



## 2-Shunt

2.1- for a speed of 850Vpm,  $V_{no}$ ?

A)  $F_{CR}=0$

To find  $V_{no}$  load we must draw the  $R_f$  line with occ and the point of intersection represent.

At  $F_{CR}=0$   $R_f=20$ ,  $V_f=I_f R_f$

$V_f=0*20=0$ ,  $V_f=0.5*20=10$

$V_f=1*20=20$ ,  $V_f=2*20=40$

From the point of intersection

$V_f=257.5V$

At  $F_{CR}=10\Omega$ ,  $R_{ft}=30\Omega$

$V_f=30*0=0$ ,  $30*1=30v$ ,  $30*2=60v$

From the point of intersection

$V_n=208V$

At  $F_{CR}=30\Omega$   $R_{ft}=30+20=50\Omega$

$V_f=50*0=0$ ,  $5*1=50$

From the point of intersection

$V_n=24V$

B)  $R_{cri}=?$   $I_{sc}=?$   $V_t=0$

To find  $R$  critical, we draw a line tangent to the occ and take any point intersection between them and find  $R_{cr}$  from  $R_{cr}=\frac{V}{I}$

$$R_{cr}=\frac{80}{2}=40\Omega$$

At Short cct  $I_f=0$   $E_A=E_{res}$

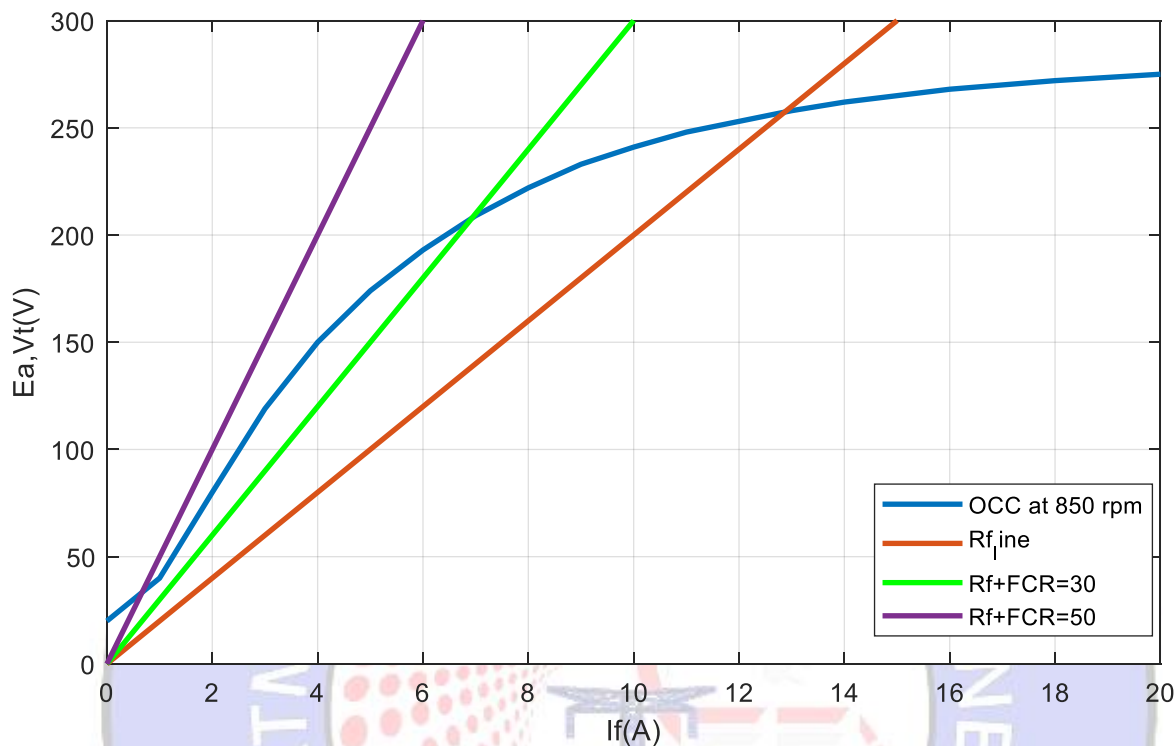
$V_t=0$   $I_A=I_{sc}$

$I_f(A)$	$V_f (v)$		
	$F_{CR}=0$	$F_{CR}=10$	$F_{CR}=30$
0	0	0	0
1	20	30	50
2	40	60	100
3	60	90	150
4	80	120	200
5	100	150	250
6	120	180	300
7	140	210	350
8	160	240	400
9	180	270	450
10	200	300	500
11	220	330	550
12	240	360	600
13	260	390	650
14	280	420	700
15	300	450	750
16	320	480	800
17	340	510	850
18	360	540	900
19	380	570	950



