

University of Anbar

College of Science

Department of Applied Geology

Fourth Year

Electromagnetics



جامعة الانبار

كلية العلوم

قسم علوم الفيزياء

المرحلة الرابعة

الكهرومغناطيسية

Electrical Field

Part one: Electric Field

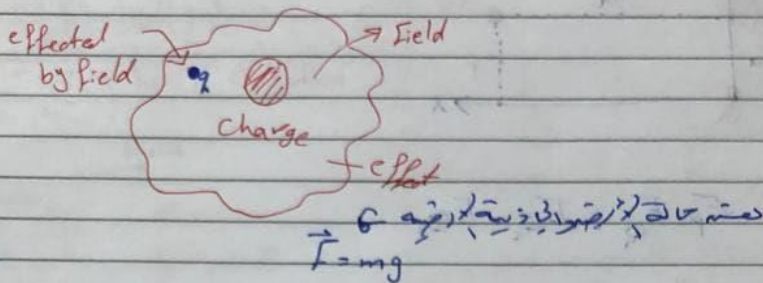
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Part one in this Chapter: Electric Field

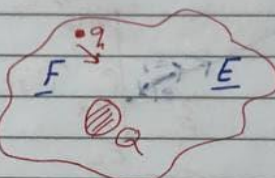
Electric Field

حقل كهربائي



$$[F = qE]$$

Electric force over q due to E



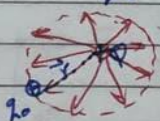
Point charge

$$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \rightarrow E = \frac{F}{q_0}$$

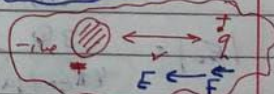
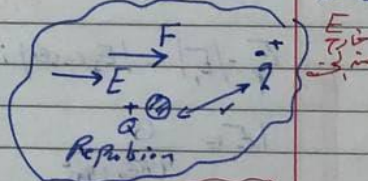
Coulomb law

$$F = \frac{q_1 q_2}{4\pi\epsilon_0 r^2} = k \frac{q_1 q_2}{r^2}$$

$$F = \frac{qQ}{4\pi\epsilon_0 r^2}$$

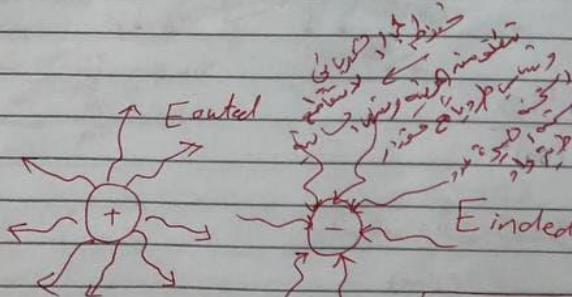


F, E in the same direction



Attraction

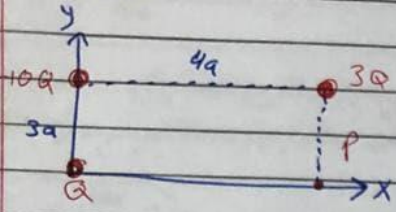
F, E in the same direction in case E



Dirig of Q حقل كهربائي E

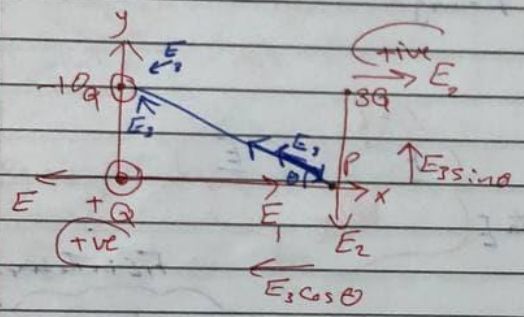
$$E = \frac{q}{4\pi\epsilon_0 r^2} \hat{r}$$

Example:-



What is E at P ?

$$E_p = E_{Q_1} + E_{Q_2} + E_{Q_3}$$

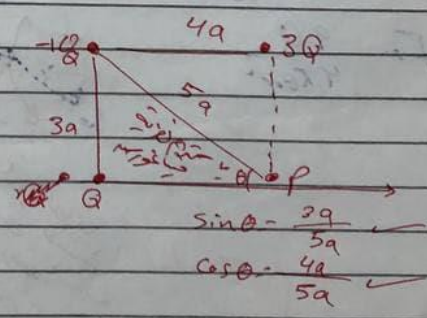


$$E_p = |E| = |E_3 \cos \theta| i + |E_3 \sin \theta - E_2| j$$

$$|E_1| = \frac{Q}{4\pi\epsilon_0 (4a)^2}$$

$$|E_2| = \frac{3Q}{4\pi\epsilon_0 (3a)^2}$$

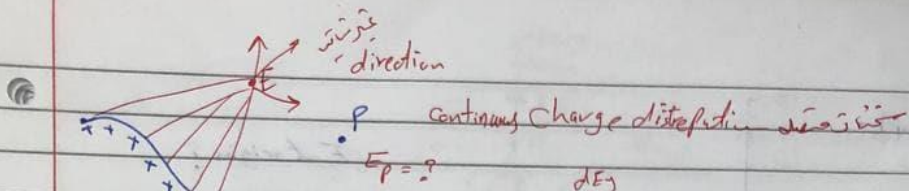
$$|E_3| = \frac{-10Q}{4\pi\epsilon_0 (5a)^2}$$



$$\sin \theta = \frac{3a}{5a}$$

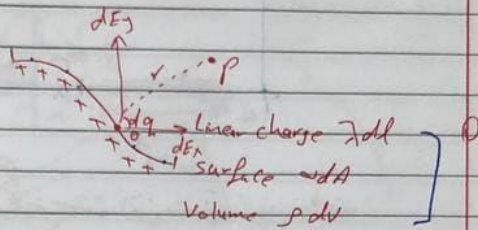
$$\cos \theta = \frac{4a}{5a}$$

تم له ذلك تم لتقويمه ip (H.w)



$$E = k \frac{q}{r^2} \hat{x}$$

direction



dE due to dq

$$|dE| = k \frac{dq}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{dq}{r^2}$$

