

## Measures of association

## DEFINITION OF BASIC TERMS

**Risk:** A probability that an individual will become ill or die within a specified period of time or age. It is used to denote incidence rate.

**Risk factor:** It can be defined as:

- a. **Risk marker.** An attribute or an exposure that is associated with an increased risk of disease or other specific outcome.
- b. **Determinant.** An attribute or exposure that increases the risk of disease or other specific outcome.
- c. **Modifiable risk factor.** A determinant that can be modified by an intervention thereby reducing the risk of disease or other specific outcome.

Estimate the association between ( exposure ) and ( disease ) using the frequency measures of the two population being compared . So to aid in the calculation of measure of association , epidemiological data are often presented in the form of ( 2x2 ) table ( four fold , contingency table ) .

	Disease yes +	Non- disease No	
Exposed yes +(study population )	a	b	a+b
Non-exposed (control population )	c	d	C+d
	a+c	b+d	Total a+b+c+d

Incidence rate in exposed ( study population ) =  $a / a+b$  .

Incidence rate in non-exposed ( control population ) =  $c / c+d$  .

RR=  $a/a+b / c/c+d$  .

Mean , number of observation in which the occurrence of interest is found / total number of observation .

NOTE:- risk factor present ( study population ) .

Risk factor absent ( control population ) .

Now if , we put study and control population above the table and disease , no disease beside , what happened .

	Study(exposed)	Control (no exposed)	
disease	a	b	A+b
No disease	c	d	C+d
total	A+c	B+d	

Incidence rate in exposed ( study population ) =  $a/a+c$  .

Incidence rate in non- exposed ( control population ) =  $b / b+d$  .

RR=  $a/a+c / b/b+d$  .

E.g, suppose the incidence of ( Hepatitis –B ) sero+ among those having previous blood transfusion is 5/1000/ year and those with no blood transfusion is 1/1000/ year . So what do such number give us ?

Blood transfusion ----- exposure .

Hepatitis –B ----- outcome .

So what is the magnitude of association between exposure and outcome .

The magnitude of association between exposure and outcome calculated by the ( Relative Risk and Attributable Risk ) , are the two most frequently used in epidemiology .

( Relative Risk ) ( RR )

Estimate the magnitude of association between exposure and outcome , or indicate the probability of developing the disease in the exposed relative to those unexposed .

So the exposure = risk factor .

Outcome= disease or death .

RR=  $I_e / I_{e-}$  . so(  $I_e$  ) incidence rate among exposed / (  $I_{e-}$  ) incidence rate among non- exposed .

$$\text{Relative risk (RR)} = \frac{\text{Incidence rate among exposed}}{\text{Incidence rate among non exposed}}$$

$I_e = a/a+b$      $I_{e-} = c/c+d$     so  $RR = a/a+b/c/c+d$  . so RR= incidence in exposed /incidence in non-exposed ( calculate from cohort study )

So by going back to the Hepatitis –B e.g .

RR= 5/1000/year / 1/1000/year= 5 times (probability of developing an outcome among the exposed compared to the non-exposed ) .

If RR=1 ( Mean no association between exposure and risk of disease ) .

If RR> 1 ( Positive association , mean increase risk among exposed ) .

If RR<1 ( Negative association , mean decrease risk among exposed ) .

(  $I_e > I_{e-}$  ) risk factor .

(  $I_e < I_{e-}$  ) protective factor .

So RR provides information that can be used in the judgment of causality .

RR , in study design, can be directly calculate only in a cohort study or experimental study ( clinical trial ) . Because incidence can not be estimated from a ( case- control ) study , RR can not be calculate directly from a case- control study , under some circumstances , the RR , in a case- control study can be estimated by the odds ratio ( OR ) .

So OR=  $ad/bc$  .

So disease x non- disease ----- case- control study .

Exposure x non- exposure ----- cohort study .

