



# Fundumantal of Electronic II

**Second Class**

Chapter05: BJT AC Analysis

Lec05\_p1

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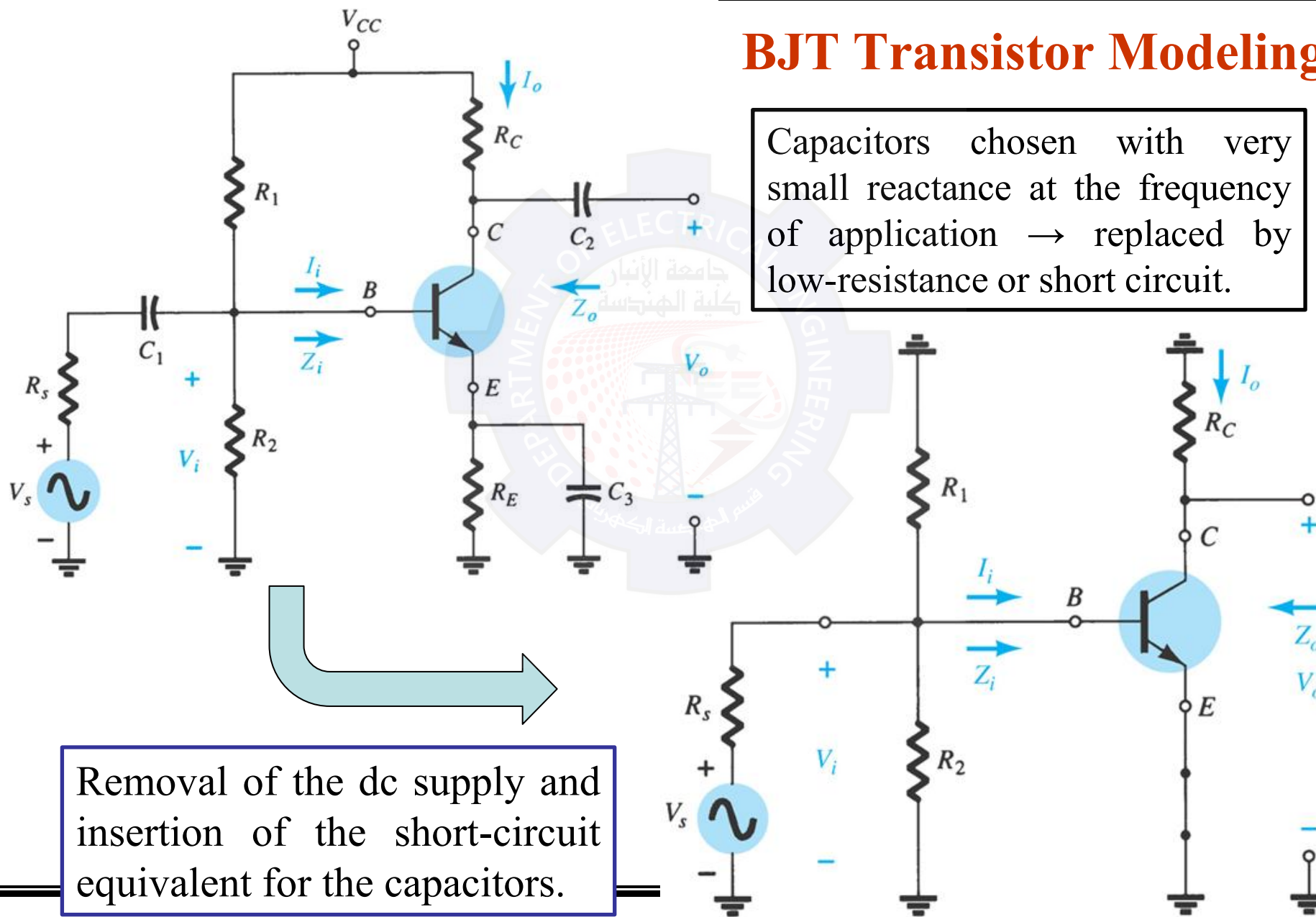
# BJT Transistor Modeling

- A model is an equivalent circuit that represents the AC characteristics of the transistor.
- A model uses circuit elements that approximate the behavior of the transistor.
- There are two models commonly used in small signal AC analysis of a transistor:
  - **$r_e$  model**
  - **Hybrid equivalent model**



## BJT Transistor Modeling

Capacitors chosen with very small reactance at the frequency of application  $\rightarrow$  replaced by low-resistance or short circuit.

