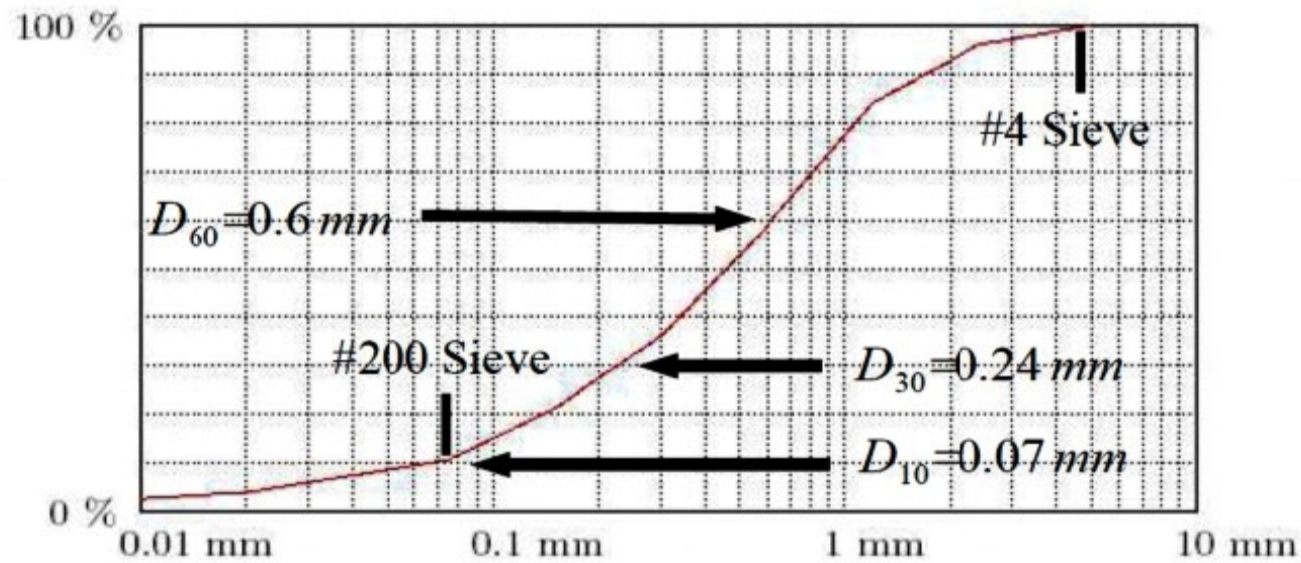
*Coefficient of Curvature C<sub>c</sub>*

$$C_c = \frac{D_{30}^2}{D_{10}D_{60}}$$





## Sieve Analysis Example



$$C_u = \frac{D_{60}}{D_{10}} = \frac{0.6}{0.07} = 8.5$$

$$C_c = \frac{D_{30}^2}{D_{10}D_{60}} = \frac{0.24^2}{0.07 \times 0.6} = 1.37$$



## *Weight-Volume Relationships, Plasticity, and Structure of Soil*

### *Topics*

- Basic Concepts
- Phase Diagram
- Important variables-  
(Water or Moisture Content-Unit Weight or Mass-Void ratio-Specific Gravity.....etc.
- Atterberg limits and consistency indices
- Soil Structure and Fabric

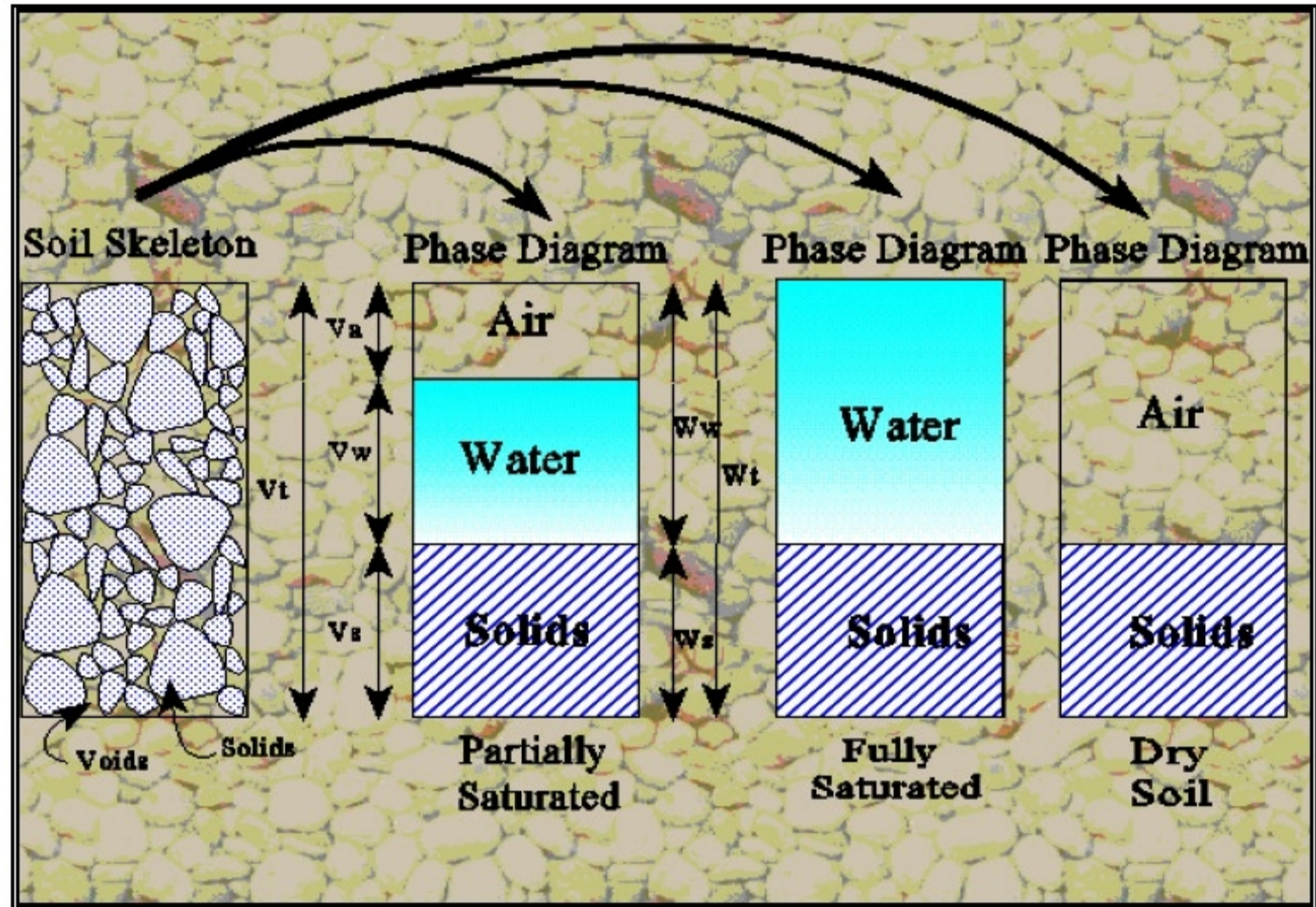




## *Basic Concepts*

- Soil is a collection of particles that do not form a totally solid substance
- Soil is a combination of:
  - ◆ Soil material in particles
  - ◆ Air
  - ◆ Water
  
- The relationship between this combination defines much of what any particular soil can do to support foundations

## Phase Diagram





### Basic Formulas

$$V_{total} = V_{air} + V_{water} + V_{soil}$$

$$W_{total} = W_{water} + W_{soil} \quad \text{or} \quad M_{total} = M_{water} + M_{soil}$$

$$W_x = \gamma_x \times V_x \quad \text{or} \quad M_x = \rho_x \times V_x$$

### Specific Gravity and Density

<ul style="list-style-type: none"> <li>● Unit Weight of Water (<math>\gamma_w</math>)                     <ul style="list-style-type: none"> <li>◆ 62.4 lb/ft<sup>3</sup></li> <li>◆ 9.81 kN/m<sup>3</sup> ≈ 10 kN/m<sup>3</sup></li> </ul> </li> </ul>	Density of Water <ul style="list-style-type: none"> <li>◆ 1.95 slugs/ft<sup>3</sup></li> <li>◆ 1 g/cm<sup>3</sup> = 1 Mg/m<sup>3</sup> = 1 Metric Ton/m<sup>3</sup></li> </ul>
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### Typical Specific Gravities for Soil Solids

<ul style="list-style-type: none"> <li>◆ Quartz Sand: 2.64 – 2.66</li> <li>◆ Silt: 2.67 – 2.73</li> <li>◆ Clay: 2.70 – 2.9</li> </ul>	<ul style="list-style-type: none"> <li>◆ Chalk: 2.60 – 2.75</li> <li>◆ Loess: 2.65 – 2.73</li> <li>◆ Peat: 1.30 – 1.9</li> <li>◆ Except for organic soils, range is fairly narrow</li> </ul>
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## Weight and Volume Relationships

$$W_x = G_x \times \gamma_w \times V_x$$

$$M_x = G_x \times \gamma_w \times V_x$$

In most cases, calculations in soil mechanics are done on a weight basis. Exceptions include wave propagation problems (earthquakes, pile dynamics,..... etc.)

