

Al-Anbar University
College of engineering
Electrical Engineering Department

fundamental of Electric Circuit 1
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Stage 1
2021-2022



LECTURE 07
WYE-DELTA TRANSFORMATION



Topics

- ▶ Δ - Connection
- ▶ Y - Connection
- ▶ Δ -Y Transformation



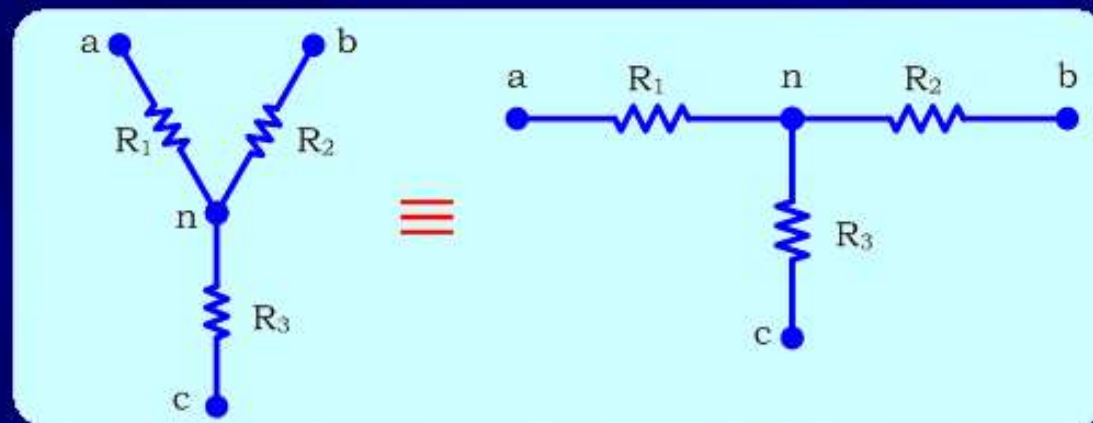
Objectives

- ▶ Recognize Y and Δ connections
- ▶ Redraw the circuit to make it easier to identify Y and Δ connections
- ▶ Use the transformation relations to perform Y- Δ transformations
- ▶ Use Y- Δ transformation to simplify analysis of certain circuits



Y - Connection

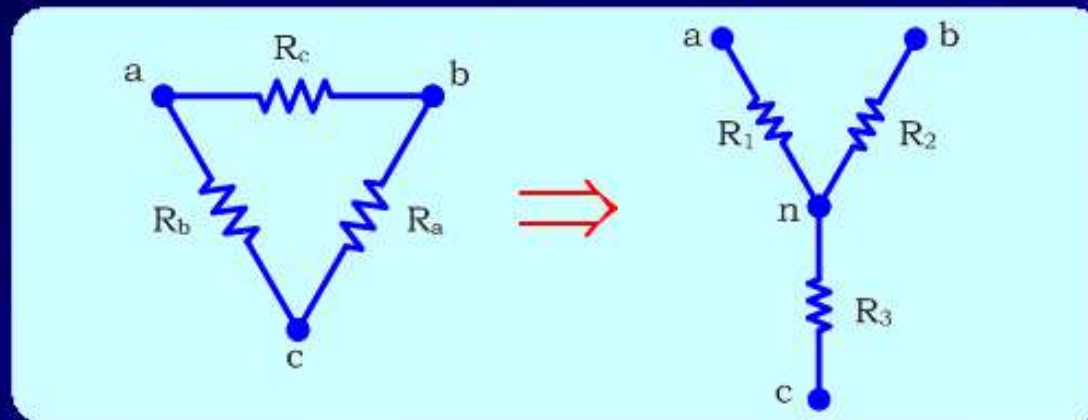
R_1 , R_2 and R_3 form a Y connection



The *terminals* of the Y connection are also labeled as a , b and c .



