

4-Reflection

If either the X or Y axis is treated as a mirror, the object has a mirror image or reflection. The reflected point P_{new} is located the same distance from the mirror (the axis) as the original point P.

4-1: Reflection on the X axis

1	0	0
0	-1	0
0	0	1

OR $X_{\text{new}} = X$
 $Y_{\text{new}} = -Y$

4-2: Reflection on the Y axis

-1	0	0
0	1	0
0	0	1

OR $X_{\text{new}} = -X$
 $Y_{\text{new}} = Y$

4-3: Reflection on the origin

-1	0	0
0	-1	0
0	0	1

OR $X_{\text{new}} = -X$
 $Y_{\text{new}} = -Y$

4-4: Reflection on the line $Y=X$

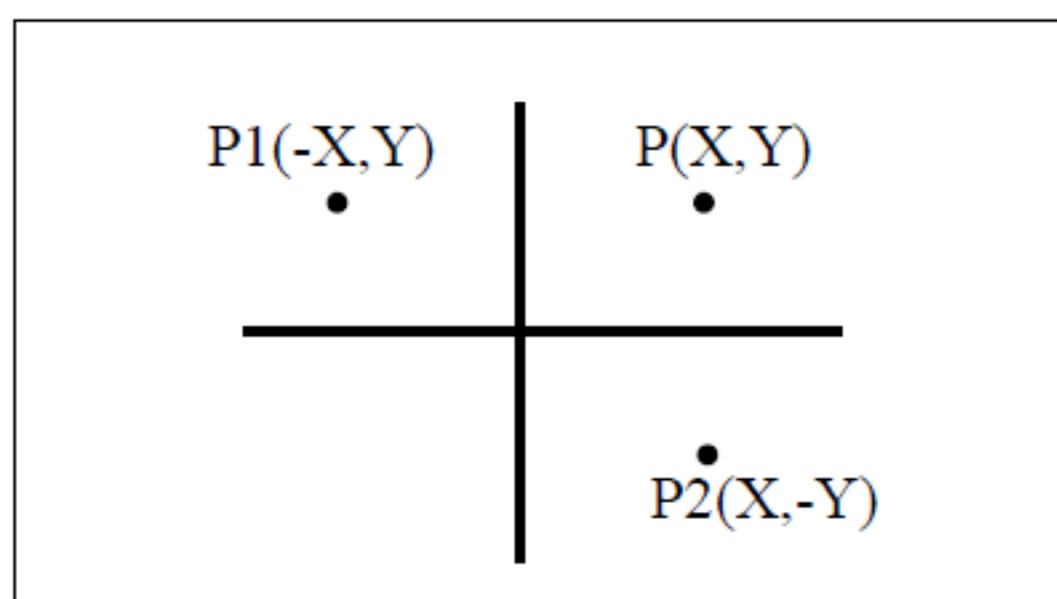
0	1	0
1	0	0
0	0	1

OR $X_{\text{new}} = Y$
 $Y_{\text{new}} = X$

4-5: Reflection on the line $Y=-X$

0	-1	0
-1	0	0
0	0	1

OR $X_{\text{new}} = -Y$
 $Y_{\text{new}} = -X$



Example 1: Reflect the point P(3,2) in :: a- X axis; b- Y axis; c-origin; d-line Y=X;

Solution : a-

$$\begin{array}{|c|c|c|} \hline 3 & 2 & 1 \\ \hline \end{array} * \begin{array}{|c|c|c|} \hline 1 & 0 & 0 \\ \hline 0 & -1 & 0 \\ \hline 0 & 0 & 1 \\ \hline \end{array}$$

$$= \begin{array}{|c|c|c|} \hline 3 & -2 & 1 \\ \hline \end{array}$$

b-

$$\begin{array}{|c|c|c|} \hline 3 & 2 & 1 \\ \hline \end{array} * \begin{array}{|c|c|c|} \hline -1 & 0 & 0 \\ \hline 0 & 1 & 0 \\ \hline 0 & 0 & 1 \\ \hline \end{array}$$

$$= \begin{array}{|c|c|c|} \hline -3 & 2 & 1 \\ \hline \end{array}$$

c-

$$\begin{array}{|c|c|c|} \hline 3 & 2 & 1 \\ \hline \end{array} * \begin{array}{|c|c|c|} \hline -1 & 0 & 0 \\ \hline 0 & -1 & 0 \\ \hline 0 & 0 & 1 \\ \hline \end{array}$$