## Important Variables

### 1. Void ratio, $e$

$$e = \frac{V_v}{V_s} \quad \text{Expressed as decimal} \quad \text{Sands (0.4 - 1.0) Clays (0.3 - 1.5)}$$

### 2. Porosity, $n$

$$n = \frac{V_v}{V_t} \times 100\% \quad \text{Expressed as percentage (0-100\%)}$$





Prove that  $n = \frac{e}{1+e}$  or  $e = \frac{n}{1-n}$

3. *Degree of saturation, S*

$$S = \frac{V_w}{V_v} \times 100\%$$

$S = 0\%$  Dry Soil,  $S = 100\%$  Saturated soil

4. *Air Content, Ac*

$$Ac = \frac{V_a}{V} \times 100\%$$

So we can show that  $Ac = n(1 - S)$

5. *Water Content,  $\omega$*

$$\omega = \frac{W_w}{W_s} \times 100\%$$

**$\omega$  can be equal to zero in dry soil and may be reached 500% in some marine and organic soils.**



## 6. Unit weight, $\gamma$

$$\text{Total unit weight, } \gamma_t = \frac{W_t}{V_t} = \frac{W_s + W_w}{V_t}$$

$$\text{Solid unit weight, } \gamma_s = \frac{W_s}{V_s} \quad \gamma_s \text{ range (25.4 kN/m}^3 \text{ - 28.5 kN/m}^3)$$

$$\text{Water unit weight, } \gamma_w = \frac{W_w}{V_w}$$

There are three other useful densities in soils engineering; they are

- Dry Unit weight,  $\gamma_d = \frac{W_s}{V_t}$
- Saturated Unit Weight,  $\gamma_{sat} = \frac{W_s + W_w}{V_t} = \frac{W_t}{V_t}$  (Va = 0, S = 100 %)
- Submerged Unit Weight,  $\gamma' = \gamma_{sat} - \gamma_w$





## 7. Specific gravity

$$G = \frac{\gamma}{\gamma_w} \quad \text{apparent} \qquad G_s = \frac{\gamma_s}{\gamma_w} \quad \text{Solid}$$

From the basic definitions provided above, other useful relationships can be derived such as:

$$\gamma_t = \frac{1+\omega}{1+e} G_s \gamma_w = \frac{G_s + Se}{1+e} \gamma_w \quad \gamma_d = \frac{\gamma_t}{1+\omega} = \frac{G_s}{1+e} \gamma_w \quad \gamma_{sat} = \frac{G_s + e}{1+e} \gamma_w$$

$$\gamma' = \frac{G_s - 1}{1+e} \gamma_w$$

**$Se = G_s \omega$**  H.W #1 prove these equations using basic definitions



## Solutions of phase problems

Probably the single most important thing you can do in solving phase problems is to draw a phase diagram & remember the following simple rules,

1. Remember the basic definitions of  $\omega$ ,  $e$ ,  $\gamma_s$ ,  $S$ , ..... etc.
2. Assume either  $V_s = 1$  or  $V_t = 1$  if not given
3. Often use  $Se = G_s \omega$



## Various Unit-Weight Relationships

**Table 3.1** Various Forms of Relationships for  $\gamma$ ,  $\gamma_d$  and  $\gamma_{sat}$

Moist unit weight ( $\gamma$ )		Dry unit weight ( $\gamma_d$ )		Saturated unit weight ( $\gamma_{sat}$ )	
Given	Relationship	Given	Relationship	Given	Relationship
$w, G_p, e$	$\frac{(1+w)G_s\gamma_w}{1+e}$	$\gamma, w$	$\frac{\gamma}{1+w}$	$G_p, e$	$\frac{(G_s + e)\gamma_w}{1+e}$
$S, G_p, e$	$\frac{(G_s + Se)\gamma_w}{1+e}$	$G_p, e$	$\frac{G_s\gamma_w}{1+e}$	$G_p, n$	$[(1-n)G_s + n]\gamma_w$
$w, G_p, S$	$\frac{(1+w)G_s\gamma_w}{1 + \frac{wG_s}{S}}$	$G_p, n$	$G_s\gamma_w(1-n)$	$G_p, w_{sat}$	$\left(\frac{1+w_{sat}}{1+w_{sat}G_s}\right)G_s\gamma_w$
$w, G_p, n$	$G_s\gamma_w(1-n)(1+w)$	$G_p, w, S$	$\frac{G_s\gamma_w}{1 + \left(\frac{wG_s}{S}\right)}$	$e, w_{sat}$	$\left(\frac{e}{w_{sat}}\right)\left(\frac{1+w_{sat}}{1+e}\right)\gamma_w$
$S, G_p, n$	$G_s\gamma_w(1-n) + nS\gamma_w$	$e, w, S$	$\frac{eS\gamma_w}{(1+e)w}$	$n, w_{sat}$	$n\left(\frac{1+w_{sat}}{w_{sat}}\right)\gamma_w$
		$\gamma_{sat}, e$	$\gamma_{sat} - \frac{e\gamma_w}{1+e}$	$\gamma_d, e$	$\gamma_d + \left(\frac{e}{1+e}\right)\gamma_w$
		$\gamma_{sat}, n$	$\gamma_{sat} - n\gamma_w$	$\gamma_d, n$	$\gamma_d + n\gamma_w$
		$\gamma_{sat}, G_s$	$\frac{(\gamma_{sat} - \gamma_w)G_s}{(G_s - 1)}$	$\gamma_d, S$	$\left(1 - \frac{1}{G_s}\right)\gamma_d + \gamma_w$
				$\gamma_d, w_{sat}$	$\gamma_d(1+w_{sat})$



## Example 1

For saturated sample with void ratio  $e = 0.6$  and  $G_s = 2.65$ .

Find:

1. porosity
2. moisture or water content
3. total unit weight

Solution:

Let  $V_s = 1 \text{ m}^3$  and  $\gamma_w = 10 \text{ kN/m}^3$

$$e = \frac{V_v}{V_s} \Rightarrow V_v = eV_s = 0.6 \times 1 = 0.6 \text{ m}^3$$

$$G_s = \frac{\gamma_s}{\gamma_w} = \frac{W_s}{V_s} \Rightarrow W_s = V_s \gamma_w G_s = 1 \times 10 \times 2.65 = 26.5 \text{ KN}$$



Since the sample is saturated then  $S=100\%$

$$\therefore V_w = V_v = 0.6 \text{ m}^3$$

$$\gamma_w = \frac{W_w}{V_w} \Rightarrow W_w = \gamma_w V_w = 10 \times 0.6 = 6 \text{ KN}$$

$$W_t = W_w + W_s = 6 + 26.5 = 32.5 \text{ KN}$$

$$V_t = V_s + V_v = 1 + 0.6 = 1.6 \text{ m}^3$$

$$n = \frac{V_v}{V_t} = \frac{0.6}{1.6} \times 100\% = 37.5\%$$

$$\omega = \frac{W_w}{W_s} = \frac{6}{26.5} \times 100\% = 22.7\%$$

$$\gamma_t = \frac{W_t}{V_t} = \frac{32.5}{1.6} \approx 20 \text{ KN / M}^3$$



## Example 2

A soil sample with dry unit weight  $\gamma_d = 18.5 \text{ KN/m}^3$  & specific gravity of solids  $G_s = 2.68$  submerges with water, the void ratio increases by 20%. Find-

1. The porosity of the soil before it was merged
2. The weight of 2 m<sup>3</sup> of the soil under the water table.

Solution:

$$\gamma_d = \frac{G_s}{1+e} \gamma_w$$

$$18.5 = \frac{2.68}{1+e} \times 10 \Rightarrow e = 0.449 = e_{dry}$$

$$\therefore n = \frac{e}{1+e} = \frac{0.449}{1+0.449} \times 100\% \cong 31\%$$

Since void ratio increased by 20% after it had been submerged





$$\therefore e_{sat} = 1.2e_{dry} = 0.539$$

$$\gamma' = \frac{G_s - 1}{1 + e} \gamma_w = \frac{2.68 - 1}{1 + 0.539} \times 10 = 10.92 \text{ kN/m}^3$$

The weight of 2 m<sup>3</sup> of submerged soil,

$$W_{sub} = \gamma' \cdot 2 = 21.84 \text{ kN}$$

### Example 3

A sample of saturated soil with  $\omega = 14\%$  and  $G_s = 2.7$ .

Find void ratio, total unit weight, and dry unit weight

Solution

$$Se = G_s \omega \Rightarrow (1)e = (2.7)(0.14) \Rightarrow e = 0.38$$

$$\gamma_t = \frac{1 + \omega}{1 + e} G_s \gamma_w = \frac{1 + 0.14}{1 + 0.38} \times 2.7 \times 10 = 22.3 \text{ kN/m}^3$$

$$\gamma_d \frac{\gamma_t}{1 + \omega} = \frac{22.3}{1 + 0.14} = 19.56 \text{ kN/m}^3$$

or

$$\gamma_d \frac{G_s}{1 + e} \gamma_w = \frac{2.7}{1 + 0.38} = 19.56 \text{ kN/m}^3$$