Δ -Y Transformation



Relations for Δ -Y Transformation

$$R_1 = \frac{R_b R_c}{R_a + R_b + R_c}$$

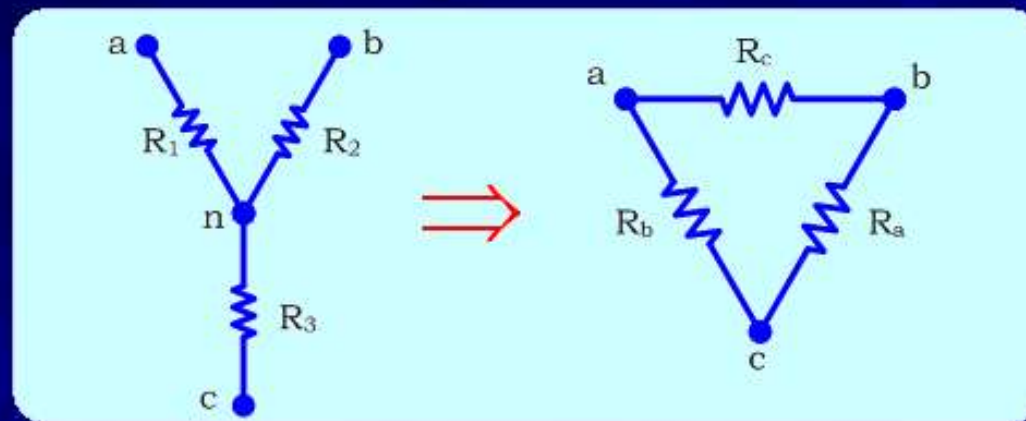
$$R_2 = \frac{R_a R_c}{R_a + R_b + R_c}$$

$$R_3 = \frac{R_a R_b}{R_a + R_b + R_c}$$

You need only to remember one of the above relations, since the other two are similar



Y- Δ Transformation



Relations for Y- Δ Transformation

$$R_a = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_1}$$

$$R_b = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2}$$

$$R_c = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3}$$

The numerator is the same making the above relations easy to recall
Notice that the nodes *a*, *b* and *c* are kept the same in both circuits



Example 1

Use $\Delta \rightarrow Y$ transformation to calculate

(a) R_{eq} seen by the voltage source (b) i_s

Solution

(a) We cannot calculate R_{eq} using the series parallel approach

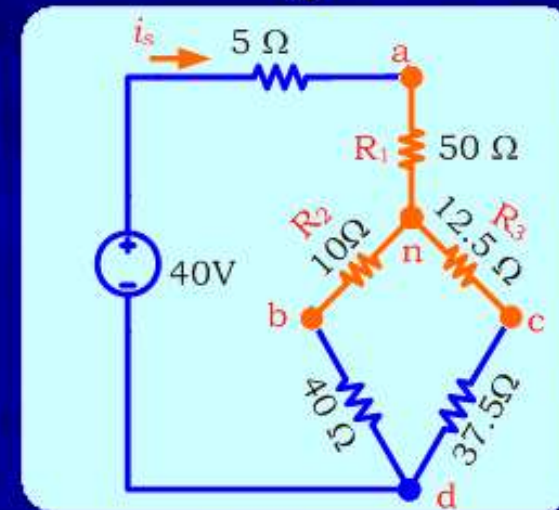
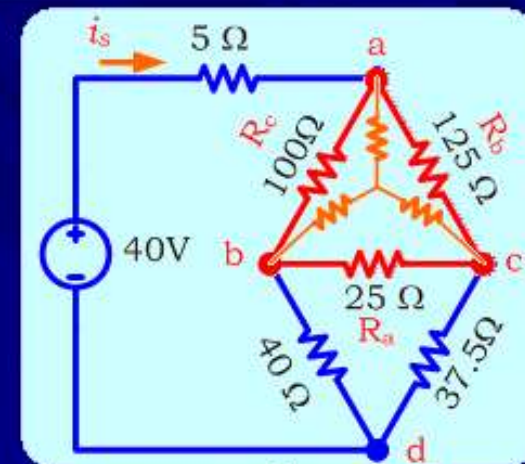
We can transform the (upper or lower) Δ to Y

