



- (e) curves of input power, output power and efficiency against torque, assuming friction and iron losses are zero;
- (f) the frequency and speed at which  $X = L$  is equal to the resistance  $R$ , if the phase inductance is 5 mH;
- (g) what is the effect of (f) on the speed/torque curve i.e. the effect of  $L > 0$  and  $L > R$  as speed increases?
6. A brushless dc motor has 3 phases and 6 poles. The electromagnetic torque is 4 Nm with a current of 0.5 A rms. Friction and iron losses produce a constant retarding torque of 0.1 Nm. The resistance and inductance per phase are 70  $\Omega$  and 50 mH. Assume optimum position feedback. Calculate
- (a) the torque and emf constants;
- (b) the emf generated for a speed of 600 rpm;
- (c) the speed of the motor for a supply voltage of 200 V (ac rms per phase) with no external load;
- (d) the speed, current and efficiency for an external load of 4 Nm and a supply voltage of 200 V ac rms;
- (e) the supply frequency for (d), and check  $\omega L < R$ .

## Chapter 10

### BLDCM

7. A brushless dc motor has 3 phases and 4 poles. The generated emf is 220 V rms sinusoidal at 1000 rpm (open circuit voltage when tested as generator with a drive motor). Calculate
- (a) the emf constant (V/Rad/s);
- (b) the torque constant (Nm/A) with optimum position feedback angle;
- (c) the speed/torque curve, if the resistance per phase is 4  $\Omega$  ;
- (d) the supply frequency at 1000 rpm;
- (e) curves of input power, output power and efficiency against torque, assuming friction and iron losses are zero;
- (f) the frequency and speed at which  $X = \omega L$  is equal to the resistance  $R$ , if the phase inductance is 5 mH;
- (g) what is the effect of (f) on the speed/torque curve i.e. the effect of  $L > 0$  and  $L > R$  as speed increases?



Solution:

$$a) E = \frac{P}{2} \lambda_m \omega_r, \quad 220 = \frac{P}{2} \lambda_m (2 * (22/7) * 1000/60)$$

$$\frac{P}{2} \lambda_m = 2.1 \text{ V/Rad/Sec}$$

$$b) T_{em} = \frac{mP}{2} \lambda_m I, \quad \frac{mP}{2} \lambda_m = 3 * 2.1 = 6.3$$

Nm/A

$$c) \omega_r = \frac{V}{p \lambda_m / 2} - \frac{R}{m(p \lambda_m / 2)^2} T_{em}$$

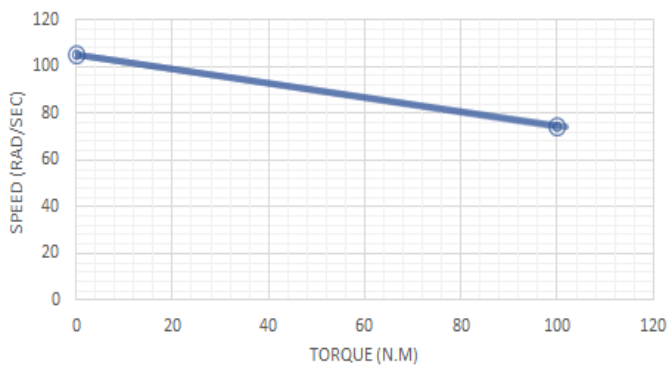
$$\omega_r = \frac{220}{2.1} - \frac{4}{3(2.1)^2} T_{em}$$

$$\omega_r = 104.76 - 0.302 T_{em}$$

Make table between speed and torque take two values of torque

When  $T_{em}=0$ ,  $\omega_r=104.76$  rad/sec

When  $T_{em}=100$ ,  $\omega_r=74.56$  rad/sec



So the curve as in Figure

$$d) \omega_r = 2w/p, \quad w = \omega_r * p/2 = 2 * (22/7) * 1000/60 * 4/2 = 209.5 \text{ Hz}$$

$$e) T_{em} = \frac{P_{em}}{\omega_r}, \quad P_{out} = p_{em} = T_{em} * \omega_r, \quad = 104.76 T_{em} \quad (1)$$

use  $T_{em}=0$ , then  $P_{out}=0$  watt,  $T_{em}=10$ , then  $p_{out}=1047.6$  watt

$$P_{in} = P_{cu} + P_{Fe} + P_{mec} + P_{out}, \quad P_{in} = P_{cu} + P_{out}$$