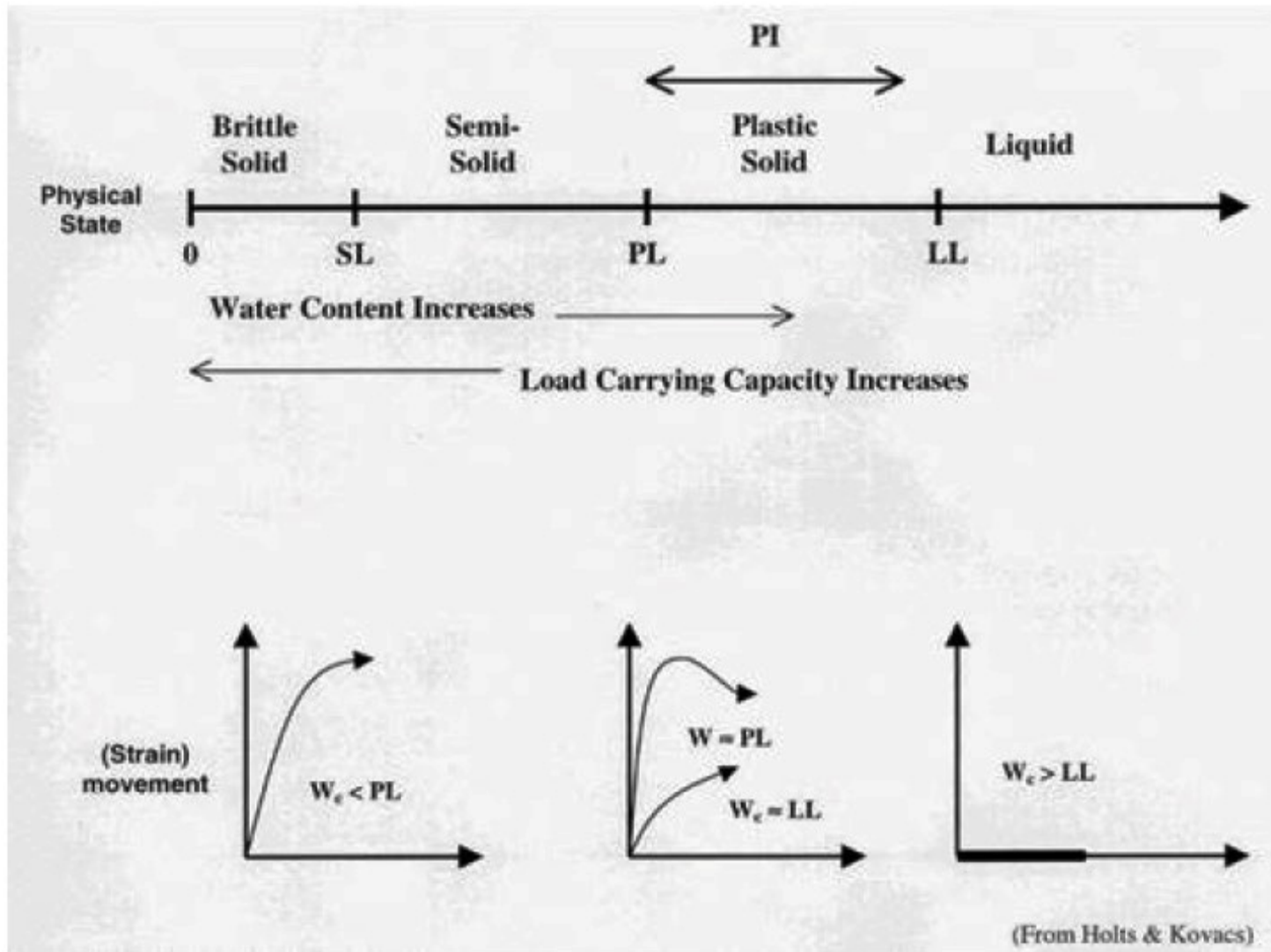


## *Atterberg limits and Consistency indices*

They are water contents at certain limiting or critical stages in soil behavior (especially, fine-grained soils). They, along with the natural water content ( $\omega_n$ ) are the most important items in the description of fine-grained soils and they are correlated with the engineering properties & behavior of fine-grained soils.

They are-

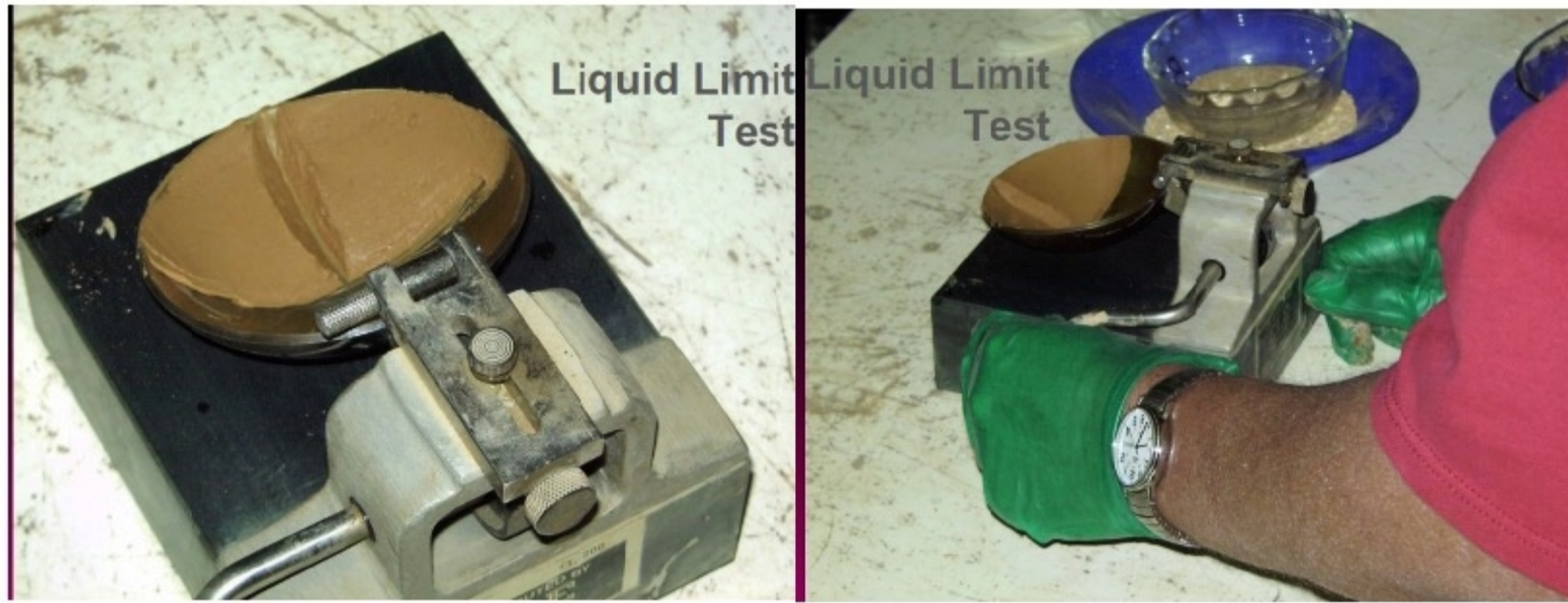
- 1- Liquid Limit (L.L or  $\omega_L$ ).
- 2- Plastic Limit (P.L or  $\omega_P$  ).
- 3- Shrinkage limit (S.L or  $\omega_S$  ).



## Liquid Limit

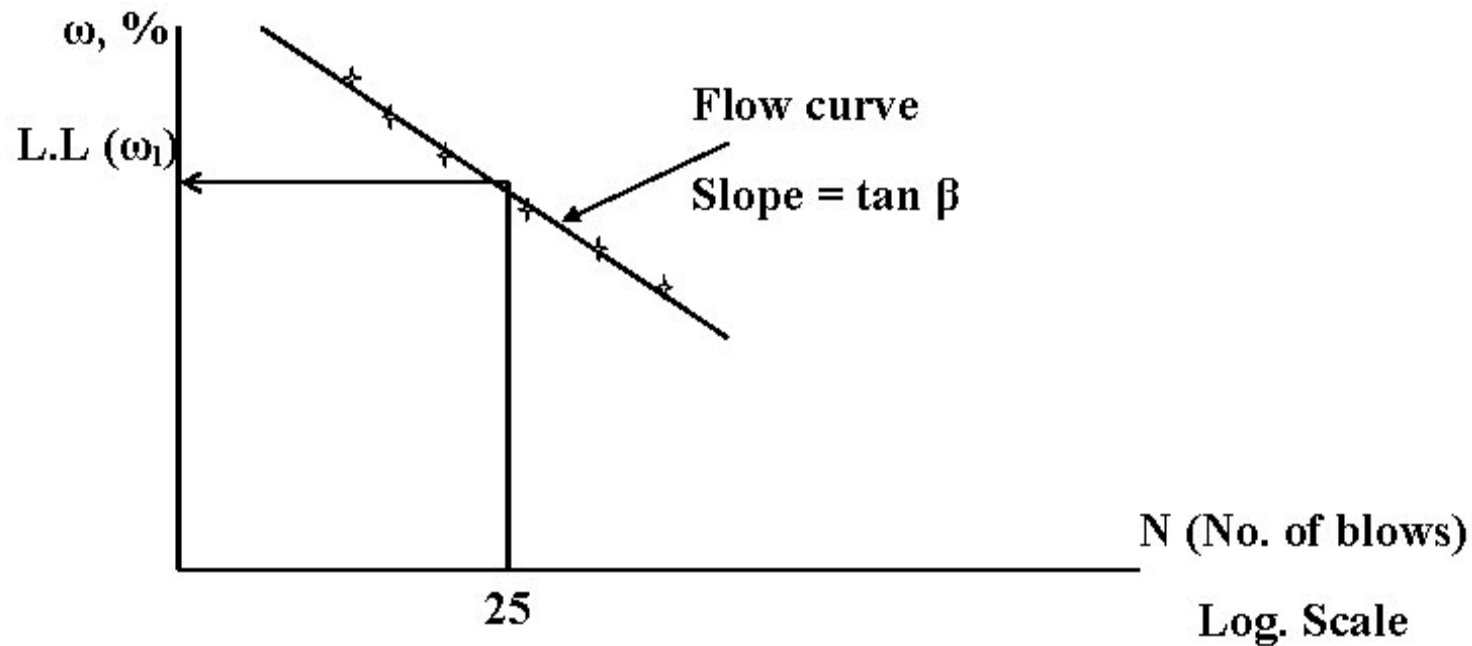
### Definition

Atterberg defined the liquid limit as a water content at which the soil becomes a viscous liquid.





