

University of Anbar

College of Science

Department of Applied Geology

Fourth Year

Electromagnetics



جامعة الانبار

كلية العلوم

قسم علوم الفيزياء

المرحلة الرابعة

الكهرومغناطيسية

Electrical Field in matter

Part One: Electrical Field in matter 1

Dr. Israa Kamil Ahmed

د. اسراء كامل احمد

Part one in this chapter: Electrical Field in matter 1

Electrical field in matter

Conductors, Basic properties

in an insulator like glass, each electron is attached to a particular atom,

in a conductor, one or more electrons per atom are free throughout the material.

i) $E=0$ inside conductor

ii) $\rho=0$ inside a conductor

This follows from Gauss law $\nabla \cdot E = \frac{\rho}{\epsilon_0}$

if $E=0$ so also is $\rho=0$

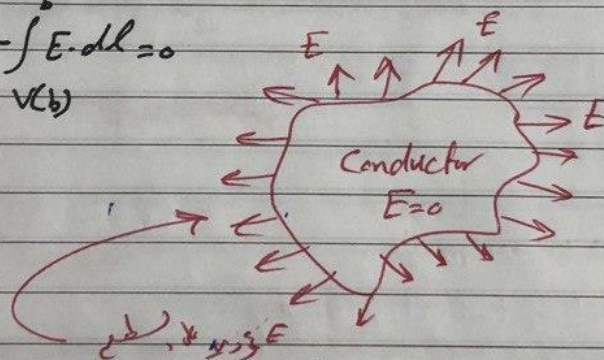
iii) Any net charge reside on the surface

iv) A conductor is an equipotential

For if a & b are any two points within or on the surface of a conductor

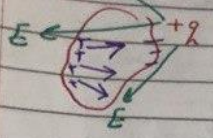
$$V(b) - V(a) = -\int_a^b E \cdot dl = 0$$

$$\text{hence } V(a) = V(b)$$



v) E is perpendicular to the surface

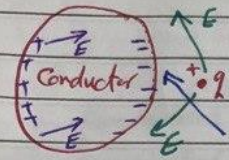
induced charges



If you hold $+q$ near uncharged conductor in figure $+q$ with Electric field line \vec{E} we must to build inside the conductor \vec{E} with opposite direction and the same magnitude

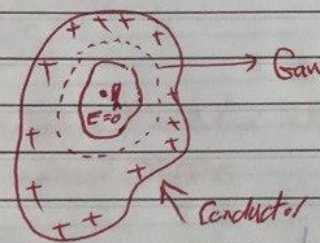
المجال الكهربائي الداخلي داخل الموصل

Since the Negative charge is closer to $+q$, there is a net force of attraction



Attraction here

if there is some cavity in the conductor, and within the cavity there is some charge, then the field in the cavity will not be zero



Gaussian surface

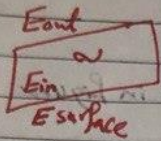
conductor

The total charge induced on the cavity wall is equal and opposite to the charge inside, if we surrounded the cavity with a Gaussian surface all the points which are in the conductor $\oint \vec{E} \cdot d\vec{a} = 0$

the net enclosed charge must be zero

But $q_{\text{enclosed}} = -q$

Electric Field on a conductor, The Force on a surface charge



3 electric field in this surface

$E_{out}, E_{inside}, E_{surface}$

$$\vec{E}_{out} = \frac{\sigma}{\epsilon_0} \vec{n}$$

Potential $-\nabla \cdot \vec{v} = \vec{E}$

$$\frac{\partial v}{\partial n} = -\frac{\sigma}{\epsilon_0} \Rightarrow \sigma = \epsilon_0 \frac{\partial v}{\partial n} \text{ surface charge on the conductor}$$

what is the force on this surface charge?

$$\vec{F} = \sigma \vec{E} \text{ (at the surface)}$$



$$\vec{E}_{above} = \vec{E}_{out} + \frac{\sigma}{2\epsilon_0} \vec{n}$$

$$\vec{E}_{below} = \vec{E}_{in} + \frac{\sigma}{2\epsilon_0} \vec{n}$$

$$\vec{E}_{outside} = \vec{E}_{above} - \frac{\sigma}{2\epsilon_0} \vec{n}$$

$$= \vec{E}_{below} + \frac{\sigma}{2\epsilon_0} \vec{n}$$

add them and divide by 2

$$\vec{E}_{out} = \frac{1}{2} (\vec{E}_{above} + \vec{E}_{below})$$

for conductor $E_{inside} = 0$

$$\frac{1}{2} (\frac{\sigma}{\epsilon_0})$$

$$= \frac{1}{2} \frac{\sigma}{\epsilon_0} \vec{n}$$

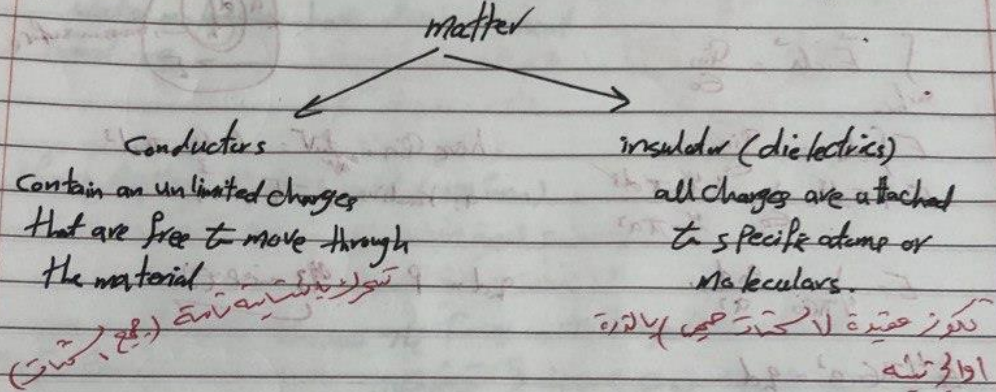
$$\vec{F} = \sigma \vec{E}_{at\ the\ surface}$$

$$= \sigma \frac{1}{2} \frac{\sigma}{\epsilon_0} \hat{n} \text{ normal direction}$$

$$= \frac{1}{2} \frac{\sigma^2}{\epsilon_0} \hat{n}$$

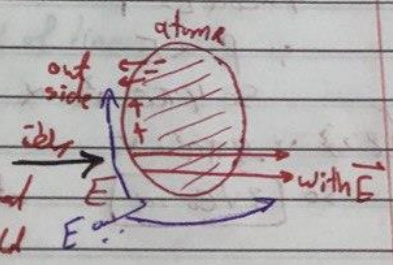
$$= \frac{\sigma^2}{2\epsilon_0} \hat{n}$$

Polarization:

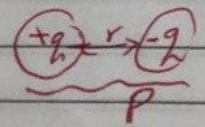


Dielectrics Polarization induced Dipoles

inside any atoms or surface or shape. There is two charges (+, -) between +q and -q there is r and this is called Dipole or P



Electric Dipole



Reference:

- 1) INTRODUCTION to ELECTRODYNAMICS, Third Edition, David j.Griffths