Transforming the upper Δ to Y

$$R_1 = \frac{R_b R_c}{R_a + R_b + R_c} = \frac{125 \times 100}{25 + 125 + 100} = \frac{125 \times 100}{250} = 50 \Omega$$

$$R_2 = \frac{R_a R_c}{R_a + R_b + R_c} = \frac{25 \times 100}{250} = 10 \Omega$$

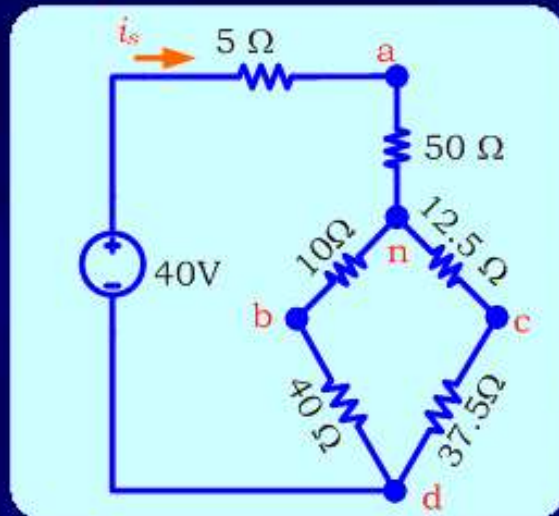
$$R_3 = \frac{R_a R_b}{R_a + R_b + R_c} = \frac{25 \times 125}{250} = 12.5 \Omega$$





Example 1 (Contd...)

Use $\Delta \rightarrow Y$ transformation to calculate (a) R_{eq} seen by the voltage source (b) i_s

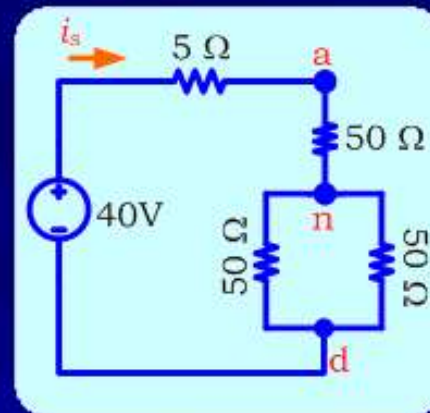


12.5Ω & 37.5Ω (in series)

$$\Rightarrow 12.5 + 37.5 = 50\Omega$$

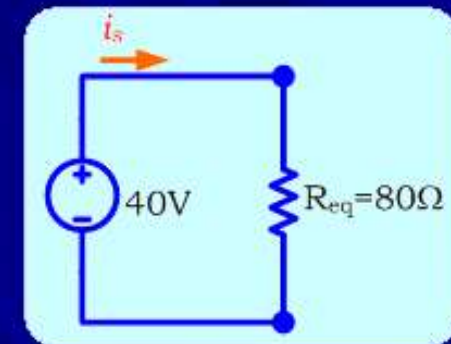
10Ω & 40Ω (in series)

$$\Rightarrow 10 + 40 = 50\Omega$$



$$\therefore R_{eq} = 5 + 50 + (50/2)$$

$$\Rightarrow R_{eq} = 80\Omega$$



$$(b) i_s = \frac{40}{R_{eq}} = \frac{40}{80} = 0.5A$$



Example 2

Let us explore some other possibilities for solving the previous problem. Repeat the previous example using $Y \rightarrow \Delta$ transformation