In practice, it is difficult to mix the soil so that the groove closure occurs at exactly 25 blows, so Casagrande did the following:





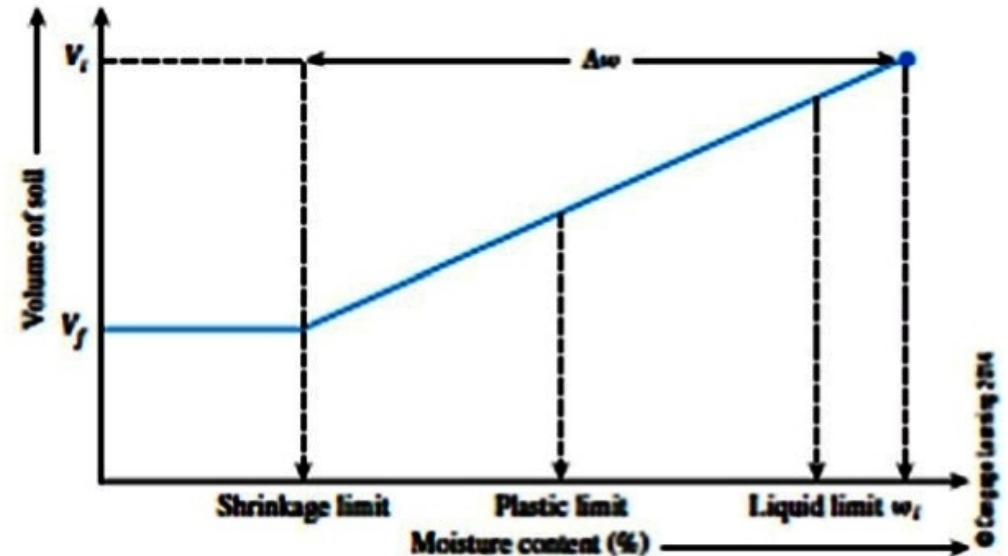
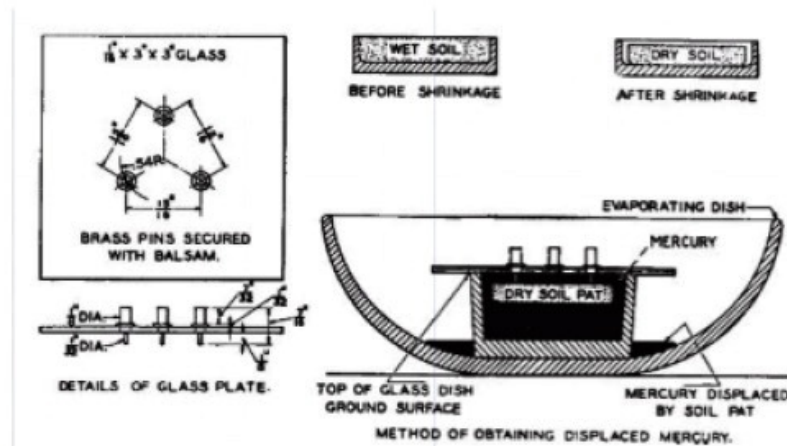
## Plastic Limit

Atterberg defined the plastic limit as water content at which soil becomes in a plastic state.



## Shrinkage Limit

It defines as a water content at which no further volume change occurs with continuous loss of moisture.





Other index properties for the soil

- Plasticity index,  $P.I = L.L - P.L$

- Flow index, 
$$F.I = \frac{\omega_2 - \omega_1}{\log N_2 - \log N_1} = \frac{\Delta\omega}{\log \frac{N_2}{N_1}} = \Delta\omega$$
  
 $\log \frac{N_2}{N_1} = 1$  for ...one...cycle

the slope of flow curve, it shows how close the clayey soil  
from the plastic state

- Toughness index,

$T.I = \frac{P.I}{F.I}$  express the soil consistency in the plastic State.

- Consistency index,



$$C.I = \frac{L.L - \omega_n}{L.L - P.L} = \frac{L.L - \omega_n}{P.I}$$

- Liquidity index,

$$- L.I = \frac{\omega_n - P.L}{P.I}$$

$L.I < 0$  --- the soil is in Brittle state

$L.I (0 - 1)$  – the soil is in plastic state

$L.I > 1$  --- the soil is in viscous liquid state

## Factors affecting the Atterberg Limits

1. Shape and size of grains.

As the grains size gets smaller the plasticity increases while grains with flaky shape had more plasticity characteristics than other shapes.

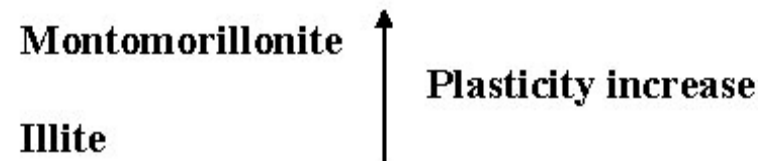


## 2. The content of clay minerals.

As the content of clay minerals increase the plasticity characteristics increase.

## 3. Type of clay minerals.

As we will describe later the characteristics of each type of clay mineral group the type will affect the plasticity characteristics and for instance



## 4. Type of ions.

The type of absorbed ions will affect the plasticity characteristics such as Na; Mg will give high plasticity while Ca will give low plasticity.

## 5. The content of organic matter.

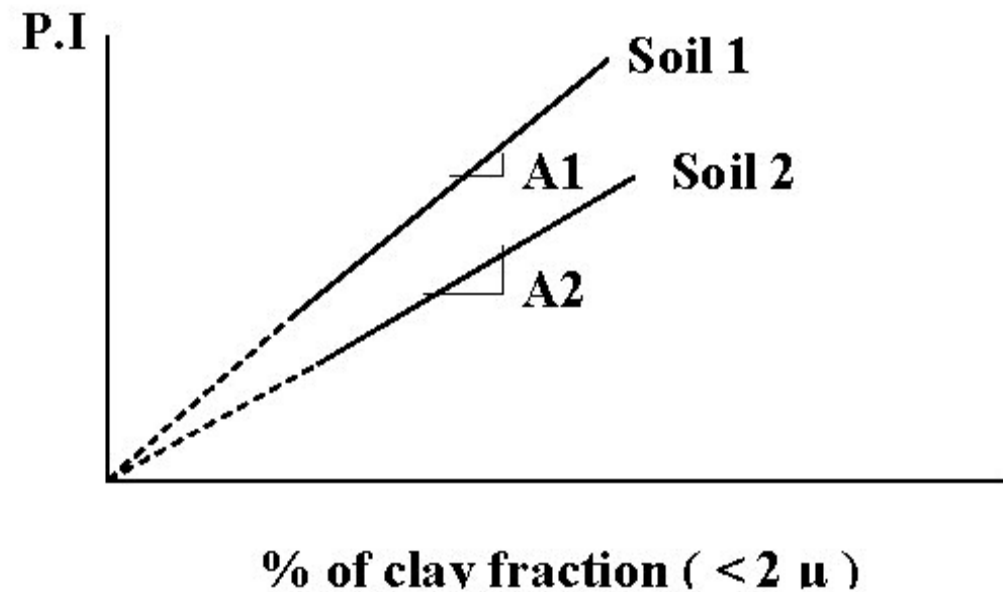
As the organic matter content increase the plasticity characteristics Increase.



## Activity

Skempton (1953) observed the following relationship. He defined a quantity called “*Activity*” which is the slope of the line correlating P.I. & % finer than 2 μm.

$$A = \frac{P.I.}{\% \text{ of clay} - \text{size fraction, by weight}}$$







This term used for identifying the swelling potential of clay soils and for certain classification properties.

<b>A</b>	<b>Soil classification</b>
<b>&lt; 0.75</b>	<b>Non Active</b>
<b>0.75 – 1.25</b>	<b>Normally Active</b>
<b>1.25 – 2.0</b>	<b>Active</b>

<b>A</b>	<b>Type of clay minerals</b>
<b>0.4 – 0.5</b>	<b>Kaolinite</b>
<b>0.5 – 1.0</b>	<b>Illite</b>
<b>1.0 – 7.0</b>	<b>Montomorillonite</b>



### Example

The following data were obtained from the liquid & plastic limits tests for a soil with  $\omega_n = 15\%$

Liquid limit test		Plastic limit test
No. of blows	Moisture content; $\omega$ %	
15	42	P.L = 18.7 %
20	40.8	
28	39.1	

### Required

- Draw the flow curve & find the liquid limit.
- Find the plasticity index of the soil
- Find L.I, C.I, F.I, T.I

