



3-4 Maximum Torque: -

Taking the derivative of T_{em} by S (dT_{em}/ds) and equating this to zero ($dt/ds = 0$) then the slip at max. torque (critical slip) can be obtained:-

$$s_m = \pm \frac{R_{2e}}{\sqrt{R_1^2 + (X_1 + X_2)^2}}$$

If neglecting the stator risis. ($R_1=0$) then

$$s_m = \pm \frac{R_{2e}}{\sqrt{(X_1 + X_2)^2}} = \pm \frac{R_{2e}}{X_{SC}}$$

Substituting S_m in the torque equation in (T_{em}) then

$$T_m = \pm \frac{3V_1^2}{\omega_1} \times \frac{1}{2(R_1 \pm \sqrt{R_1^2 + (X_1 + X_2)^2})^2}$$

Neglecting the $R_1=0$ then the maximum torque is

$$T_m = 1.5 \frac{V^2}{\omega_1 X_{SC}} = 0.2388P \frac{V^2}{f_1 X_{SC}}$$

The max. torque value is inversely proportional to the short circuit reactance ($T_m \propto 1/X_{SC}$) and it is independent of (R_{2e}): that means it's no effect of R_{2e} on T_m value.

To have max. torque at starting: $T_s = T_m$

Then $S_m = 1 = R_{2e}/X_{SC}$ Or $R_{2e} = X_{sc} = X_1 + X_{sc}$

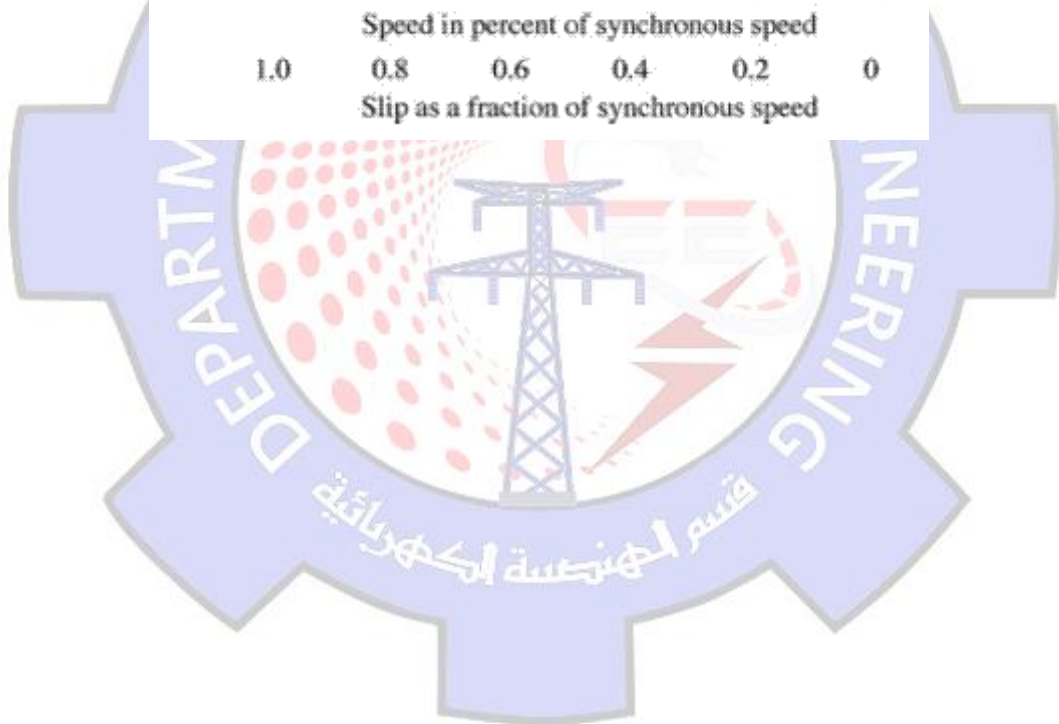
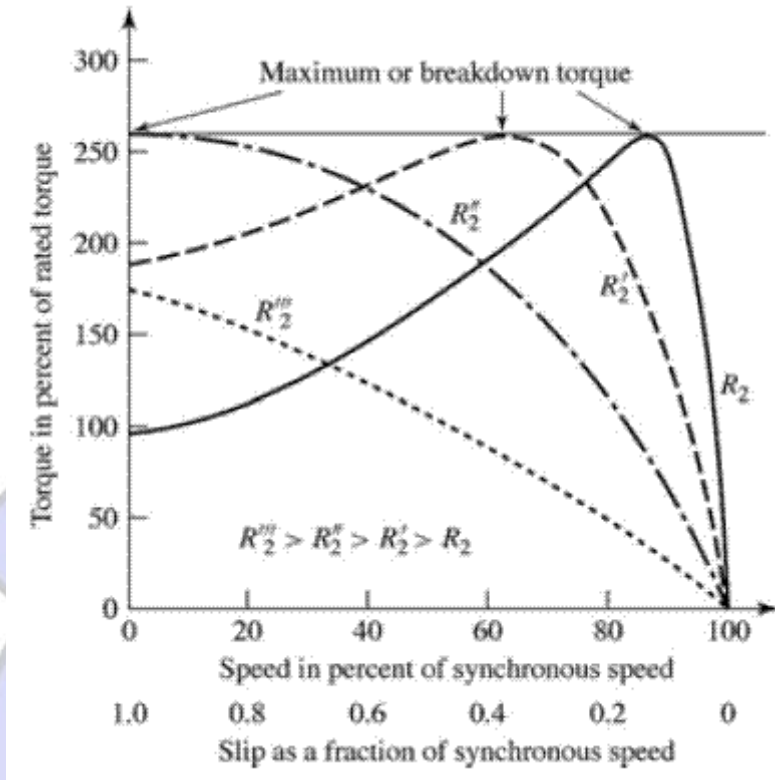
This means that $\phi_2 = 45^\circ$ and $\cos \phi_2 = 0.707$