$$V_t = E_a - I_a R_A, \quad 0 = E_{res} - I_{s.c} R_A$$

$$I_{s.c} = \frac{E_{res}}{R_A} = \frac{20}{0.25} = 80A$$



c)

1) when  $FCR=10$   $n_{cri}=?$

To find critical speed at  $FCR=10\Omega$ . we draw the  $R_{f-line}$  when  $R_f=10+20=30\Omega$  take any value of  $(I_f)$  and alling it on occ and  $R_f$ -line  $FCR=10\Omega$  and find the value of  $E_1$  from  $R_f$  line and  $E_0$  from occ at new speed and applied :

$$\frac{E_1}{E_0} = \frac{n_1}{n_0} \quad \text{When } I_f=1A \quad E_0=40V \quad \text{from occ at } 850Vpm$$

$$E_1=30V \quad \text{from } R_f \text{ line } FCR=10\Omega$$

$$\frac{E_1}{E_0} = \frac{n_1}{n_0} \rightarrow \frac{30}{40} = \frac{n_1}{850} \rightarrow n_1 = 637.5 \text{ rpm}$$

2) at  $FCR=30\Omega$ , same procedure in (1) using  $R_{f-line}$  when  $R_f=30+20=50\Omega$ , when  $I_f=3$ ,  $E_0=120V$ ,  $E_1=150$

$$\frac{E_1}{E_0} = \frac{n_1}{n_0} \rightarrow \frac{150}{120} = \frac{n_1}{850} \rightarrow n_1 = 1062.5 \text{ rpm}$$



**D)**

At  $F_{CR}=0$ , to get minimum speed we take any value of  $(I_f)$  in the med points of  $R_f$  line and falling it on occ and  $F_{CR}=0$  and find  $E_0/E_1$ , At  $I_f=2$

$E_0=80$  on occ,  $E_1=40$  on  $R_f$  ( $F_{CR}=0 \Omega$ )

$$\frac{E_1}{E_0} = \frac{n_1}{n_0} \rightarrow n_1 = \frac{40 * 850}{80} = 425 \text{ rpm}$$

**2-2-**

**A)**  $R_c=?$  And  $I_{s.c}=?$  at 1100 rpm, we take the point (80V, 2A) from occ at 850 rpm

$$E_1 = \frac{1100 * 80}{850} = 103.52 \text{ V}, R_c = \frac{E_1}{I_f} = \frac{103.52}{2} = 51.76 \Omega$$

$$E_1 = \frac{1100 * 20}{850} = 25.88 \text{ V}$$

$$I_{s.c} = \frac{25.88}{0.25} = 103.52 \text{ A}$$

The good solution must draw the OCC at 1100 rpm and plot a tangent line to new OCC.

**B)**  $V_{nL}=?$   $F_{CR}=0$

We plot occ at  $N=1100$  rpm

And plot the  $R_f$  line ( $F_{CR}=0$ )

$R_f=20$  850 rpm

$V_f=I_f R_f$ ,  $V_f=0 * 20=0$

$V_f=20 * 0.5=10$ ,  $V_f=20 * 1=20$

$$E_A = \frac{E_0 * 1100}{850}$$

$$E_A = \frac{20 * 1100}{850} = 25.88$$

$$E_A = \frac{24 * 1100}{850} = 31.05$$

The intersection point between the OCC and  $R_f$ -line get

$V_{n \text{ load}}=351.5 \text{ V}$

**2-3-**

$V_t=E_A-I_A R_A$ , The intersection point between the OCC and  $R_f$ -line get at  $F_{CR}=0$