**Solution**

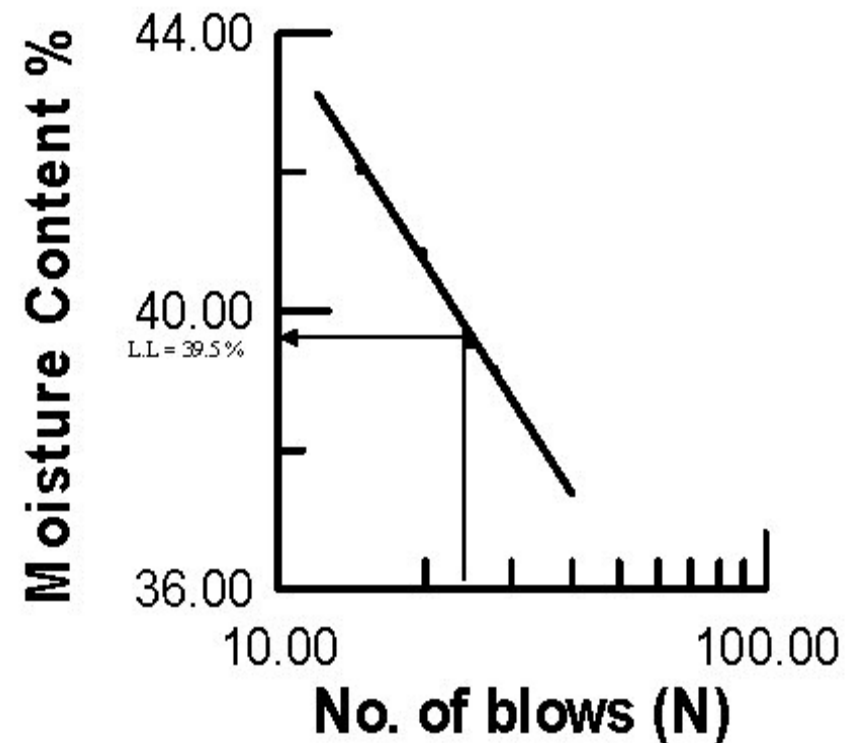
$$P.I = L.L - P.L = 39.5 - 18.7 = 20.8$$

$$L.I = \frac{\omega_n - P.L}{P.I} = \frac{15 - 18.7}{20.8} = -0.178 < 1$$

$$C.I = \frac{L.L - \omega_n}{P.I} = \frac{39.5 - 15}{20.8} = 1.178$$

$$F.I = \frac{42 - 40.8}{\log 15 - \log 20} = -9.6$$

$$T.I = \frac{P.I}{F.I} = \frac{20.8}{9.6} = 2.167$$

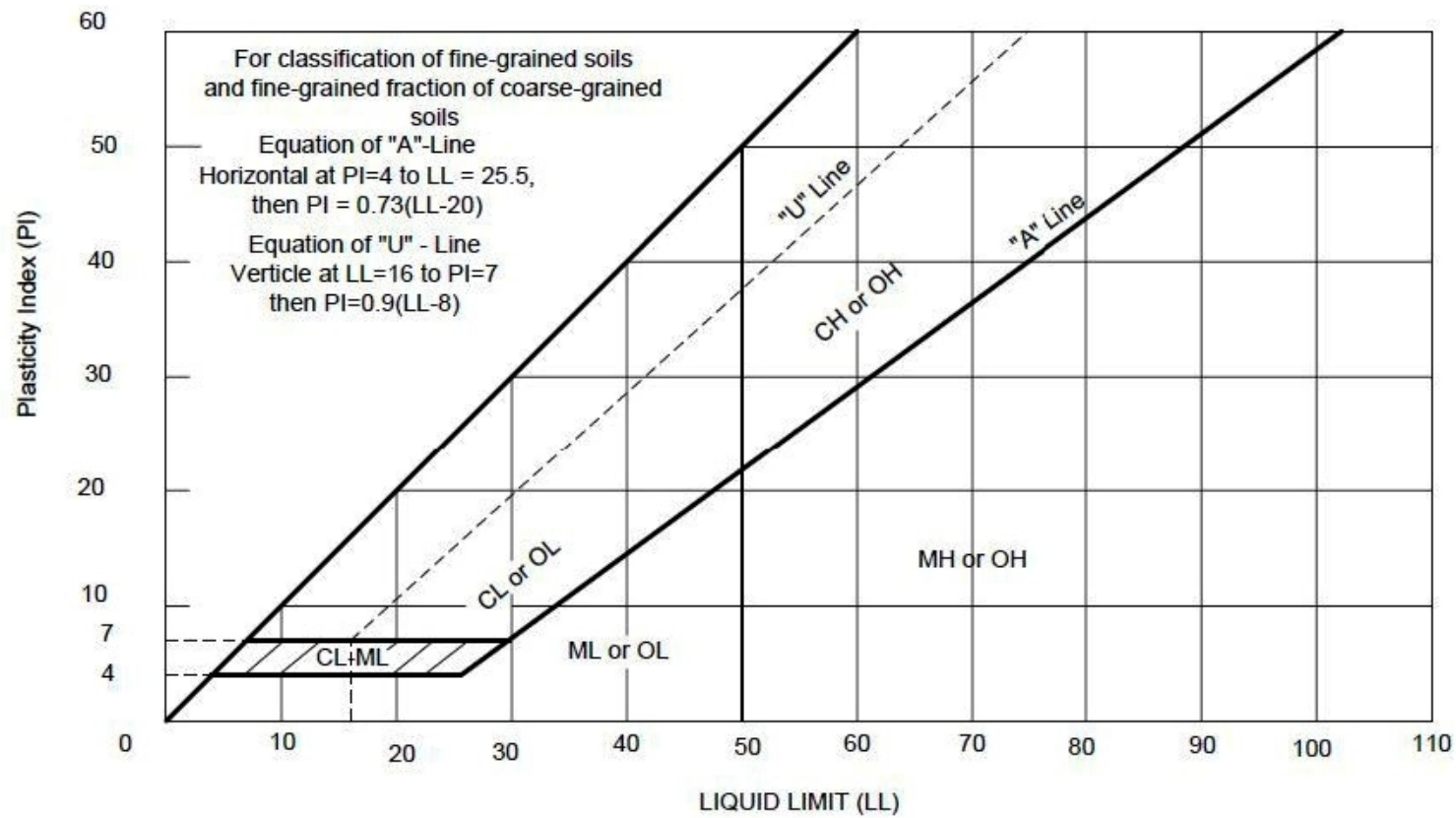


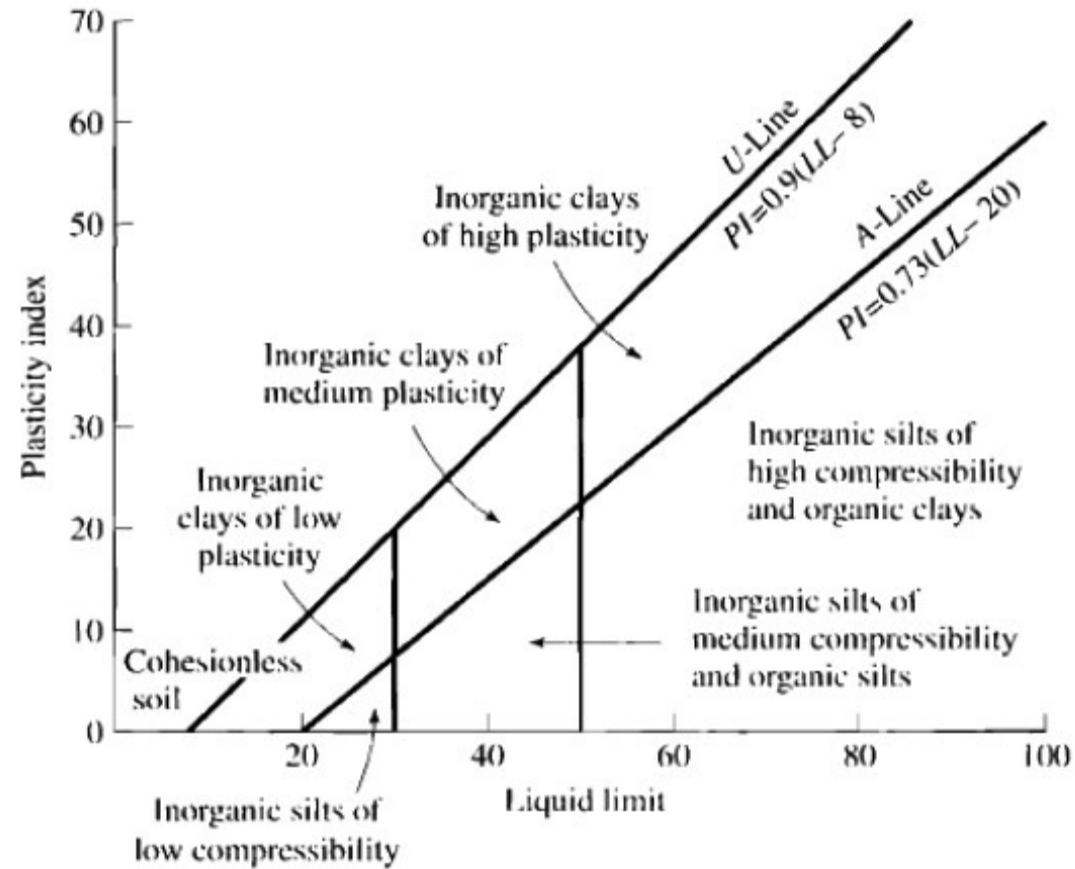
The soil is heavily preconsolidated since  $\omega_n$  is smaller than P.L & lower than L.L.



# Plasticity Chart

## Casagrande (1932)







## ***Soil Structure and Fabric***

In geotechnical engineering, the structure of a soil affects or governs the engineering behavior of particular soil and is taken to mean both –

1. ***Geometric arrangement*** of the particles or mineral grains with respect to each other (soil fabric).
2. ***Interparticle forces*** which may act between the particles or minerals grains. They probably have two main causes : *Orientation of the adsorbed water and Cementation*

## **Factors that affect the soil structure are-**

- The shape, size, and mineralogical composition of soil particles,
- The nature and composition of soil water.