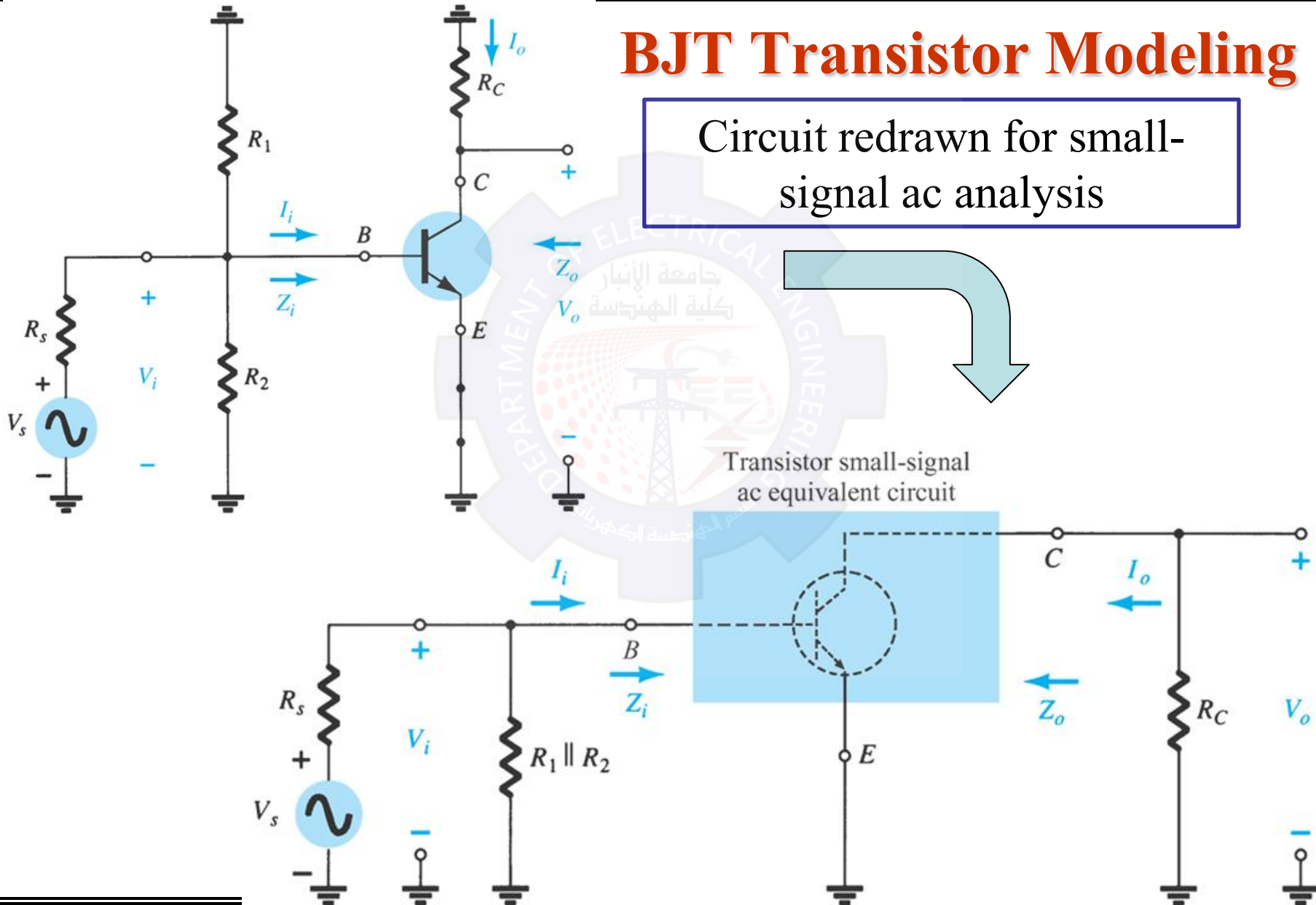


Removal of the dc supply and insertion of the short-circuit equivalent for the capacitors.