$V_{n \text{ load}}=257.5$

**A)**

$V_f(V)$	$F_{CR}(0)$	$E_A$ at 1100 rpm	$I_f$	$E_A$
0		25.88	0	20
20		51.76	1	40
40		103.52	2	80
60		154	3	119
80		194.11	4	150
100		225.17	5	174
120		249.76	6	193
140		270.47	7	209
160		287.29	8	222
180		301.529	9	233
200		311.88	10	241
220		320.94	11	248
240		327.41	12	253
260		333.88	13	258
280		339.05	14	262
320		346.88	16	268
360		352	18	272
400		355.88	20	275



$$V_t = E_A = 257.5 \text{ V} \quad \text{when } I_A = 0$$

$$V_t = 257.5 - 150 \times 0.25 = 220$$

$$\text{B) } V_t = 220 \text{ V} \quad I_L = ? \quad V_r = ?$$

$$E_A = V_t + I_A R_A$$

$$I_A = \frac{E_A - V_t}{R_A} = \frac{257.5 - 220}{0.25} = 150 \text{ A}$$

$$I_L = I_A - I_f \rightarrow I_L = 150 - 11 = 139 \text{ A}$$

$$V_R = \frac{V_{NL} - V_t}{V_T} = \frac{257.5 - 220}{220} \times 100\% = 17\%$$

$$\text{C) } V_T = ? \quad I_L = ? \quad V_R = ? \quad R_L = 1.5 \Omega$$

$$V_t = I_L \times R_L$$

$$V_t = 0 \times 1.5 = 0 \rightarrow I_L = 0$$

$$V_t = 30 \times 1.5 = 45$$

$$V_t = 60 \times 1.5 = 90$$

$$\text{from occ, } V_t = 221 \text{ V, } I_L = 148 \text{ A}$$

$$V_R = \frac{V_{NL} - V_t}{V_T} = \frac{257.5 - 221}{221} \times 100\%$$

$$V_R = 16.5\%$$

$$\text{D) from the curves of OCC and } r_f\text{-line}$$

$$I_{\text{break down}} = I_{\text{max}} = \frac{\Delta V}{R_0} = \frac{193 - 120}{0.25}$$

$$\Delta V = 73 \quad \text{FCR} = 0$$

$$I_{\text{max}} = \frac{73}{0.25} = 292 \text{ A}$$

## 2-4-

$$\text{FCR} = ? \quad V_t = 220 \quad I_L = 80 \text{ A}$$

$$\text{Using external characteristic when } I_L = 80 \text{ A, } V_t = 227 \text{ V}$$