(a) R_{eq} seen by the voltage source (b) i_s

Solution

(a) Redraw the circuit

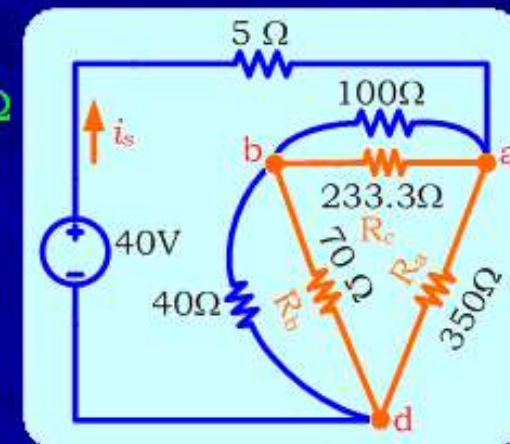
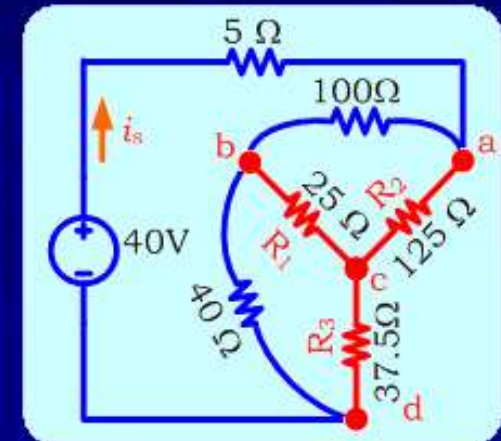
25 Ω , 125 Ω and 37.5 Ω form a Y connection

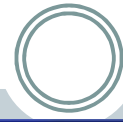
Using Y to Δ transformation

$$R_a = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_1} = \frac{25 \times 125 + 125 \times 37.5 + 37.5 \times 25}{25} = 350 \Omega$$

$$R_b = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2} = \frac{8750}{125} = 70 \Omega$$

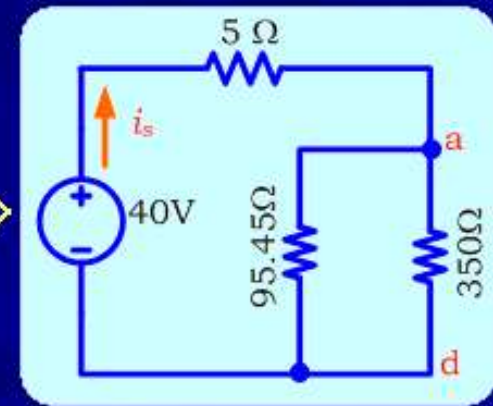
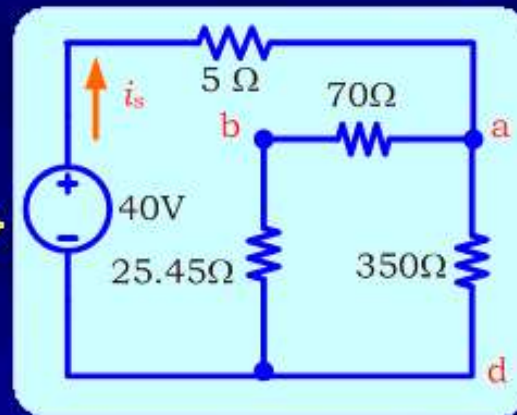
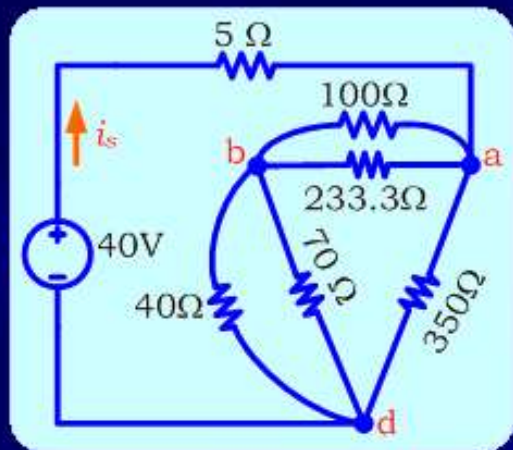
$$R_c = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3} = \frac{8750}{37.5} = 233.33 \Omega$$





Example 2 (Contd...)