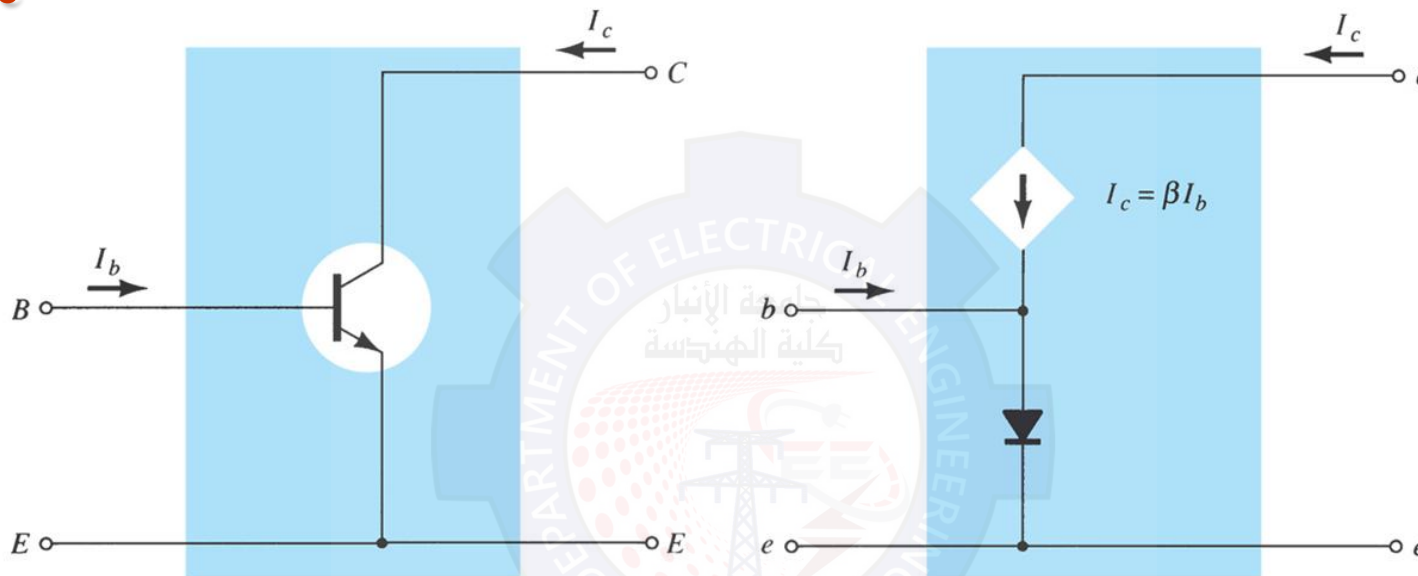
# BJT Transistor Modeling

Circuit redrawn for small-signal ac analysis





# The $r_e$ Transistor Model Common Emitter Configuration

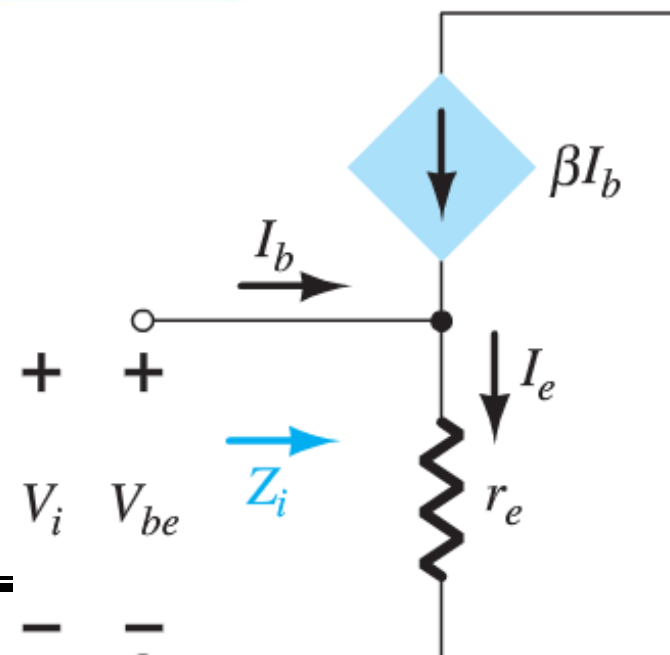


$$Z_i = \frac{V_i}{I_b} = \frac{V_{be}}{I_b}$$