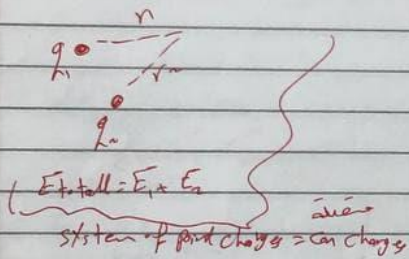
vector ← magnitude

Component of dE

$$dx = dE \cos \theta$$

$$dy = dE \sin \theta$$

dq direction \hat{r} is $\hat{r} = \frac{\vec{r}}{r}$



direction → Continuous charge

∫ → Sum of continuous quantity

$$E_x)_{total} = \int dE_x$$

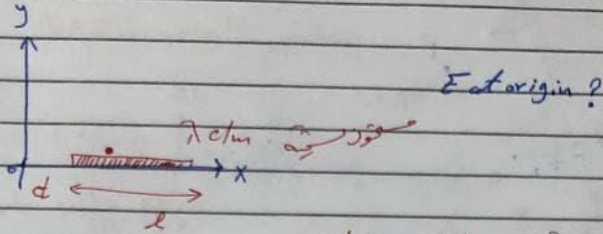
end of charge

$$E_y)_{total} = \int dE_y$$

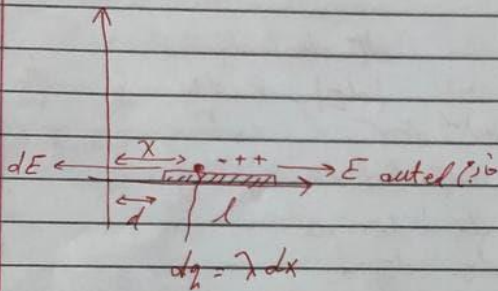
start of charge

direction (4)
(1) (2) (3) (4)

Example:



لا يمكن التعامل مع الشحنة كقوة نقطية لأنها موزعة على طول (ولذلك يمكن أن تكون شحنة موزعة على طول) بدلاً من ذلك



$$dE = \frac{dq}{4\pi\epsilon_0 x^2} = \frac{\lambda dx}{4\pi\epsilon_0 x^2}$$

$$\text{total } E = \int dE = \int_{x_{\text{start}}=d}^{d+l} \frac{\lambda dx}{4\pi\epsilon_0 x^2}$$

$$= \frac{\lambda}{4\pi\epsilon_0} \int_d^{d+l} \frac{dx}{x^2}$$

$$= \frac{\lambda}{4\pi\epsilon_0} \left(\frac{-1}{x} \right)_d^{d+l}$$

$$= \frac{\lambda}{4\pi\epsilon_0} \left[\frac{-1}{d+l} - \left(\frac{-1}{d} \right) \right]$$

$$E = \frac{\lambda}{4\pi\epsilon_0} \left[\frac{1}{d} - \frac{1}{d+l} \right]$$

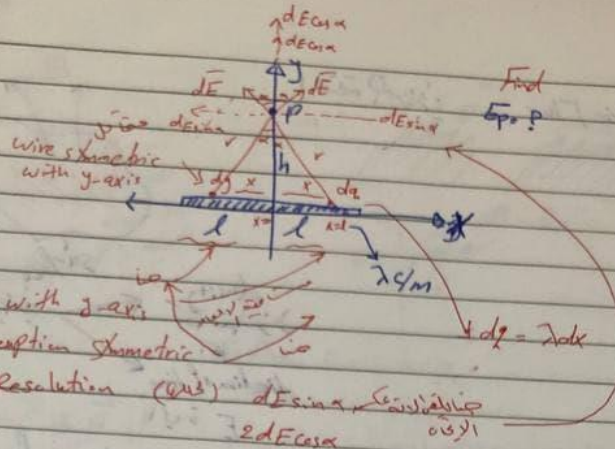
نلاحظ
Vector
في اتجاه اليمين

$$E = \frac{\lambda}{4\pi\epsilon_0} \left[\frac{1}{d} - \frac{1}{d+l} \right] (-i)$$

التي هي في اتجاه اليمين
فيكون في اتجاه اليمين (-i)

1000

Example:



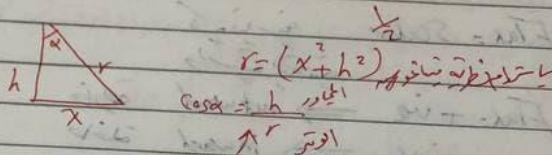
- Symmetric with y-axis
- ∴ charge distribution symmetric

2) dE net resolution (cos alpha) $\frac{dE \sin \alpha}{2dE \cos \alpha}$

$$dE_{total} = 2dE \cos \alpha$$

Coulomb law Geometry

$$dE = \frac{dq}{4\pi\epsilon_0 r^2}$$



$$dE = \frac{\lambda dx}{4\pi\epsilon_0 r^2}$$

$$dE_{total} = \frac{2\lambda h dx}{4\pi\epsilon_0 r^3}$$

$$E_{total} = \int_{x=0}^{x=l} \frac{2\lambda h dx}{4\pi\epsilon_0 (x^2 + h^2)^{3/2}}$$

integration with respect to x

Unit vector \hat{j} along H.W. direction

∴ \hat{j}

∴ symmetric with y-axis

Reference:

- 1) INTRODUCTION to ELECTRODYNAMICS, Third Edition, David j.Griffths