E.g, Data from a ( cohort study ) of oral contraceptive use and bacteruria among women aged ( 16- 49 ) years .

	Bacteruria	no-bacteruria	
	Yes +	No -	
OC used yes +	27	455	482
No OC used	77	1831	1908
total	104	2286	2390

Cohort study , mean incidence and start from exposure .

$I_e = 27 / 482 \times 1000 = 56.02 / 1000 / \text{year}$  .

$I_{e-} = 77 / 1908 \times 1000 = 40.36 / 1000 / \text{year}$  .

$RR = I_e / I_{e-} = 56.02/1000 / 40.36/1000 = 1.39$  ( no unit ) . so 1.39 times more is the risk of developing bacteruria in the exposed group ( taking oral contraceptive pills ) than not taking OC .

E.G- Data from a case-control study of current oral contraceptive use and ( myocardial infarction ) in premenopausal female nurses .

NOTE. When researcher used case- control study means start from diseases , and can estimate percentage .

	MI ( YES)	NO (MI)	
OC used (yes)	23	304	327
(NO) OC used	133	2816	2949
total	156	3120	3276

SO,  $OR = ad/bc = 23 \times 2816 / 304 \times 133 = 1.6$  . those who are on OC used have a (1.6) times risk to have MI than those who do not take OC . So very important to know the type of study ( cohort or case- control ) study why ? Just observe the following .

EG, A hypothesis case- control study of cigarette smoking and lung cancer

	Case (yes) CA lung	Control (no) CA lung	
Smoking (yes)	70	30	100
(no) smoking	30	70	100
	100	100	200

$OR = ad/bc = 70 \times 70 / 30 \times 30 = 5.4$ .

But  $RR = 70/100 / 30/100 = 2.3$  .

The same example above but ( 100 cases and 1000 control ) , increase number of control ( هنا جانز في الدراسة ) .

	CA lung (yes) cases	(NO) CA lung control	
Smoking (yes)	70	300	370
(no) smoking	30	700	730
	100	1000	1100

$OR = ad/bc = 70 \times 700 / 300 \times 30 = 5.4$  ( the same above ) .

But  $RR = 70/370 / 30/ 730 = 4.6$  Change .

So OR is more stable estimate than RR in case-control study , therefore RR is not beneficial in case-control study .

Second ( Attributable risk ) ( AR ) .

Also called ( risk difference , excess risk , and rate difference ) .

It is provide information about the absolute effect of the exposure , i.e – the excess risk of disease among the exposed compared to the non-exposed .

$AR = I_e - ( I_{e-} ) = a/a+b - c/c+d$

$AR = \text{Incidence rate exposed} - \text{Incidence rate in non-exposed}$  , calculate in (cohort study ) . Back to hepatitis –b e.g .

**AR= 5/1000/year – 1/1000/year= 4/1000/year . ( absolute measure , effect of the exposure ) . The value of AR indicate the number of cases of the disease among the exposed that can be attribute to the exposure itself .**

**OR, The number of cases of the disease among the exposed that could be eliminated if the exposure was eliminated .**

**Now returned back to Bacteriuria and OC table , so**

**AR=Ie-(Ie-) = 56.02/1000/year- 40.36/1000/year=15.66/1000/year .**

**So 15.66/ 1000/year ---- 1566/100000/year are attributable to OC use among the group who are exposed .**

**Note :- AR is only calculated from cohort study and can not calculated from case-control study . The value of RR dose not necessarily give an idea about the AR , if I have a higher RR dose not mean the AR is high and vice- versa .**

**Not:- if AR=0 (ZERO) , exposure has no relation .**

**If AR> 0 , exposure has relation to the out come .**

**If AR<0 , exposure is protective . e.g ( vitamin supplementation)or ( good personal hygiene ) or ( vaccination ) .**

**E.G:- Annual mortality rate per 100000 , one exposure and two outcome.**

	CA LUNG	CHD
Cig, smoking	140	669
Non-smoking	10	413
RR	14	1.6
AR	130/100000/year	256/100000/year

