

# Point Processing

image processing operations may be divided into into three classes based on the information required to perform the transformation.

1. **Transforms**: We require a knowledge of all the grey levels in the entire image to transform the image. In other words, the entire image is processed as a single large block. This may be illustrated by the diagram shown in figure (1)
2. **Spatial filters**: To change the grey level of a given pixel we need only know the value of the grey levels in a small neighborhood of pixels around the given pixel.
3. **Point operations**: A pixel's grey value is changed without any knowledge of its surrounds.

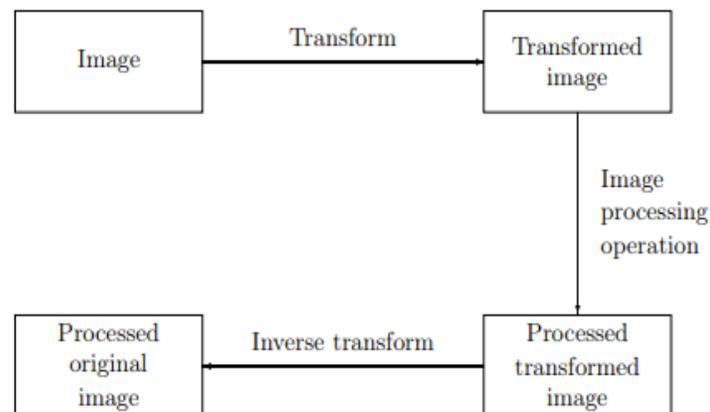


Figure (1): Schema for transform processing.

## **Arithmetic operations:**

These operations act by applying a simple function

$$Y=f(x)$$

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to each grey value in the image. Thus  $f(x)$  is a function which maps the range  $0 \dots 255$  on to itself.

Simple functions include adding or subtract a constant value to each pixel:

**1-Linear gray scale transformation:**

$$Y=x+c \text{ or } y=x-c$$

" or multiplying each pixel by a constant:

$$Y=cx$$

the values by setting:

$$y=255 \text{ if } y>255, \quad y=0 \text{ if } y<0$$

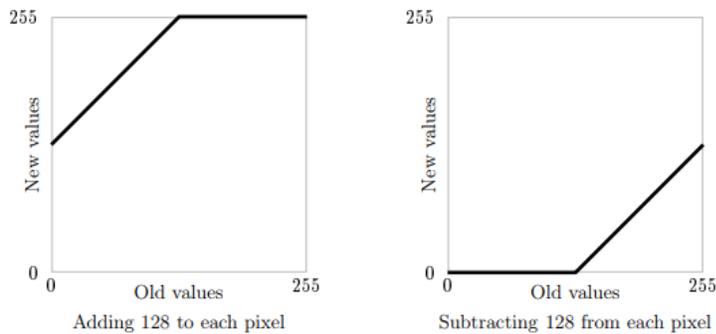
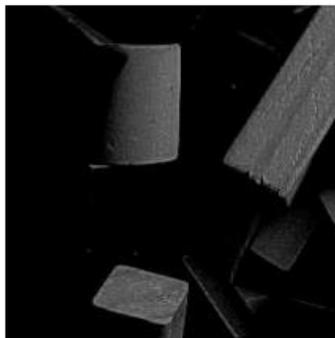


Figure (2): Adding and subtracting constant.



