

Ex1: write program to create stack with size=10 to store the student's degree, compute number of succeed students and print the original stack.

Ex2: write function to insert three elements to stack.

Stack applications:

1. **Treat the programs which have sub programs.**

2. Mathematic expiration

As now the Mathematic expiration divides into three expirations:

- Infix notation:

Where the sine in middle of operands → $x/2$, $a-b$, $3+4$

- Prefix Notation: → $/x\ 20$, $-a\ b$, $+ 3\ 4$

- Postfix Notation: → $x\ 20\ /\ ,\ a\ b\ - ,\ 3\ 4\ +$

Note: In high level languages, infix notation cannot be used to evaluate expressions.

<u>Type of operation</u>	<u>the Priority</u>
^ (power), Unary (-), Unary (+), Not	4
*, /, AND, DIV, MOD	3
+, -, OR	2
=, <, >, !=, <=, >=	1

Note:

- In high level languages, infix notation cannot be used to evaluate expressions.
- A common technique is to convert a infix notation into postfix notation, then evaluate it.

Concert Infix notation to Postfix Notation algorithm using two stacks:

1. Initialize two empty stacks, (st1) to store operands, (st2) to store the operators of the mathematic operations.

- Read the tokens from the infix string one at a time from left to right
- If the token is operands then push it in **st1**.
- If the token is lift parentheses then push it in **st2**.
- If the token is right parentheses then pop all the operators from **st2** and push it in **st1** .

- Repeat this step until left parentheses is encountered, then remove and ignore the left parentheses and right parentheses.
- If the token is operator then pop all operators (if you found) which have priority higher than or equal the priority of the current operator from **st2** and push it in **st1**, then push the current operators in **st2**.

Else

Push the current operator in **st2**

2. After all the characters are read and the **st2** is not empty then Pop the stack and add the tokens to the **st1**
3. Return the Postfix **st1**.

Ex1: convert the following expressions from infix to postfix using two stacks.

$$a-b*(c+d)/(e-f)^g*h$$

<u>st2</u>	<u>st1</u>	<u>symbol</u>	<u>steps</u>
.....	a	a	1
-	a	-	2
-	ab	b	3
- *	ab	*	4
- * (ab	(5
- * (abc	c	6
- * (+	abc	+	7
- * (+	abcd	d	8
- *	abcd+)	9
نلاحظ هنا عند ورود القوس الأيمن يتم إخراج (نقل) جميع العمليات الحسابية لغاية القوس الأيسر من المكس (ST2) إلى (ST1) مع إخراج القوس الأيسر ليهمل هو والقوس الأيمن.			
- /	abcd+*	/	10
- / (abcd+*	(11
- / (abcd+*e	e	12
- / (-	abcd+*e	-	13
- / (-	abcd+*ef	f	14
- /	abcd+*ef-)	15
- / ^	abcd+*ef-	^	16
- / ^	abcd+*ef-g	g	17
- *	abcd+*ef-g^/	*	18
لان أسبقية الضرب (*) >= أسبقية الرفع (^) والقسمة (/)			
- *	abcd+*ef-g^/h	h	19
هنا انتهت جميع المدخلات لذا ينقل المتبقي في المكس (ST2) الى المكس (ST1) بالتتابع ليصبح			
	abcd+*ef-g^/h*-		20

Ex2: convert from infix to postfix using two stacks. $M:=X/6+(a-2*(b/3)^5+f)^2$

<u>st2 for operators</u>	<u>st1 for operands</u>	<u>input char</u>	<u>Step no.</u>
.....	M	M	1
:=	M	:=	2
:=	MX	X	3
:=/	MX	/	4
:=/	MX6	6	5
:=+	MX6/	+	6
:=+(MX6/	(7
:=+(MX6/a	A	8
:=+(-	MX6/a	-	9
:=+(-	MX6/a2	2	10
:=+(-*	MX6/a2	*	11
:=+(-*(MX6/a2	(12
:=+(-*(MX6/a2b	B	13
:=+(-*(/	MX6/a2b	/	14
:=+(-*(/	MX6/a2b3	3	15
:=+(-*(MX6/a2b3/)	16
:=+(-*^	MX6/a2b3/	^	17
:=+(-*^	MX6/a2b3/	5	18
:=+(+	MX6/a2b3/5^*-	+	19
:=+(+	MX6/a2b3/5^*-F	F	20
:=+	MX6/a2b3/5^*-F+)	21
:=+^	MX6/a2b3/5^*-F+	^	22
:=+^	MX6/a2b3/5^*-F+2	2	23
.....	MX6/a2b3/5^*-F+2^+:	24

Ex3: convert from infix to postfix using two stacks. $(A>B)AND ((E-C>A)OR(G<F))$.

Evaluate postfix expressions algorithm:

1. Initialize one stack (**st**) .
2. Read the tokens from the postfix string one at a time from left to right •
3. If token is operand, push it in **st**.
4. If the token is operator, implement this operation on the two operand in **st** and then put the result in **st**.
5. After all the characters are read, the result in st is the final result.

Ex: convert the following infix expression to postfix and compute its value.

$$7+8-6*3/2.$$

After conversion we have the postfix $78+63*2/-$

To get the value :

<u>St</u>	<u>Input char</u>	<u>Step no.</u>
7	7	1
7 8	8	2
15	+	3
15 6	6	4
15 6 3	3	5
15 18	*	6
15 18 2	2	7
15 9	/	8
6	-	9