## Structures in Cohesionless Soil

The structures generally encountered in cohesionless soils can be divided into two major categories:-

1. *Single – grained structure*
2. *Honeycombed structure*

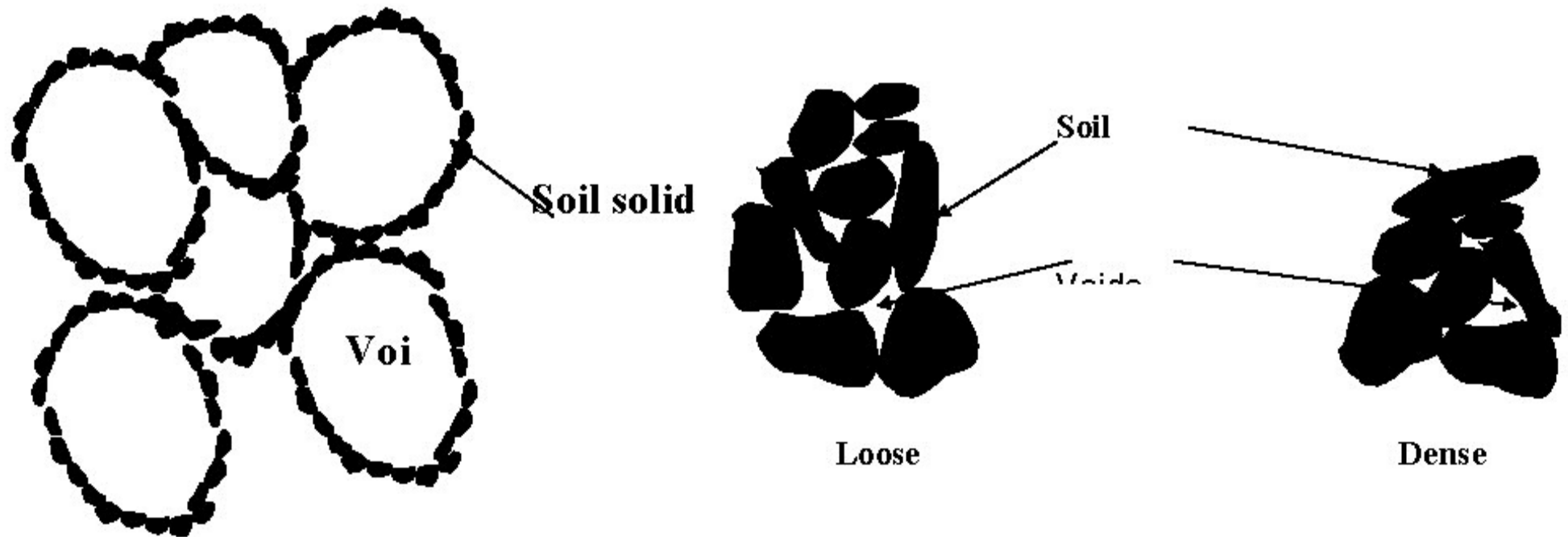
### *Single – grained structure*

A useful way to characterize the density of a natural granular soil is with relative density  $D_r$  as described before.

### *Honeycombed structure*

In this structure, relatively fine sand and silt form small arches with chains of particles as shown in the figure below. Soils exhibiting honeycombed structure have large void ratios and they can carry the ordinary static load.

However, under heavy load or when subjected to shock loading, the structure breaks down, resulting in large settlement.



## Structures in Cohesive Soils

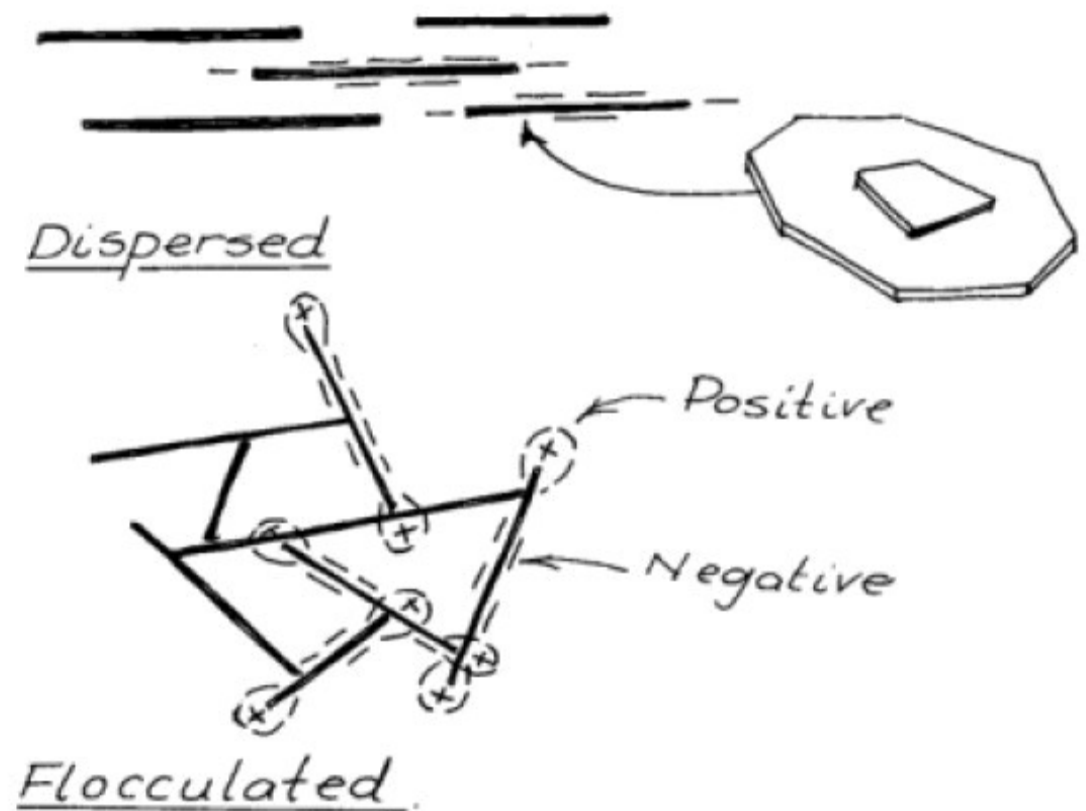
### 1. Dispersed structure

### 2. Flocculated structure

The interparticle forces are relatively large, so that the interparticle forces and the geometric arrangement of the grains will make the structure in cohesive soils.

If two particles approach each other in a suspension, the forces acting on them are

1. the Van der Waals forces of attraction, and
2. the repulsion between the two positively ionised adsorbed layers.



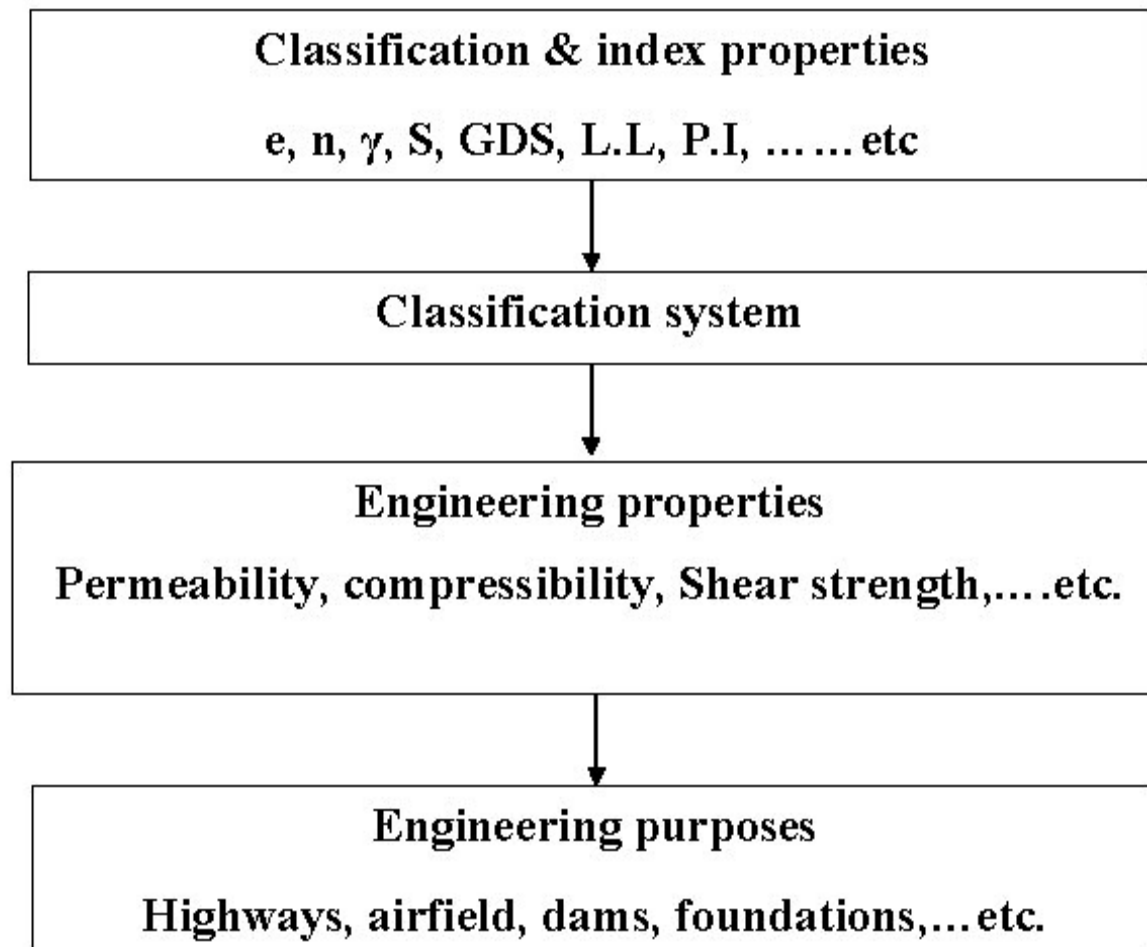
## *Soil Classification*

### *Introduction*

A soil classification system-

- ◆ It is the arrangement of different soils with similar properties into groups & subgroups based on their application or to their probable engineering behavior.
- ◆ It provides a common language to briefly express the general characteristics of soils, which are infinitely varied, without detailed descriptions.
- ◆ Most of the soils classification systems that have been developed for engineering purposes are based on simple index properties such as *particle size distribution & plasticity*.
- ◆ Although there are several classification systems now in use, none is totally definitive of any soil for all possible applications, because of the wide diversity of soil properties.