$$E_A = V_t + I_A R_A, E_A = 220 + 80 \times (0.25) = 240 \text{ V}$$

$$\text{When } E_A = 240 \text{ V, from OCC so } I_f = 10 \text{ A}$$

$$\text{So } R_{ft} = 220 / 10 = 22 \Omega$$

$$\text{So } \text{FCR} = 22 - 20 = 2 \Omega$$

## 2-5-

$$N = 350 \text{ Rpv} \quad \text{FCR} = 0 \quad V_b = 2 \text{ V}$$

$$\Delta E = ? \quad \Delta I_f = ? \quad V_t = 220$$

$$I_L = 56 \text{ A, } I_f = \frac{220}{20} = 11 \text{ A}$$

$$\text{From occ } E_0 = 248 \text{ V, } I_A = I_L + I_f = 56 + 11 = 67$$

$$E_A = V_t + I_A R + V_b$$





$$E_A = 220 + 67(0.25) + 2 = 238.75V, \quad \text{From occ } I_f^* = 9.7$$

$$\Delta E = E_0 - E_A, \quad \Delta E = 248 - 238.75 = 9.25V$$

$$\Delta I_f = I_f - I_f^* \quad \Delta I_f = 11 - 9.7 = 1.3A$$

**3-Compound** short shunt, cumulative,  $n=850$  rpm,  $N_f=600$   $R_f=20$

**3-1-**  $F_{CR}=0$   $V_t=220$   $I_L=150$   $N_s=?$   $V_r=?$   $R_s=0$

$$I_f = \frac{220}{20} = 11A \quad I_s = I_L = 150$$

$$I_A = I_f + I_L \Rightarrow I_A = 150 + 11 = 161A$$

$$E_A = V_t + I_A R_A \Rightarrow E_A = 220 + 161 \cdot 0.25 = 260.25$$

From occ  $I_{eq}=13.5$

$$I_{eq} = I_f + \frac{N_s}{N_f} * I_s$$

$$13.5 = 11 + \frac{N_s}{600} * 150$$

$$2.5 = \frac{N_s}{600} * 150 \quad N_s = 10 \text{ turns}$$

$$V_{n \text{ load}} = 257.5V$$

$$V_r = \frac{V_{nL} - V_t}{V_t} * 100\%$$

$$V_r = \frac{257.5 - 220}{220} * 100\% = 17\%$$

**3-2-**

$$N_s=15 \quad R_s=0.05 \quad F_{CR}=0 \quad V_b=2V$$

$$V_t=220V \quad I_L=80A \quad I_A=? \quad E_A=?$$

$$\text{KVL, } V_{sh} = V_t + V_s, \quad V_{sh} = 220 + 0.05 * 80, \quad V_{sh} = 224$$

$$I_f = \frac{V_{sh}}{R_f} = \frac{224}{20} = 11.2A, \quad I_A = I_f + I_L = 80 + 11.2 = 91.2A$$