b1: Adding 128

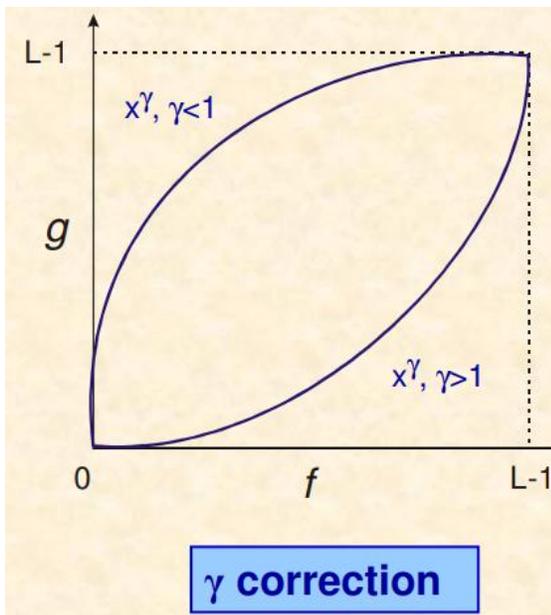
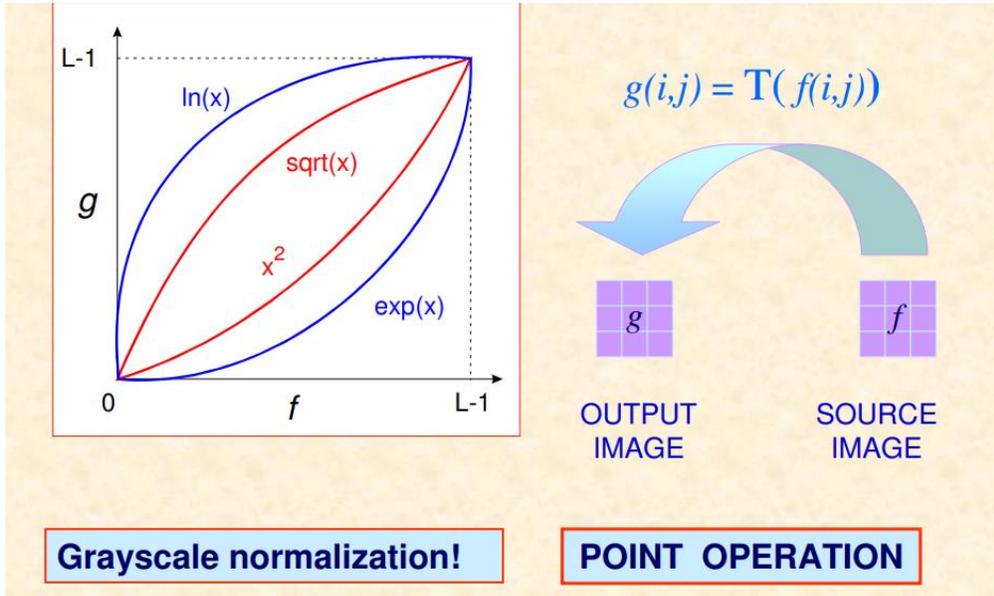


b2: Subtracting 128

Figure 3: Arithmetic operations on an image: adding or subtracting a constant.

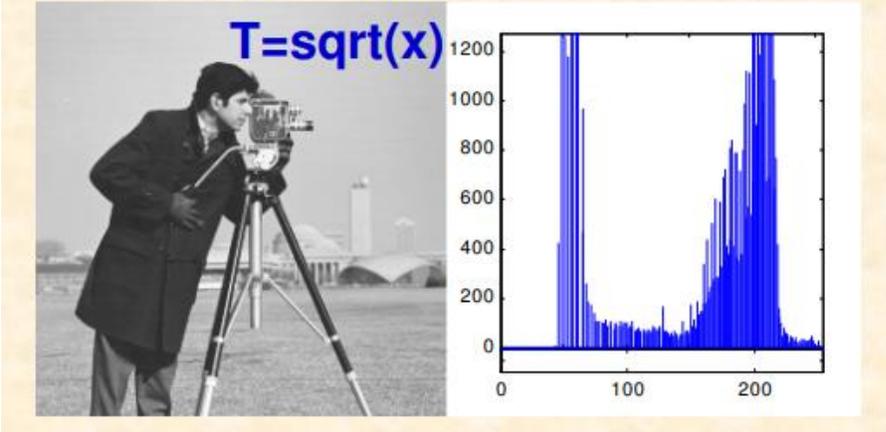
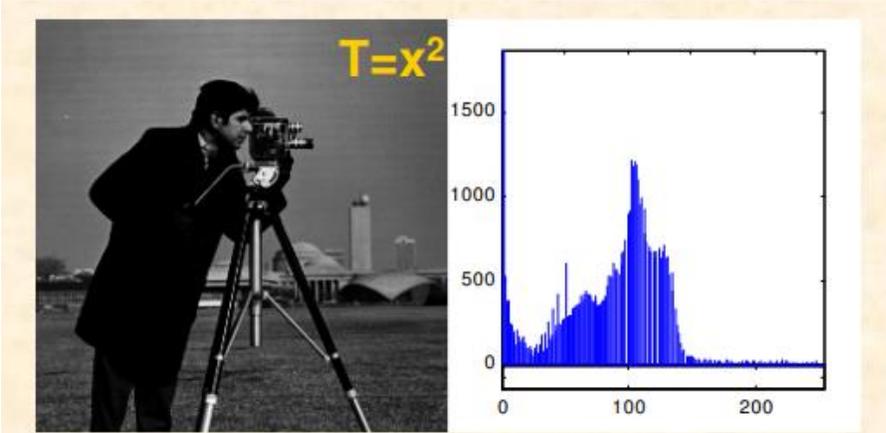
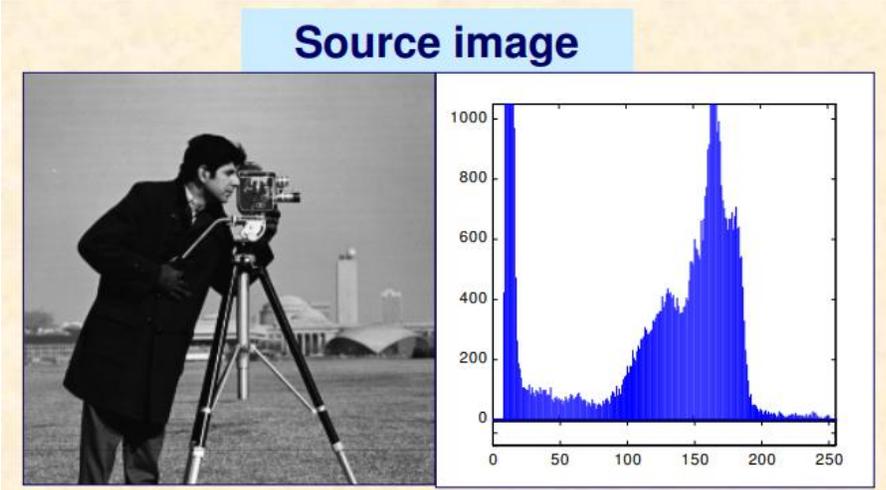
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## 2-Non Linear gray scale transformation:



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**Examples**



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## Histograms:

Given a greyscale image, its histogram consists of the histogram of its grey levels; that is, a graph indicating the number of times each grey level occurs in the image.

- In a dark image, the grey levels (and hence the histogram) would be clustered at the lower end:
- In a uniformly bright image, the grey levels would be clustered at the upper end:
- In a well contrasted image, the grey levels would be well spread out over much of the range.

There are **two** ways to enhance its contrast, by spreading out its histogram:

### 1- Histogram stretching (Contrast stretching):

Example :Suppose an image with the histogram shown in figure (4):

Gray level	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
$n_i$	15	0	0	0	0	70	110	45	70	35	0	0	0	0	0	15

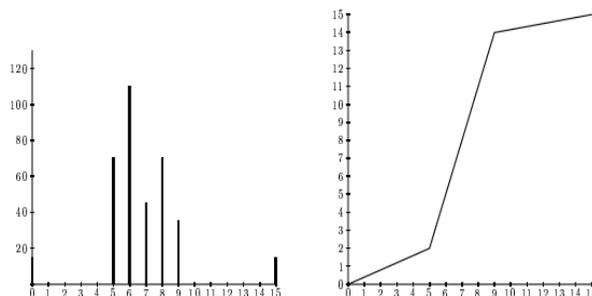


Figure 5: A histogram of a poorly contrasted image, and a stretching function.

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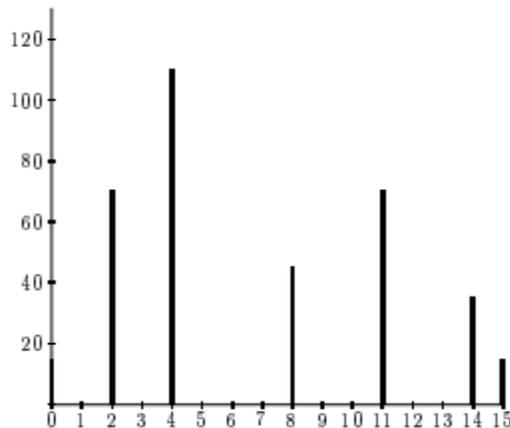
The gray level 5-9 according the gray level 2-14. Apply the equation to get the new gray level.

$$J = [(14-2)/(9-5)](i-5)+2$$

where i is the original grey level and j its result after the transformation

i	5	6	7	8	9
j	2	5	8	11	14

and the corresponding histogram:



## 2-Histogram Equalization:

Sometimes a better approach is provided by histogram equalization. To transform the grey levels to obtain a better contrast image, we change gray level I to

$$\frac{1}{n} (n_0 + n_1 + n_2 + n_3 + \dots + n_i)(L-1)$$

And this number is rounded to the nearest integer.