**Her give us direct incidence .**

**This is a cohort study the exposure is smoking , the outcome is either lung cancer or CHD .**

**RR= Ie/ Ie- = 140/ 10 = 14 in CA lung .**

**RR= Ie-Ie- = 669/ 413=1.6 in CHD .**

**SO 14 mean a person who smokers will have a 14 times chance to die from lung ca than non- smoker . 1.6 times chance to die from CHD than a non- smoker .**

**So 1.6 times chance to die from CHD than a non- smoker .**

**But , AR=Ie-(Ie-), smoking leading to lung CA , 140-10=130/100000/year**

**Smoking leading to CHD , 669-413=256/100000/year .**

**So more smokers die due to CHD than from lung CA . If I wanted to do a public health program to decreases death rates due to smoking , I would choose death due to CHD , because CHD has a higher incidence , according to the table , so financial and personal would be distributed on preventing death of smokers due to CHD .**

**THIRD, Attributable risk percent ( AR% ) .**

**Estimates the proportion of the disease , among the exposed that is attributable to the exposure . Gives an idea about the proportion of the disease in the exposed that could be prevented by eliminating the exposure .**

**IR among exposed – IR among non exposed**

**Percentage reduction = ----- X 100**

**IR among exposed**

**AR%=AR/Iex100%.**

**AR%=Ie-(Ie-) / Iex100% . ( calculated in cohort study ) .**

**But in case- control study , AR%=OR-1/ORX100% .**

**FOURTH , Population attributable risk. (PAR) .**

PAR predicts the reduction in risk achievable if a risk is removed from a population . Estimates the excess rate of disease in the total study population of exposed and non-exposed individuals that is attributable to the exposure or helps to determine which exposure have the most relevance affect to the health of a community . It is calculated by multiplying AR by prevalence of exposure to the risk factor .

**PAR= ARX Proportion of population exposed ( prevalence of exposure).**

**( prevalence of exposure in the total population , from an external source , or that of the study population if it representative the general population .**

**E.G:-Consider a cohort study of decompression illness (DCI) , taken in one year , with 500 divers with a variation in heart anatomy known as a patent foramen ovale (PFO) controlled against 500 divers without a (PFO) . The result are summarized as follows .**

	DCI( disease)	No(DCI) NO disease	total
PFO(Exposed)	2	498	500
No PFO(Non-exposed)	1	499	500

**OR .**

	PFO(exposed)	No PFO(non-exposed)(control)	
DIC	2	1	
No DIC	498	499	
TOTAL	500	500	

It is widely believed that a POF , or any other right –to-left circulatory shunt , increases the risk of DIC . Some 30% of individuals within the general population have a POF , and some surveys have shown that a similar proportion of divers have a POF . Calculated

**a- RR.**

**b-AR.**

**c-AR% .**

**d-PAR .**

**NOTE :-**

**1- When the disease is rare so  $a/a+b = a/b$  and  $c/c+d = c/d$  , therefore the odds ratio closely approximates the RR if the disease is rare . when there is chronic disease , but low prevalence ( less than 10% )  $OR=RR$  .**

**E.G :- In a study about lung CA in smokers , (90) cases of lung CA , were diagnosis in smokers in a population of ( 100000) person . these figures were compared to only (7) cases of lung CA among non-smokers . This study was performed in a population known to be of low smoking prevalence , where the prevalence of smoking was only (2%) calculated :- a- RR , b-AR , c-AR% , d-PAR .**

**Q/4 . What is risk ?**

**Risk --- probability of an event to occur . ( this event is either dangerous or not ) .**

**Q/5. What is the difference between a risk and a rate ?**

**Rate mathematical expression between 2 variables , so it is the only measure that represent the risk . Any rate must have three measures . 1- It is a proportion 2- Time factor 3- Population at risk .**