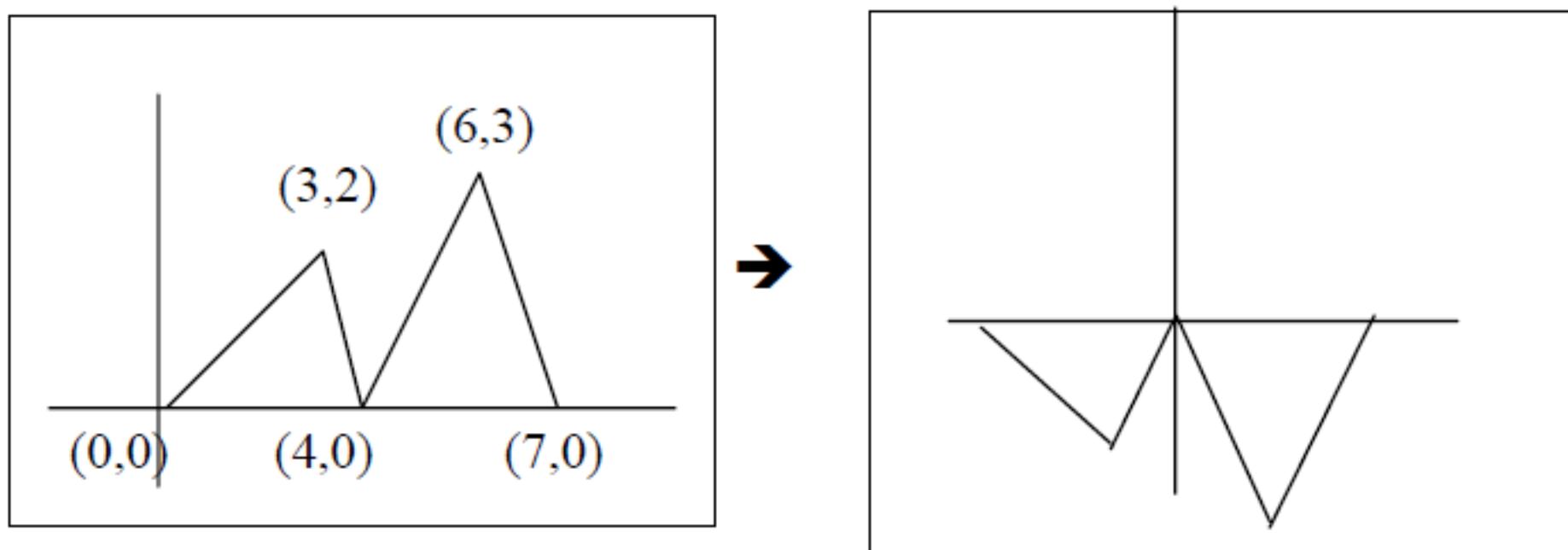
$$= \begin{array}{|c|c|c|} \hline -3 & -2 & 1 \\ \hline \end{array}$$

d-

$$\begin{array}{|c|c|c|} \hline 3 & 2 & 1 \\ \hline \end{array} * \begin{array}{|c|c|c|} \hline 0 & 1 & 0 \\ \hline 1 & 0 & 0 \\ \hline 0 & 0 & 1 \\ \hline \end{array}$$

$$= \begin{array}{|c|c|c|} \hline 2 & 3 & 1 \\ \hline \end{array}$$

Example 2: What (3*3) matrix will change the center of the scene to the origin, and reflect the mountains in the lake? [the center of the scene is (4,0)]



Solution:

First: Translate by $TX = -4$

1	0	0
0	1	0
-4	0	1

Second: Reflection on X axis

1	0	0
0	-1	0
0	0	1

Now multiply the two matrices :

1	0	0
0	1	0
-4	0	1

*

1	0	0
0	-1	0
0	0	1

The single matrix that perform Translation and Reflection is

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1	0	0
0	-1	0
-4	0	1

0	0	1
3	2	1
4	0	1
6	3	1
7	0	1

*

1	0	0
0	-1	0
-4	0	1

=

-4	0	1
-1	-2	1
0	0	1
2	-3	1
3	0	1