$$E_A = V_t + I_A (R_A + R_s) + 2$$

$$E_A = 220 + 91.2(0.25 + 0.05) + 2 = 249.36V$$

$$I_{eq} = 11 + \frac{15}{600} * 80 = 13A$$

$$E_0 = 258V, \quad \Delta E = 258 - 249 = 9V$$

**3-3-**

$$N_s=16 \quad R_s=0.05 \quad I_L=150 \quad I_f=10 \quad V_b=2V$$

$$\text{Fund } F_{CR}=? \quad V_r, V_t$$

$$I_L = I_s = 150$$

$$I_A = 150 + 10 = 160A$$



$$I_{eq} = I_f + \frac{N_s}{N_f} * I_s$$

$$I_{eq} = 10 + \frac{16}{600} * 150 = 14A$$

From occ  $E_A = 262.5V$

$$V_t = E_A - I_A (R_A + R_s) - V_b$$

$$V_t = 262.5 - 160(0.25 + 0.05) - 2 = 212.5V$$

$$V_{sh} = V_f = V_t + V_s$$

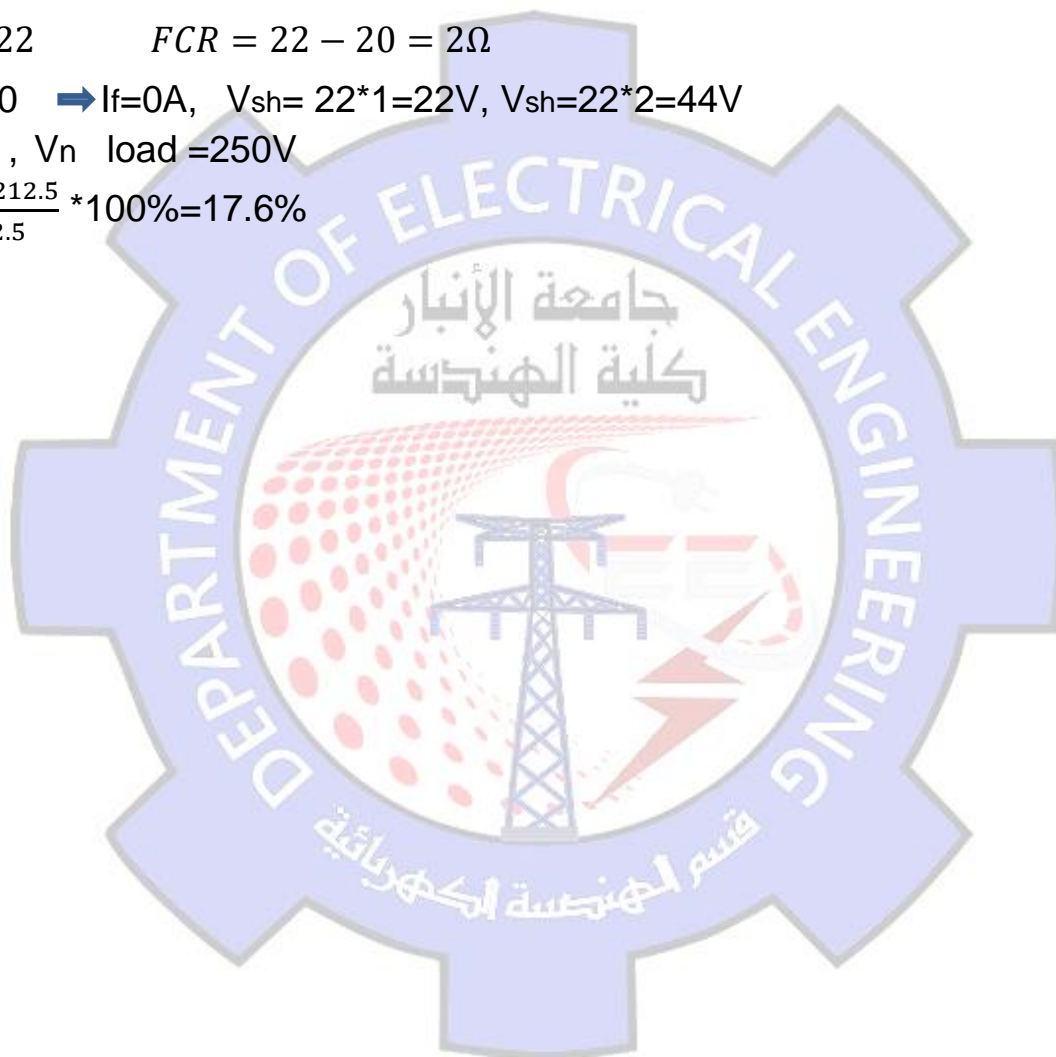
$$V_{sh} = 212.5 + 150 * 0.05 = 220$$

$$R_f = \frac{220}{10} = 22 \quad FCR = 22 - 20 = 2\Omega$$

$$V_{sh} = R_f I_f = 0 \Rightarrow I_f = 0A, \quad V_{sh} = 22 * 1 = 22V, \quad V_{sh} = 22 * 2 = 44V$$

From occ,  $V_n \text{ load} = 250V$

$$VR = \frac{250 - 212.5}{212.5} * 100\% = 17.6\%$$





## EXERCISES

Unless otherwise stated, assume that (a) winding resistances are given at the working temperatures, (b) the demagnetizing effect of armature reaction is negligible, and (c) the brush contact drop is 2V.

Answers obtained from graphical solutions are approximate and cannot be reproduced exactly. In some questions you have to use your judgment to make simplifying assumptions.

**Questions 1-8** refer to **machine 1** which is a dc generator rated at 3 KW, 125 V, and 1150 rpm. The OCC is given in the adjacent table. The armature winding resistance is  $0.38 \Omega$  and the commutating winding resistance is  $0.0716 \Omega$ . The field winding has 1070 turns per pole and its resistance is  $66.6 \Omega$ .

$I_f(A)$	$E_A(V)$
0.0	6
0.08	11
0.20	26
0.40	52
0.50	64.5
0.66	79
0.84	94
1.08	110
1.34	125
1.67	140
1.93	150
2.20	159
2.52	167
2.92	175
3.40	183

- Machine 1 is separately excited from a 150 V source.
  - Find the field current at rating; also find the setting of the field control resistor and the voltage regulation.
  - The load resistance and field control resistance remain as in part (a), but the speed is raised to 1500 rpm. Find the terminal voltage and current, and the voltage regulation.
  - The generator runs at 1500 rpm and delivers rated current at rated voltage. Find the field current, FCR, and VR.
  - The machine is delivering rated current at rated at rated voltage with FCR set at  $40 \Omega$ . Find the speed and VR.
- Machine 1 is separately excited from a 150 V source, but it has no interpoles. The brushes are shifted to improve commutation. The generator operates are rating with FCR set at  $16 \Omega$ .
  - Find the voltage regulation.
  - Determine the demagnetizing effect of armature reaction in volts and in field amps.
- Machine 1 is operated as a shunt generator.
  - The generator is started with no external field resistance. Find the voltage to which it builds up at 1150 rpm, and find the minimum speed at which it can build up.
  - repeat part (a) for a cold start (assume an ambient temperature of  $20^\circ C$ ).
  - what is the maximum field circuit resistance that allows build-up at 1150 rpm? at 800 rpm? at 1500 rpm?