Use $Y \rightarrow \Delta$ transformation to calculate (a) R_{eq} seen by the voltage source (b) i_s



$$40\Omega \parallel 70\Omega \\ \Rightarrow \frac{40 \times 70}{40 + 70} = 25.455\Omega$$

$$100\Omega \parallel 233.33\Omega \\ \Rightarrow \frac{100 \times 233.33}{100 + 233.33} = 70\Omega$$

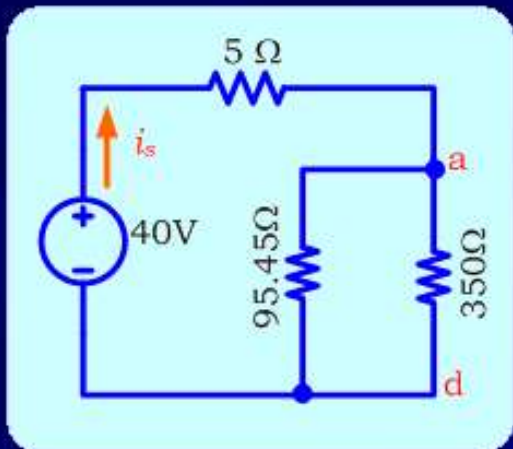
$$70\Omega \text{ \& \; } 25.45\Omega \text{ (in series)} \\ \Rightarrow 70 + 25.45 = 95.45\Omega$$

$$95.45\Omega \parallel 350\Omega \\ \Rightarrow \frac{95.45 \times 350}{95.45 + 350} = 75\Omega$$

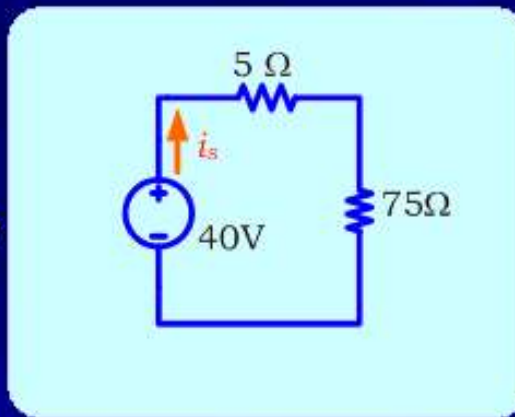


Example 2 (Contd...)

Use $Y \rightarrow \Delta$ transformation to calculate (a) R_{eq} seen by the voltage source (b) i_s



$$95.45\Omega \parallel 350\Omega$$
$$\Rightarrow \frac{95.45 \times 350}{95.45 + 350} = 75\Omega$$

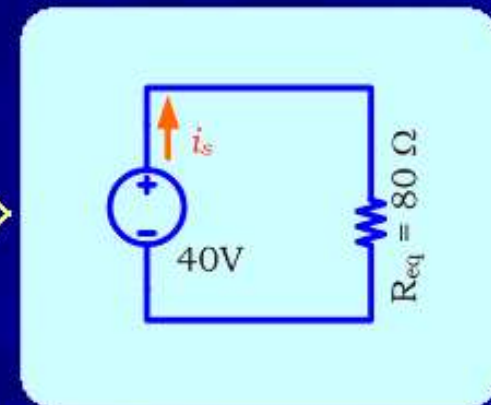


5 Ω & 75 Ω (in series)

$$\Rightarrow 5 + 75 = 80\Omega$$

$$\therefore R_{eq} = 80\Omega$$

same answer as before



$$(b) \quad i_s = \frac{40}{R_{eq}} = \frac{40}{80} = 0.5A$$