



الكلية : التربية للعلوم الصرفة

القسم او الفرع : الرياضيات

المرحلة: الثالثة

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اسم المادة باللغة العربية : نظرية احتمالية 1

اسم المادة باللغة الإنكليزية : Probability Theory 1

اسم المحاضرة الأولى باللغة العربية: طرق العد (مبادئ العد)

اسم المحاضرة الأولى باللغة الإنكليزية : Counting Techniques

## Chapter one

## (Counting Technique (مبادئ العد )

Fundamental principle of counting

المبادئ الأساسية لطرق العد

### Multiplication principle

If set's A1 and A2 have  $n_1$  and  $n_2$  element respectively there are  $n_1 \times n_2$  ways in which one select from A1 and then one select from A2

### Example:

Suppose that a person has a choice of five shirts and the three trousers then he has  $5 \times 3 = 15$  different choice of wearing a dress

### Additional principle

If set's A1 and A2 have  $n_1$  and  $n_2$  element respectively there are  $n_1 + n_2$  ways in which either select from A1 or A2 we assume that no two selections can be carried out simultaneously.

For  $n \in I^+$ ,  $r=0,1,\dots,n$  where  $I^+$  is the set of positive Integers  $P(n,r) = \frac{n!}{(n-r)!}$ ,

If  $r=n \Rightarrow P(n,n) = n!$  should order with select

**Example:** How many there chigit numbers can be formed from the six chigits 1,3,5,6,7 and 9

Solution:  $P(6,3) = \frac{6!}{(6-3)!} = 6 \times 5 \times 4 = 120$

### A permutation of elements with Repetitions

The number of permutation of  $n$  (elements)(objects, things symbols) of which  $n_1$  are alike  $n_2$  others are alike ,...one  $n_k$  are alike Is given by  $p(n,n_1,n_2,\dots, n_k)$  provided  $n_1+n_2+\dots+n_k=n$

In notation  $p(n, n_1, n_2, \dots, n_k) = \frac{n!}{n_1! n_2! \dots n_k!}$  When  $\sum_{i=1}^k n_i = n$

**Example:** A committee consisting of ten members visits a metropolitan city to investigate the changing scenario with respect to traffic problem

**Example:** three books are recommended for basic course in mathematics (Analysis) and five books for the probability theory. The total number of ways a student can choose the book is  $3+5=8$  ways

We can generalize the addition principle as if sets  $A_i$  ( $i=1, 2, \dots, k$ ) have respectively  $n_i$  ( $i=1, 2, \dots, k$ ) elements there are  $n_1 + n_2 + \dots + n_k = \sum_{i=1}^k n_i$  Ways.