

3.2.3 Double integrate over non rectangular regions

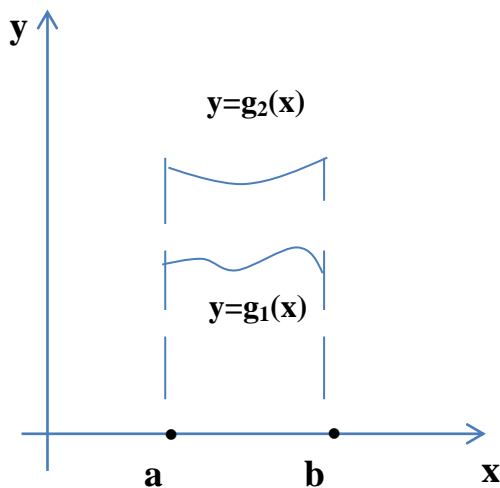
We will limit our study of double integral over non-rectangular regions to two basic types of regions , (type I , and type II)

Type I region : it is bounded on the left and right by vertical lines $x=a$ and $x=b$ it is bounded below and above by continuous curves $y=g_1(x)$ and $y=g_2(x)$

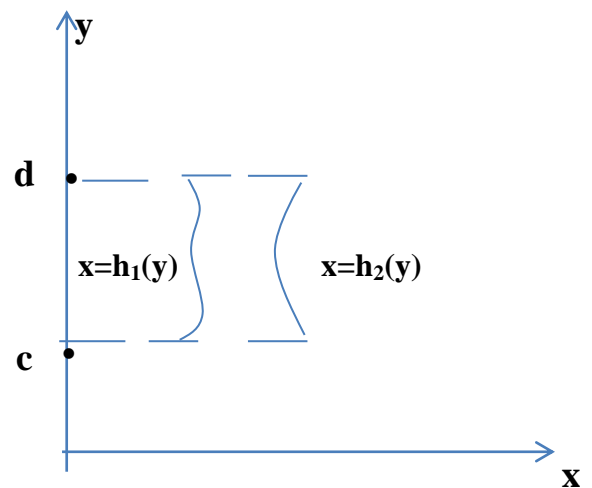
$$((g_1(x) \leq g_2(x) \text{ for } a \leq x \leq b))$$

Type II region : it is bounded below and above by horizontal lines $y=c$ and $y=d$ and it is bounded on the left and right by the curves $x=h_1(y)$ and $x=h_2(y)$

$$((h_1(y) \leq h_2(y) \text{ for } c \leq y \leq d))$$



Type I



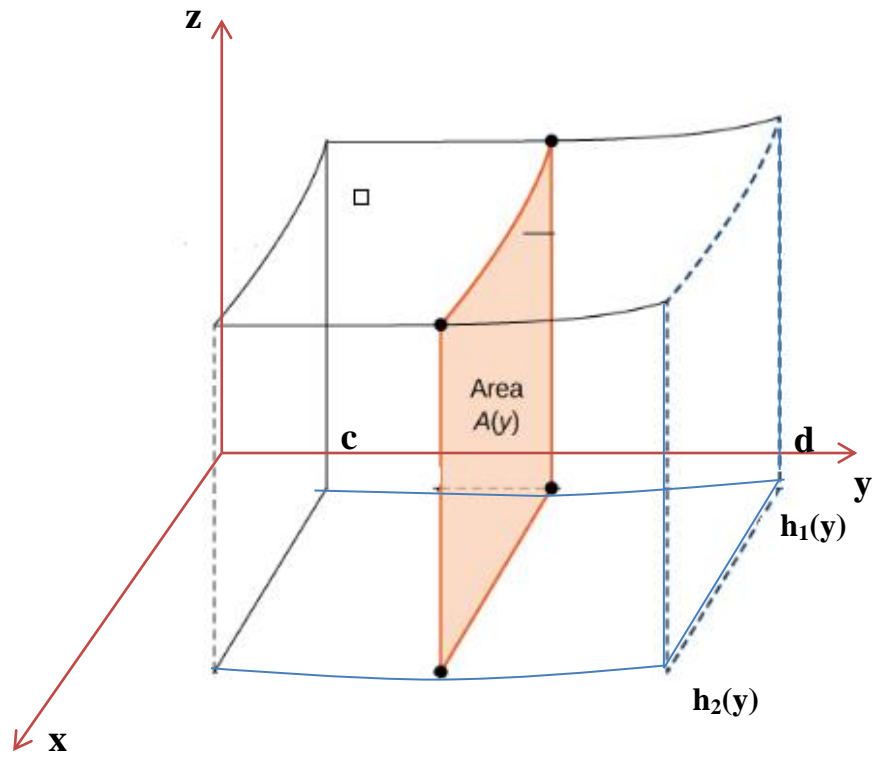
Type II

$$\iint_R f(x, y) dA = \int_a^b \int_{g_1(x)}^{g_2(x)} f(x, y) dy dx \quad \text{Type I}$$

$$\iint_R f(x, y) dA = \int_c^d \int_{h_1(y)}^{h_2(y)} f(x, y) dx dy \quad \text{Type II}$$

$$A(y) = \int_{h_1(y)}^{h_2(y)} f(x, y) dx$$

$$V = \int_c^d \int_{h_1(y)}^{h_2(y)} f(x, y) dx dy$$



$$A(x) = \int_{g_1(x)}^{g_2(x)} f(x, y) dy$$

$$V = \int_a^b \int_{g_1(x)}^{g_2(x)} f(x, y) dy dx$$