### **Example**

Suppose our images

Lect.9

Gray level	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
$n_i$	15	0	0	0	0	0	0	0	0	70	110	45	80	40	0	0

$$n_i = 15 + 0 + 0 + 0 + 0 + 0 + 0 + 0 + 0 + 0 + 70 + 110 + 45 + 80 + 40 + 0 + 0 = 360$$

$$L - 1 = 15$$

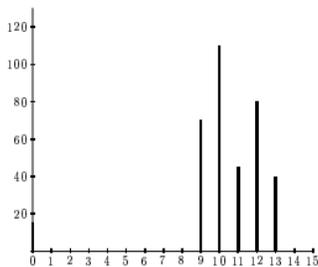
To equalize this histogram, we form running totals of the  $n_i$ ,

$$15/360 = 1/24$$

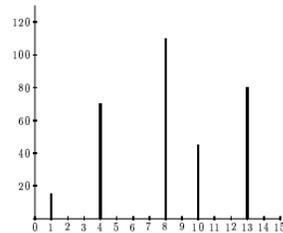
Grey level $i$	$n_i$	$\Sigma n_i$	$(1/24)\Sigma n_i$	Rounded value
0	15	15	0.63	1
1	0	15	0.63	1
2	0	15	0.63	1
3	0	15	0.63	1
4	0	15	0.63	1
5	0	15	0.63	1
6	0	15	0.63	1
7	0	15	0.63	1
8	0	15	0.63	1
9	70	85	3.65	4
10	110	195	8.13	8
11	45	240	10	10
12	80	320	13.33	13
13	40	360	15	15
14	0	360	15	15
15	0	360	15	15

We now have the following transformation of grey values, obtained by reading off the first and last columns in the above table:

Original grey level $i$	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Final grey level $j$	1	1	1	1	1	1	1	1	1	4	8	10	13	15	15	15

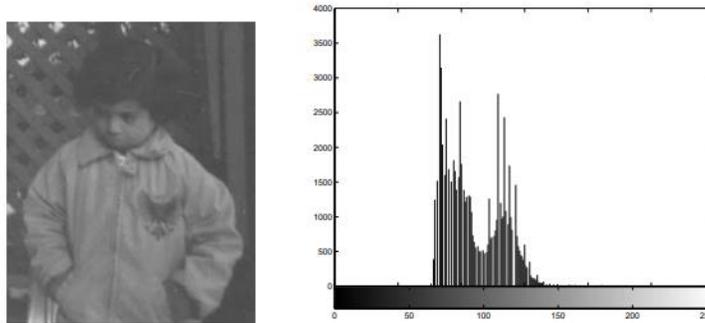


Before Histogram Equalization

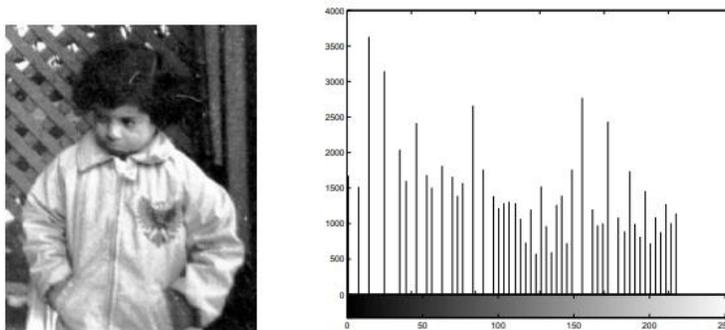


After Histogram Equalization

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Before Histogram Equalization



After Histogram Equalization

**Thresholding :**

**1 -Single thresholding:** A greyscale image is turned into a binary (black and white) image by first choosing a grey level in the original image, and then turning every pixel black or white according to whether its grey value is greater than or less than  $T$ :

A pixels become becomes white if its gray level  $> T$ .

A pixels become becomes black if its gray level  $\leq T$

Thresholding is a vital part of image segmentation, where we wish to isolate objects from the background. It is also an important component of robot vision.

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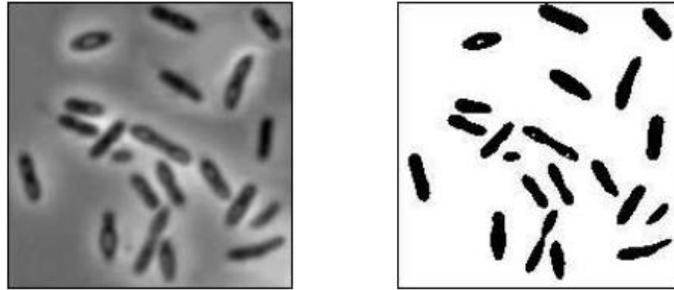


Figure (6): Thresholded image of bacteria at  $T > 100$

Thresholding provides a very simple way of showing hidden aspects of an image. For example, the image paper as shown in figure (7):

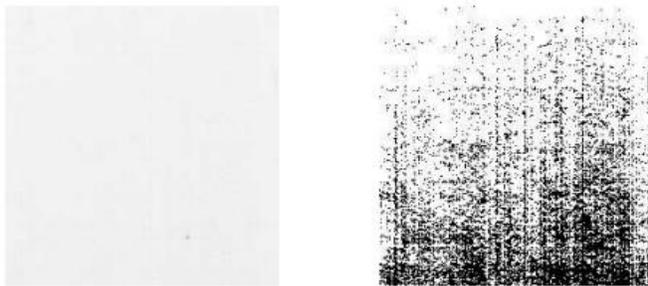


Figure (7): The paper image and result after thresholding.