3-5 Starting Torque:-

At starting $S=1$, substituting this slip value in torque equation then.

$$T_s = \frac{3V_1^2}{\omega_1} \cdot \frac{R_{2e}}{(R_1 + R_{2e})^2 + (x_1 + x_{2e})^2}$$

Usually if it is required that $T_s = T_m$ then $S_m = 1$ or $R_{2e} = X_{2e}$ if it should be rotated that $R_{2e}/s =$ constant always or $\frac{R_2}{s} = \frac{R_2'}{s'} = \frac{R_2''}{s''} = \frac{R_2'''}{s'''}$





3- 6 Effect of Applied Voltage:-

From approximate equivalent cct and assuming $Z_1=0$ then

$$T_m = \frac{3}{\omega_1} \cdot \frac{V_1^2 R_{2e}}{(R_{2e})^2 + (S X_{2e})^2} \quad \text{since } T_1 = T_2 = T$$

Then

$$\frac{V_1^2 S_1 R_{2e}}{(R_{2e})^2 + (S_1 X_{2e})^2} = \frac{V_2^2 S_2 R_{2e}}{(R_{2e})^2 + (S_2 X_{2e})^2}$$

$$\text{OR } \left(\frac{V_1}{V_2}\right)^2 = \frac{S_2}{S_1} \left(\frac{R_{2e}^2 + (S_1 X_{2e})^2}{R_{2e}^2 + (S_2 X_{2e})^2}\right)$$