- d. Find the field circuit resistance that allows the generator to build up to rated voltage at rated speed.
  - e. With no external field resistance, what is the maximum accelerating voltage during build-up at 1150 rpm? What is the corresponding field current?
  - f. The generator build –up to rated voltage with the external field resistance set to zero. Find the speed.
4. Machine 1 is operated as a shunt generator at 1150 rpm.
- a. Find the short circuit current.
  - b. Find the breakdown current when the external field resistance is set to give rated voltage at no load.
  - c. Find the maximum breakdown current.
5. Machine 1 is operated as a shunt generator at 1150 rpm. The terminal voltage is at rated value.
- a. Find the current and VR when FCR is shorted out.
  - b. Repeat part (a) for a field control resistor of  $20\Omega$ .
  - c. Find the value of the external field resistance when the generator delivers rated current; also find VR.
6. Machine 1 runs at 1150 rpm and supplies a load current of 20A with a field current of 1.58 A. find VR and. FCR for the following cases:
- a. Separate excitation as in problem I.
  - b. Shunt connection.
  - c. Cumulative compound, long shunt connection. The series field winding has 18 turns/pole and its resistance is  $0.069\Omega$ .
  - d. Cumulative compound, short shunt connection. Series field winding as in part c.
  - e. Differential compound, short shunt connection. Series field winding as in part c.
7. Machine 1 is connected in long shunt cumulative with a series field wdg of 18 turns/pole and  $0.069\Omega$  resistance. It is operating at rating with a diverter across the series field wdg.





- a. Estimate the diverter resistance when the shunt field external resistance is set at  $20\ \Omega$  and the ratio of diverter resistance to series field resistance is 0.5 ; also find the voltage regulation.

- b. Estimate the diverter resistance when VR is zero.

8. Machine 1 is connected in long shunt cumulative compound as in problem 7. There is no diverter and no interpoles. The brushes are shifted from the q-axis to improve commutation. Find the demagnetising effect of armature reaction in volts and in field amps.

9. The machine described in the exercises of pages 4.6 and 5.4 is run as a generator at 800 rpm. Armature current is 100 A. The no load voltage is 271 V, and the Armature reaction is not negligible. Find the load current, terminal voltage, and voltage regulation for the following cases:

- a) Separate excitation.

- b) Shunt connection.

- c) Cumulative compound long shunt connection. The series field wdg has 12 turns /pole and its resistance is  $25\ m\Omega$ .

10. A series generator has the OCC given in the table. The armature resistance is  $0.6\ \Omega$ . The field wdg has 50 turns /pole, and its resistance is  $0.1\ \Omega$ . The brushes are shifted from the q-axis so that the demagnetizing armature reaction is 750 AT/pole when the load current is 60A.

- a) Plot the external characteristic up to a load current of 90 A.

- b) What is the load current and terminal voltage when the load resistance is  $2\ \Omega$ ?

- c) What is the critical load resistance?

- d) Find the load current when the terminal voltage is 85 V?

- e) What is the maximum voltage?

- f) A diverter  $0.15\ \Omega$  is connected across the field winding; find the terminal voltage when the load current is 70A?

Amps	volts
0	5
4	20
8	39
10	49
15	69
20	87
26	107
30	117
35	126
40	131
45	134
50	136
60	140
80	144

Volte	Amp
15.5	0.0
15.4	2.0
15.2	3.8
14.9	5.7
14.7	6.8
14.5	7.8
14.0	9.8
13.5	11.5
13.0	13.0
12.2	14.6
11.9	15.8
10.5	19.0