The role of classification system in geotechnical engineering practice is-



## **A- Textural classification**

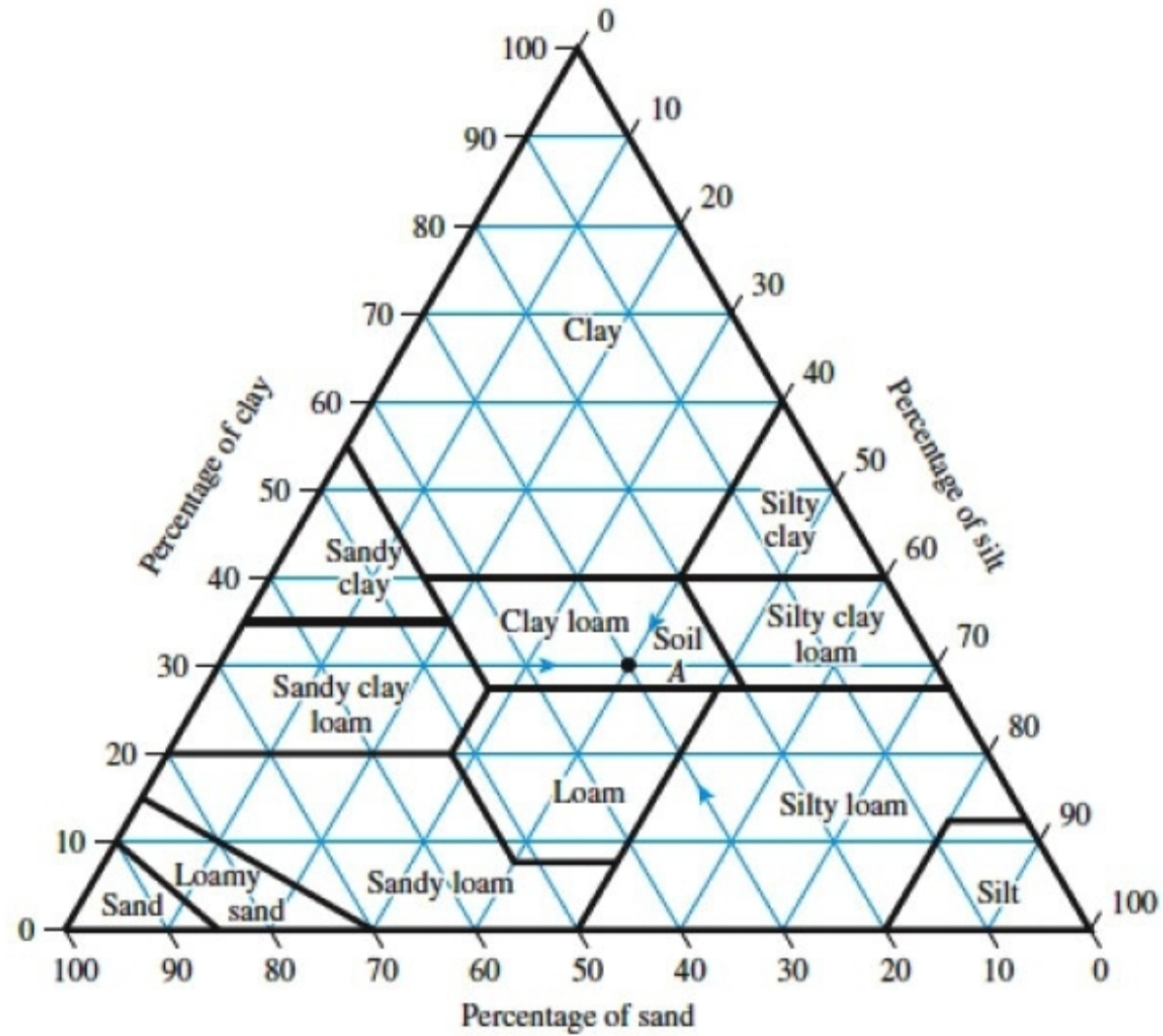
In general classification systems divided soils into the following categories on the basis of particle size. *Gravel; Sand; Silt; and Clay,*

but the nature of soils are mixtures of particles from several size groups, so if we know the principle components of the soils, we can name the soils such as Sandy Clay, Silty Clay ; and so forth.

One of these systems is the system developed by AASHTO (American Association of State Highway and Transportation Official).the the following chart is used to classify the soil, It is based on the particle size limits

Sand – size	2.0 – 0.075	mm in diameter
Silt – size	0.075 – 0.002	mm in diameter
Clay – size	smaller than 0.002	mm in diameter







The chart is based only on the fraction of the soil that passes through the no. 10 sieve. Otherwise, a correction will be necessary if a certain percentage of the soil particles are larger than 2 mm in diameter, as shown below-

The modified textural composition are-

$$\text{Modified \% Sand} = \frac{\%sand}{100 - \%gravel} \times 100\%$$

$$\text{Modified \% Silt} = \frac{\%silt}{100 - \%gravel} \times 100\%$$

$$\text{Modified \% Clay} = \frac{\%clay}{100 - \%gravel} \times 100\%$$



Then the soil is classified by proceeding in the manner indicated by the arrows & the soil named according to the zone that falls in it as shown in the following example.

**Example**

**Given**

	Particle – size distribution (%)			
<i>Soil</i>	<i>Gravel</i>	<i>Sand</i>	<i>Silt</i>	<i>Clay</i>
A	0	18	24	58
B	18	<del>51</del> 62.2	<del>22</del> 26.83	<del>9</del> 10.96

**Required-**

Classify the soils using textural classification of AASHTO



Solution- Soil B percentages need to be corrected while percentages of soil A need no correction and we can use the % directly

Soil B

$$\text{Modified \% Sand} = \frac{51}{100 - 18} \times 100 = 62.2\%$$

$$\text{Modified \% Silt} = \frac{22}{100 - 18} = 26.83\%$$

$$\text{Modified \% Clay} = \frac{9}{100 - 18} = 10.96\%$$

Using AASHTO chart we classified the soil A as clay and soil B As gravelly Sandy loam



**Other classification systems**

1-AASHTO System

2-Unified Soil Classification System (USCS).At present, we will consider (USCS) only

<b>AASHTO</b>	<b>BOULDERS</b>	<b>GRAVEL</b>	<b>SAND</b>			<b>SILT</b>	<b>CLAY</b>	<b>COLLOIDAL</b>
			<b>COARSE</b>	<b>MEDIUM</b>	<b>FINE</b>			
	75	4.75	2	0.425	0.075	0.005	0.001	

<b>USCS</b>	<b>BOULDERS</b>	<b>COBBLES</b>	<b>GRAVEL</b>		<b>SAND</b>			<b>FINES (SILT &amp; CLAY)</b>
			<b>COARSE</b>	<b>FINE</b>	<b>COARSE</b>	<b>MEDIUM</b>	<b>FINE</b>	
	300	75	19	4.75	2	0.425	0.075	

## **Unified Soil Classification System (USCS)**

Casagrande in 1942 during World War 2, it was revised in 1952. At present, it widely used among engineers.

This system classifies soils under two broad categories

- 1- **Coarse – grained soils** that are gravelly and sandy in nature with less than 50% passing through the no.200 sieve. The group symbols start with prefixes of either **G** or **S**. besides cobble and boulder without the symbol.(see the table in your notes)
- 2- **Fine – grained soils** with 50% or more passing through the no. 200 sieve. The group symbols start with prefixes **M**; **C**; **O** & **Pt**. (see the tables in your notes).