$$V_{be} = I_e r_e = (I_c + I_b) r_e = (\beta I_b + I_b) r_e$$

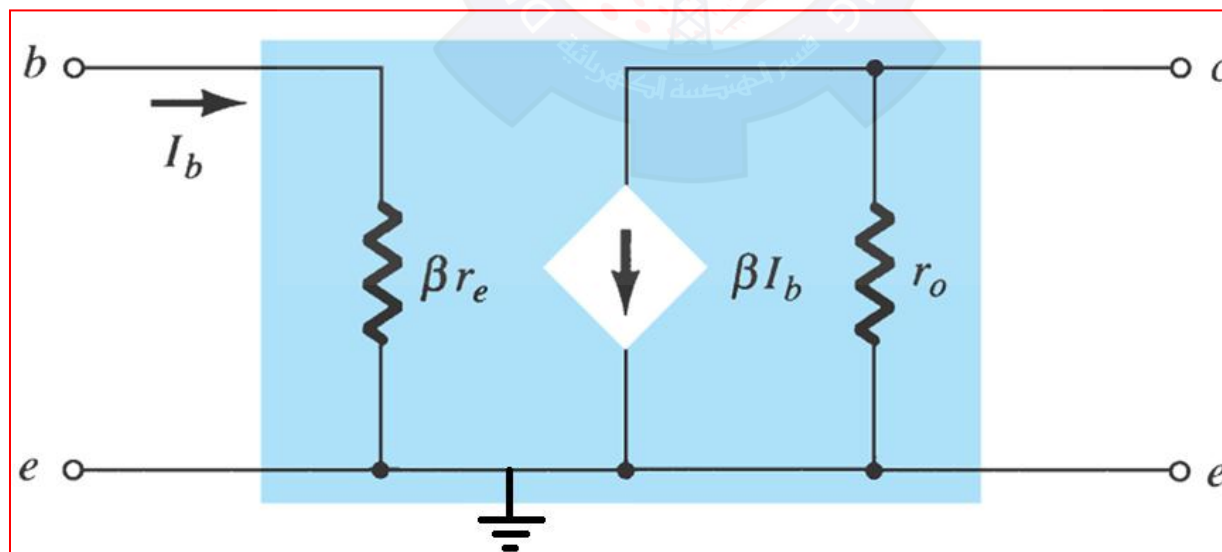
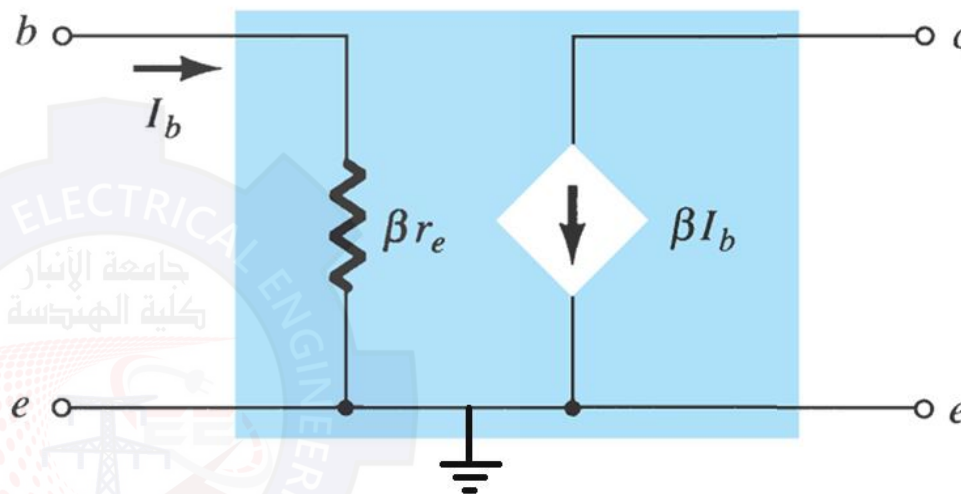
$$= (\beta + 1) I_b r_e$$

$$Z_i = \frac{V_{be}}{I_b} = \frac{(\beta + 1) I_b r_e}{I_b} = (\beta + 1) r_e \approx \beta r_e$$