11. A battery is rated at 12 V and 10 A. it has a constant internal resistance of  $0.2 \Omega$ .
- Find the load resistance and VR at rating.
  - Find the voltage, current, and VR when the load resistance is  $0.8 \Omega$  and when it is  $1.6 \Omega$ .
12. A dc generator has the external characteristic given in the adjacent table.
- Find the voltage, current, and VR when the load resistance is  $0.8 \Omega$  and when it is  $1.6 \Omega$ .
  - Find the load current, load resistance, and VR when the terminal voltage is 12.5 V.
  - Find the terminal voltage, load resistance, and VR when the load current is 18 A.
13. The battery of problem 11 and the generator of problem 12 are operated in parallel.
- Find the voltage, current; and VR when the load resistance is  $0.8 \Omega$  and when it is  $1.6 \Omega$ .
  - Determine who the battery and generator share the load current in part a.
  - Find the voltage and currents when there is no external load. What does this case represent?
14. The adjacent table gives the (V-I) characteristics for two dc generators, G1 and G2 and for a nonlinear resistor.
- Find the voltage, current, voltage regulation (VR) when G1 is only loaded by (i)  $1.5 \Omega$  resistor (ii)  $R_n$  resistor (iii)  $1.5 \Omega$  parallel with  $R_n$ .
  - Repeat part (a) for G2 is only.
  - Repeat part (a) when G1 and G2 are in parallel.
  - Determine the current sharing of the two generators for part (c).

Amp.	volts		
	G1	G2	$R_n$
0	360	360	0
50	351	357	50
100	339	352	114
150	323	347	180
200	302	338	230
250	277	326	265
300	244	310	291
350	202	286	312
400	----	256	328
450	----	221	340
500	----	----	343

## ANSWERS

Recall that answers obtained from graphical solutions are approximate and cannot be reproduced exactly. That is, your solution might be correct although your answer appears different from the one given here. An error is indicated only if the difference is rather large.

1. a. 1.61A,  $26.6 \Omega$ , 10.2 %. b. 163.6 V, 31.4A, 9.8%.



- c. 1.0A, 82 , 10.2%. d. 1235 rpm, 10.2%.
2. a. 16.8%, b. 9.9V, 0.24 A.
3. a. 167.5 V, 589 rpm. b. 181.5 V, 485 rpm. c.  $130\Omega$ ,  $90.5\Omega$ ,  $170\Omega$ .  
d.  $93\Omega$ , e. 39 V, 0.96 A. f. 968 rpm.
4. a. 8.86 A. b. 34.8 A. c. 81 A.
5. a. 45.7 A, 34%. b. 4.3 A, 9.2 %. c.  $10\Omega$ , 22.4%.]
6. a. 8.8%,  $28.3\Omega$ . b. 19.4%,  $12.4\Omega$ . c. 0.9%,  $20.3\Omega$ .  
d. 1.5%,  $22.1\Omega$ . e. 50.5%,  $2.18\Omega$ .
7. a.  $73m\Omega$ , 9.2%. b.  $208m\Omega$ .
8. 30 V, 0.42 A.
9. a. 100 A, 248.5 V, 9%. b. 94A, 240 V, 12.8%. c. 94A, 261 V, 3.8%.
- 10.a. volts: 30.5, 57, 78.5, 95, 101.7, 102, 100.4, 98, 95. b. 67.4A, 100.8V; 50.8A, 101.7V.  
c.  $2.9\Omega$ . d. 40A, 90A. e. 102 V. f. 67.8V.
- 11.a. 1.2, 16.7. b. 11.2 V, 14 A, 25%; 12.4V, 7.8A, 12.5%.
12. a. 12.2V, 15.2A, 27.4%; 14.3V,  $0.61\Omega$ , 42%. b. 14.3,  $0.87\Omega$ , 24%. C. 11V,  $0.61\Omega$ , 42%.
13. a. 13.2V, 16.5A, 14%; 14.1V, 8.8A, 6.4%. b. 4.1A, 12.4A; - 0.6A, 9.4A. c. 15V, 5.1A.
14. a. 301V, 201A, 19.6%; 270.5V, 261A, 33.1%; 217.5V, 333A, 65.5%. b. 333V, 223A, 8.1%; 300V, 321A, 20%; 253.5V, 402A, 42%. C. 345V, 231A, 4.4%, 325.5V, 392 A, 10.6%; 301V, 522A, 19.6% d. 74A, 160A; 143A, 251A; 202A, 320A.