Other symbols used for the classification are –

**W** – well graded

**P** – poorly graded





**L** – low plasticity ( $L.L < 50\%$ )

**H** – high plasticity ( $L.L > 50\%$ )

So the group symbols may be one of the followings for-

- *Coarse – grained soils*

**GW , SW    GW – GM , SW – SM    GM , SM**

**GP , SP    GW – GC , SW – SC    GC , SC**

**GP – GM , SP – SM**

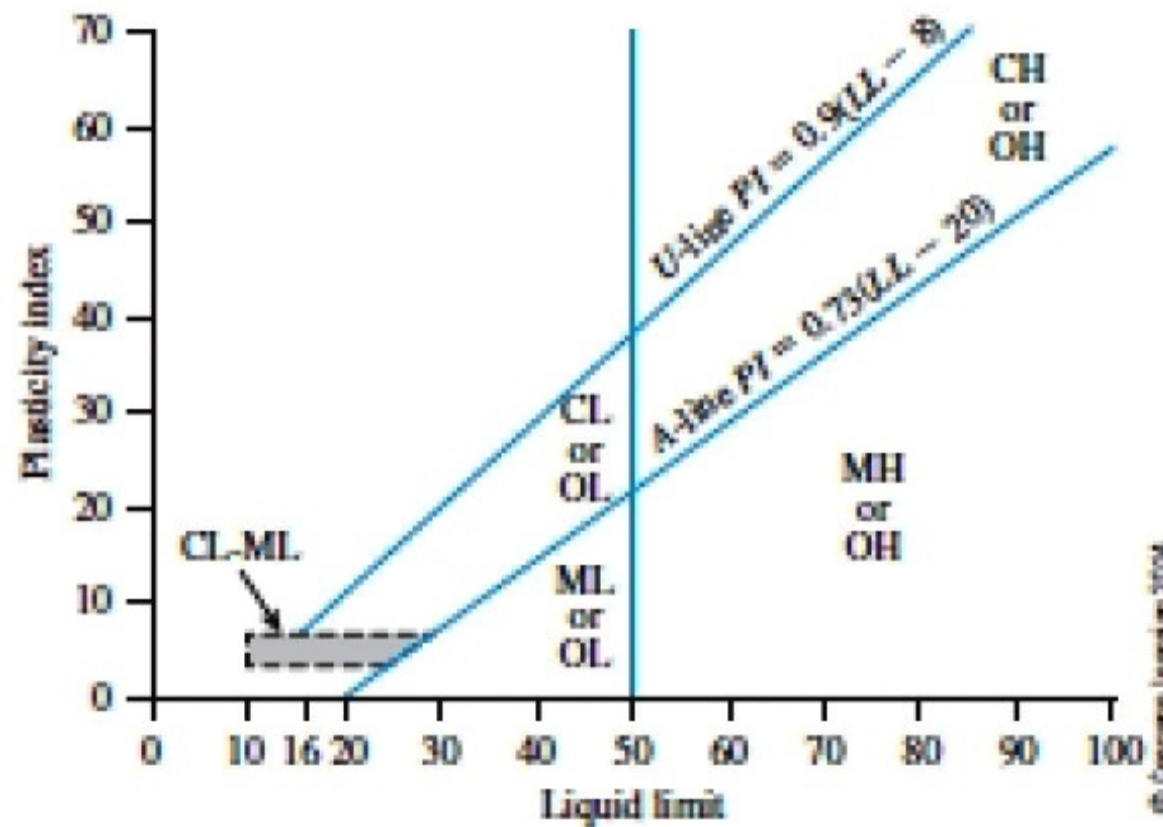
**GP – GC , SP – SC**

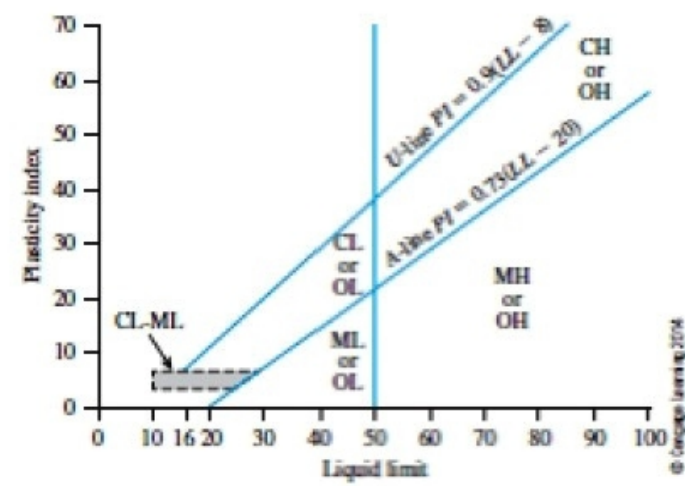
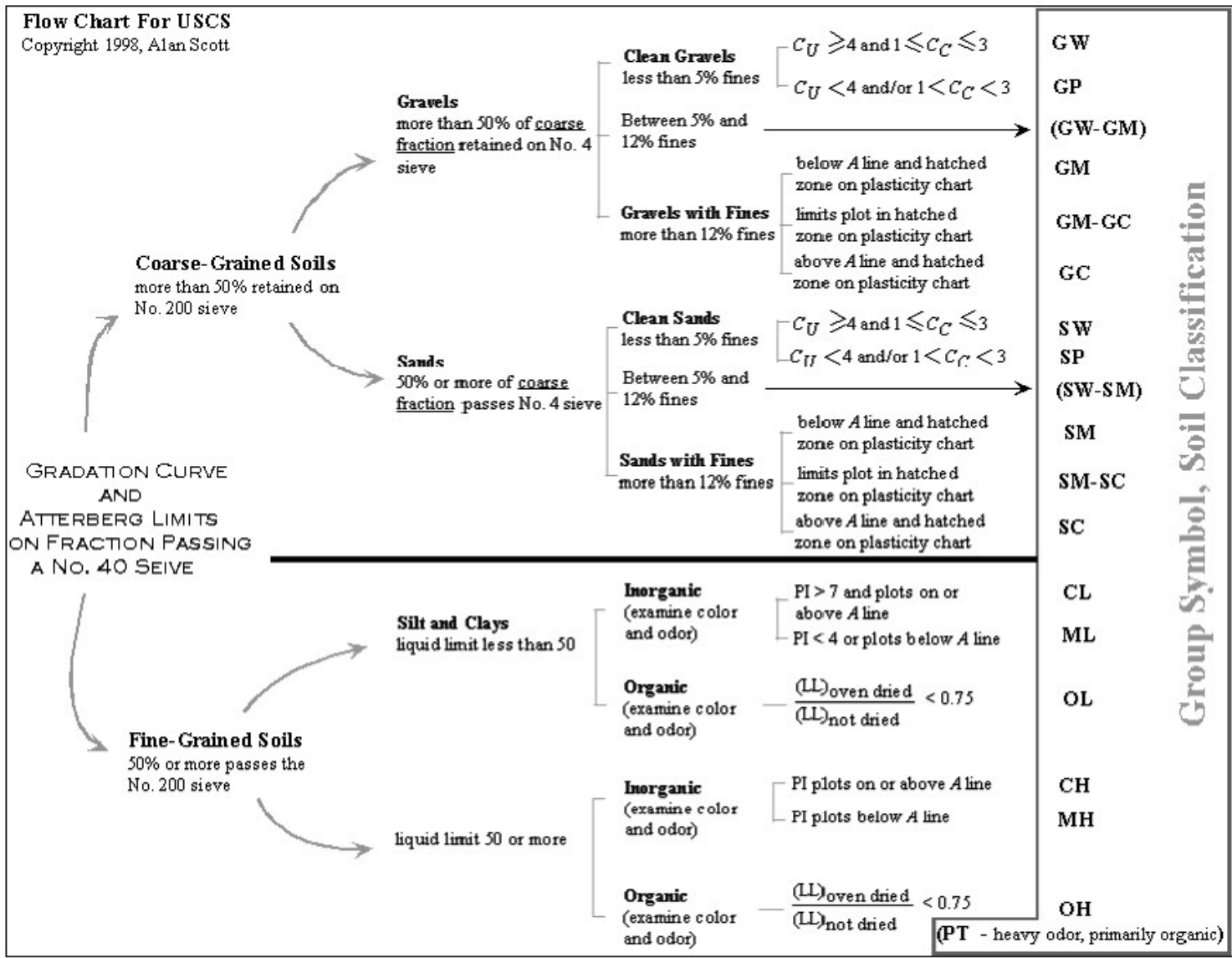
- *Fine – grained soils*

**CL , ML , OL    CH , MH , OH    CL – ML & Pt**



The plasticity chart used in USCS is shown below which is developed by Casagrande (1948) and modified to some extent here.







### Example

Following are the results of a sieve analysis and L.L & P.L tests for two soils

Sieve size	Soil 1 % passing	Soil 2 % passing
No.4 (4.75 mm)	99	97
No. 10 (2 mm)	92	90
No. 40 (0.475 mm)	86	40
No. 100	78	8
No. 200 ( 0.075 mm)	60	5
L.L	20	-
P.L	15	-
P.I	5	NP (Not Plastic)



## Required

Classify the soil according to USCS

## Solution

1-Plot the GSD curve for the two soils.

2-For soil, 1 % passing no. 200 sieve is greater than 50% so it is fine grained soil and by using plasticity chart the soil plots in the zone (CL – ML).

3-For soil 2 % passing no. 200 sieve is less than 50% so it is coarse – grained soil.

$F_1$  (% passing no. 4 & retained on No.200 sieve)

$$F_1 > \frac{100 - 5}{2} = 47.5\% \text{ so the symbol is S (Sand)}$$

Referring to the GSD curve we find  $D_{10} = 0.18 \text{ mm}$   $D_{30} = 0.34 \text{ mm}$   $D_{60} = 0.71 \text{ mm}$



$$C_u = \frac{D_{60}}{D_{10}} = 3.9 < 6; C_c = \frac{D_{30}^2}{D_{10} \cdot D_{60}} \cong 0.91 \approx 1$$

as  $C_u$  &  $C_c$  does not meet the requirements of well-graded the soil is poorly graded, the symbol will be SP, but since % passing no. 200 sieve = 5% the soil will take a dual symbol since the soil is NP so the symbol is SM

so the symbol will be SP – SM.