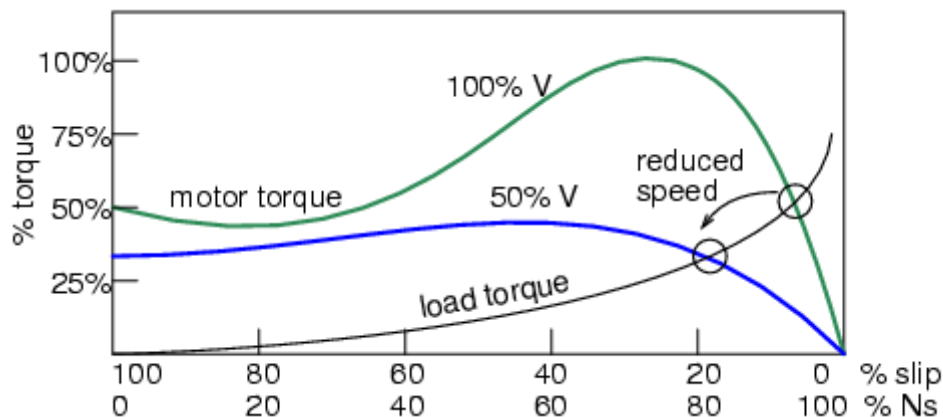
Since slip variation will not effect the value in the rotor coil of machine then.

$$\frac{T_1}{T_2} = \left(\frac{V_1}{V_2}\right)^2 = \frac{S_2}{S_1} \quad \text{Since } S_1 X_{2e} = S_2 X_{2e}$$

If $V_2=0.75V_1$ then $T_2=0.44 T_1$

That mane the voltage variation ΔV must be in rang of (10-(-5))%

$\Delta V=+10\%$, -5%





3-7 Ratio of Max To Rated Torque:-

$$T_r = \frac{3V^2}{\omega 1} \cdot \frac{R2e/sr}{(R1 + R2e/sr)^2 + (x1 + x2)^2}$$

$$T_m = \frac{3V^2}{\omega 1} \cdot \frac{\frac{R2e}{sm}}{\left(R1 + \frac{R2e}{sm}\right)^2 + (x1 + x2)^2}$$

$$K_{mr} \text{ or } \mu_m = \frac{T_m}{T_r}$$

$$\mu_m = \frac{\left(R1 + \frac{R2e}{sr}\right)^2 + (X1 + X2e)^2}{\left(R1 + \frac{R2e}{sm}\right)^2 + (X1 + X2e)^2} \cdot \frac{sr}{sm}$$

$$S_m = \frac{R2}{\sqrt{R1^2 + (X1 + X2)^2}} \rightarrow R1^2 + (X1 + X2)^2 = \left(\frac{R2}{S_m}\right)^2$$

$$(X1 + X2)^2 = \left(\frac{R2}{S_m}\right)^2 - R1^2$$

$$\mu_m = \frac{R1^2 + 2R1 \frac{R2}{Sr} + \left(\frac{R2}{Sr}\right)^2 + \left(\frac{R2}{S_m}\right)^2 - R1^2}{R1^2 + 2R1 \frac{R2}{Sr} + \left(\frac{R2}{Sr}\right)^2 + \left(\frac{R2}{S_m}\right)^2 - R1^2} \cdot \frac{sr}{sm}$$

$$= \frac{2R1R2 + \frac{R2^2}{Sr} + sr \left(\frac{R2}{S_m}\right)^2}{2R1R2 + \frac{R2^2}{S_m} + \frac{R2^2}{S_m}} \times \frac{R2^2}{R2^2} \text{ divided}$$

$$= \frac{\frac{2R1}{R2} + \frac{1}{Sr} + \frac{Sr}{S_m^2}}{\frac{2R1}{R2} + \frac{1}{S_m} + \frac{1}{S_m}} \times \frac{sm}{sm}$$

$$\mu_m = \frac{\frac{sm}{sr} + \frac{sr}{sm} + 2sm \frac{R1}{R2}}{2 + 2Sm \frac{R1}{R2}}$$



$$\mu_m = \frac{\frac{sm}{sr} + \frac{sr}{sm} + Q}{2 + Q} \quad Q = 2Sm \frac{R1}{R2}$$

$$Z1 = 0, \quad Q = 0$$

$$\frac{Tm}{Tr} = \frac{\frac{sm}{sr} + \frac{sr}{sm}}{2} = 2 \frac{Tm}{Tr} = \frac{Sm^2 + Sr^2}{Sm Sr}$$

$$\frac{Tm}{Tr} = \frac{Sm^2 + Sr^2}{2Sm Sr}$$

$$\mu_m = 1.7 \dots\dots 3$$