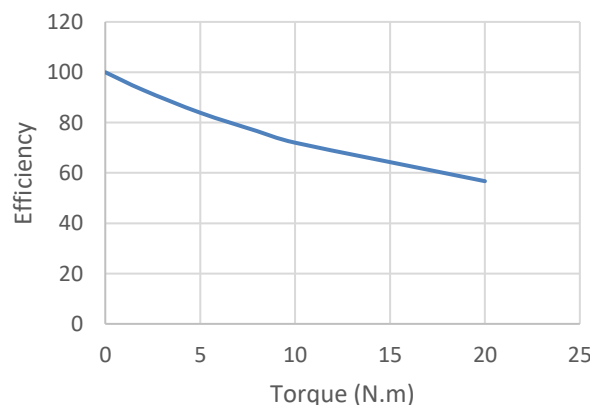
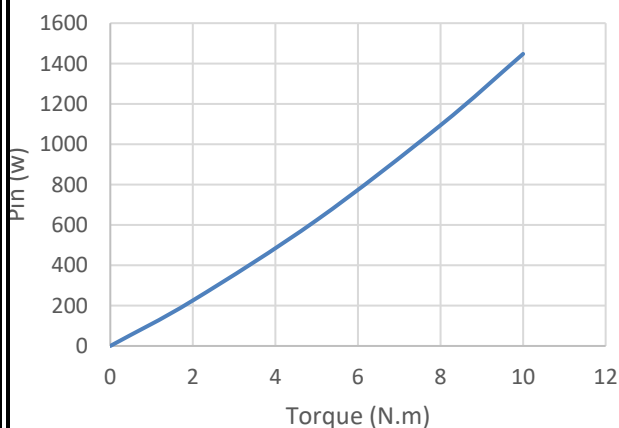
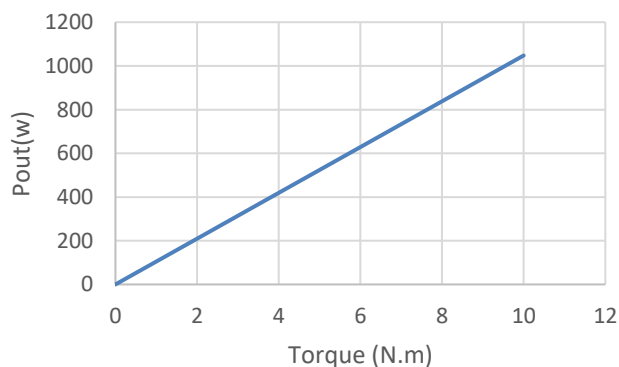
$$P_{in} = mR I^2 + T_{em} * \omega_r, \quad I = \frac{2 * T_{em}}{mP \lambda_m} \text{ sub in } P_{in}$$

$$P_{in} = mR \frac{2 * T_{em}^2}{m^2 P^2 \lambda_m^2} + T_{em} * \omega_r, \quad P_{in} = 4 \frac{T_{em}^2}{2.1^2} + T_{em} * 104.76$$

$$P_{in} = 0.302 T_{em}^2 + 104.76 T_{em} \quad (2)$$

$$T=0, \text{ then } p_{in}=0, \quad T=2, \quad p_{in}=225.5$$

$T_{em}$	$P_{out}$
0	0
2	209.5
5	523.8
8	838
10	1047.6



Other calculation in table



$$\eta = \frac{P_{out}}{P_{in}} = \frac{T_{em} * \omega_r}{0.302T_{em}^2 + 104.76 T_{em}}$$

$$\eta = \frac{104.76}{4 T_{em} + 104.76} \times 100\% \quad (3)$$

T=0,  $\eta = 100\%$ , T=2, Type equation here.

T <sub>em</sub>	P <sub>in</sub>
0	0
2	225.5
5	623.8
8	1094
10	1447.6

T <sub>em</sub>	Effe
0	100
2	
5	98.5
8	
10	
20	
100	

f)  $X=wL=R$ ,  $w=R/L$   
 $W=4/(0.005)=800$  Hz  
 $W_r=2w/p=2*800/4=400$  rad /sec

g)  $w_r = \frac{V}{p\lambda_m/2} - \left( \frac{R}{m(p\lambda_m/2)^2} + j \frac{wL}{m(p\lambda_m/2)^2} \right) T_{em}$

When L increased the drop-in speed will increased at constant torque while the torque will decreased also when L increased at constant speed