## 2- Double thresholding:

Here we choose two values and  $T_1$  and  $T_2$  apply a thresholding operation.

A pixels become becomes white its gray level between  $T_1$  and  $T_2$ .

A pixels become becomes black if its gray level is otherwise.

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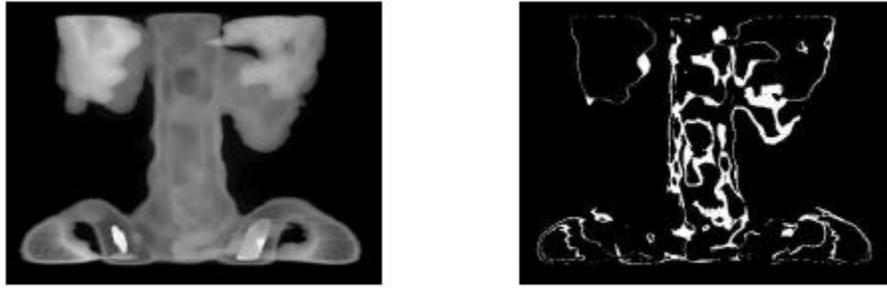


Figure (8): The image spins the result after double thresholding.

### Applications of thresholding:

1-To remove unnecessary detail from an image, to concentrate on essentials. But this information may be all we need to investigate sizes, shapes, or numbers of blobs.

2-To bring out hidden detail. This was illustrated with paper and spine images. In both, the detail was obscured because of the similarity of the grey levels involved.

3-When we want to remove a varying background from text or a drawing. We can simulate a varying background by taking the image text as shown figure (9).

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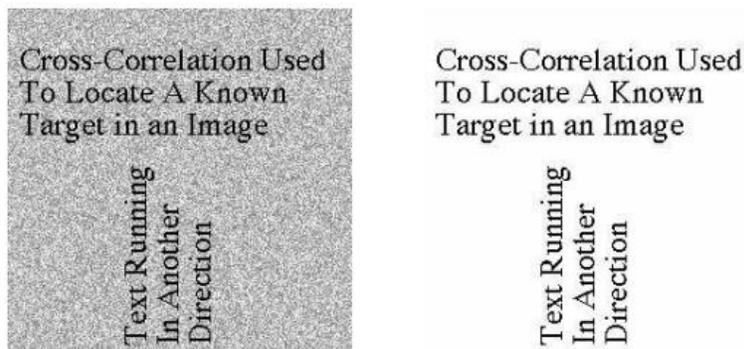


Figure (9): Text on a varying background, and threshold

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## Exercises :

1- Consider the following 8x8 image.

3	148	117	148	145	178	132	174
2	176	174	110	185	155	118	165
0	100	124	113	193	136	146	108
0	155	170	106	158	130	178	170
9	196	138	113	108	127	144	139
6	188	143	183	137	162	105	169
9	122	156	119	188	179	100	151
8	176	137	114	135	123	134	183

Threshold it at

(a) level 100

(b) level 150

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2,3

The following table gives the number of pixels at each of the grey levels 0-7 in an image with those grey values only:

0	1	2	3	4	5	6	7
3244	3899	4559	2573	1428	530	101	50

Draw the histogram corresponding to these grey levels, and then perform a histogram equalization and draw the resulting histogram.

The following tables give the number of pixels at each of the grey levels 0-15 in an image with those grey values only. In each case draw the histogram corresponding to these grey levels, and then perform a histogram equalization and draw the resulting histogram.

(a)

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
20	40	60	75	80	75	65	55	50	45	40	35	30	25	20	30

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(b)

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	40	80	45	110	70	0	0	0	0	0	0	0	0	15

9. The following small image has grey values in the range 0 to 19. Compute the grey level histogram and the mapping that will equalize this histogram. Produce an  $8 \times 8$  grid containing the grey values for the new histogram-equalized image.

```

12  6  5  13  14  14  16  15
11 10  8  5  8  11  14  14
 9  8  3  4  7  12  18  19
10  7  4  2  10 12  13  17
16  9 13 13 16 19 19 17
12 10 14 15 18 18 16 14
11  8 10 12 14 13 14 15
 8  6  3  7  9  11 12 12

```