

## FIRST AND FOLLOW

The construction of a predictive parser is aided by two functions associated with a grammar G. The functions **FIRST** and **FOLLOW** allow us to fill in the entries of a predictive parsing table for G.

Ex. 1:-

A. Give the predictive parsing table for the following grammar:-

$$E \rightarrow E+T/T$$

$$T \rightarrow T*F/F$$

$$F \rightarrow (E)/id$$

B. Show the moves of the parser for the input (id+id) \* id

Solution:-

A. Elimination of left recursion:-

$$E \rightarrow TE'$$

$$E' \rightarrow +TE'/\epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT'/\epsilon$$

$$F \rightarrow (E)/id$$

Finding FIRST and FOLLOW:-

$$\text{FIRST}(E) = \text{FIRST}(T) = \text{FIRST}(F) = \{ (, id \}$$

$$\text{FIRST}(E') = \{ +, \epsilon \}$$

$$\text{FIRST}(T') = \{ *, \epsilon \}$$

$$\text{FOLLOW}(E) = \{ ), \$ \}$$

$$\text{FOLLOW}(E') = \text{FOLLOW}(E) = \{ ), \$ \}$$

$$\text{FOLLOW}(T) = \text{FIRST}(E') = \{ +, \epsilon \} + \text{FOLLOW}(E')$$

$$= \{ +, ), \$ \}$$

$$\text{FOLLOW}(T') = \text{FOLLOW}(T) = \{ +, ), \$ \}$$

$$\text{FOLLOW}(F) = \text{FIRST}(T') = \{ *, \epsilon \} + \text{FOLLOW}(T') = \{ *, +, ), \$ \}$$

So the Predictive Parsing table is,

T \ NT	id	+	*	(	)	\$
E	E → TE'			E → TE'		
E'		E' → +TE'			E' → ε	E' → ε
T	T → FT'			T → FT'		
T'		T' → ε	T' → *FT'		T' → ε	T' → ε
F	F → id			F' → (E)		

**B. Moves made by predictive parser on Input id+id\*id**

STACK	INPUT	OUTPUT
\$E	id + id * id\$	$E \rightarrow TE'$
\$E'T	id + id * id\$	$T \rightarrow FT'$
\$E'T'F	id + id * id\$	$F \rightarrow id$
\$E'T'(id	id) + id * id\$	Remove id
\$E'T'	+id * id\$	$T' \rightarrow \epsilon$
\$E'	+id * id\$	$E' \rightarrow +TE'$
\$E'T(+	+)id * id\$	Remove +
\$E'T	id * id\$	$T \rightarrow FT'$
\$E'T'F	id * id\$	$F \rightarrow id$
\$E'T'(id	id) * id\$	Remove id
\$E'T'	* id\$	$T' \rightarrow *FT'$
\$E'T'F(*)	*)id\$	Remove *
\$E'T'F	id\$	$F \rightarrow id$
\$E'T'(id	id)\$	Remove id
\$E'T'	\$	$T' \rightarrow \epsilon$
\$E'	\$	$E' \rightarrow \epsilon$
\$	\$	

**Ex.No:2:-** Give the Predictive parsing table for the following Grammar,

$$S \rightarrow iEtSS'/a$$

$$S' \rightarrow eS/\epsilon$$

$$E \rightarrow b$$

Solution:-

Elimination of Left Recursion

The above grammar has no left Recursion. So we move to First and Follow.

$$\text{First}(S) = \{i, a\}$$

$$\text{First}(S') = \{e, \epsilon\}$$

$$\text{First}(E) = \{b\}$$

$$\begin{aligned} \text{Follow}(S) &= \text{First}(S') = \{e, \epsilon\} + \text{Follow}(S') \\ &= \{e, \$\} \end{aligned}$$

Follow (E) = {t, \$}

Follow (S') = Follow(S) = {e, \$}

So the Predictive Parsing table is,

T NT	a	B	e	i	t	\$
S	$S \rightarrow a$			$S \rightarrow iEtSS'$		
S'			$S' \rightarrow eS$ $S' \rightarrow \epsilon$			$S' \rightarrow \epsilon$
E		$E \rightarrow b$				

**Ex.No:3:-** Give the Predictive parsing table for the following Grammar,

$S \rightarrow CC$

$C \rightarrow cC/d$

Solution:-

First(S) = First(C) = {c,d}

Follow(S) = { \$ }

Follow( C ) = First ( C ) = { c, d, \$ }

So the predictive parsing table is

T NT	c	d	\$
S	$S \rightarrow CC$	$S \rightarrow CC$	
C	$C \rightarrow cC$	$C \rightarrow d$	

**Ex.No:3:-** Give the Predictive parsing table for the following Grammar.

$$S \rightarrow iCtSS' / a$$

$$S' \rightarrow eS / \epsilon$$

$$C \rightarrow b$$

Solution:-

$$\text{FIRST}(S) = \{ i, a \}$$

$$\text{FIRST}(S') = \{ e, \epsilon \}$$

$$\text{FIRST}(C) = \{ b \}$$

$$\begin{aligned} \text{FOLLOW}(S) = \text{FIRST}(S') &= \{ e, \epsilon \} + \text{FOLLOW}(S') \\ &= \{ e, \$ \} \end{aligned}$$

$$\text{FOLLOW}(S') = \text{FOLLOW}(S) = \{ e, \$ \}$$

$$\text{FOLLOW}(C) = \{ t, \$ \}$$

So the predictive parsing table is

T NT	a	B	e	i	t	\$
S	$S \rightarrow a$			$S \rightarrow iCtSS'$		
S'			$S' \rightarrow eS$ $S' \rightarrow \epsilon$			$S' \rightarrow \epsilon$
C		$C \rightarrow b$				

## References

1. J. Tremblay, P.G. Sorenson, "The Theory and Practice of Compiler Writing ", McGRAW-HILL, 1985.
2. W.M. Waite, L.R. Carter, "An Introduction to Compiler Construction", Harper Collins, New York, 1993
3. A.W. Appel, "Modern Compiler Implementation in, Cambridge University Press, 1998
4. Internet Papers
5. Aho, R. Sethi, J.D. Ullman, " Compilers- Principles, Techniques and Tools" Addison-Wesley, 2007