# The $r_e$ Transistor Model Common Emitter Configuration

$$r_e = \frac{26 \text{ mV}}{I_E}$$





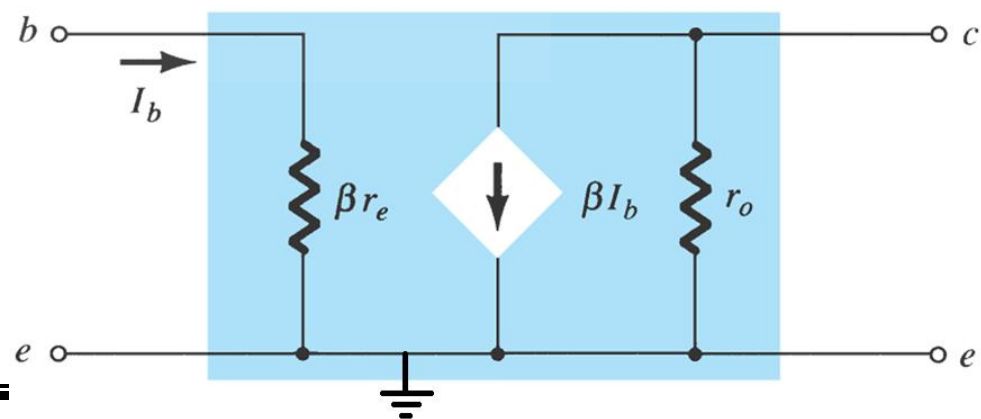
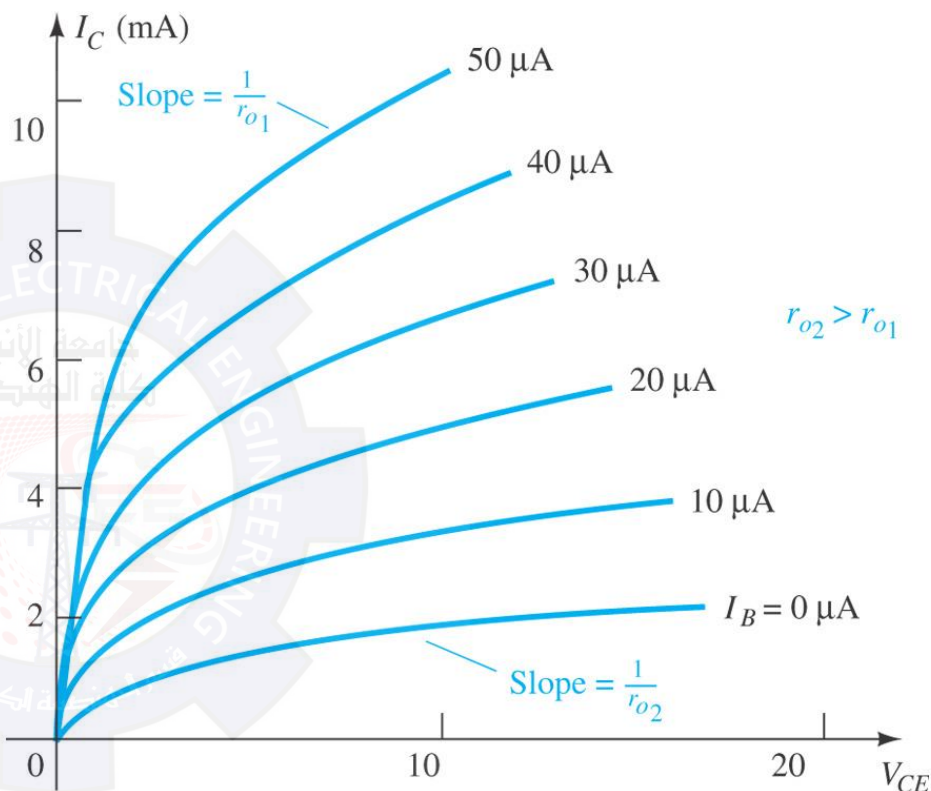
# The $r_e$ Transistor Model

## Common Emitter Configuration

$$\text{slope} = \frac{\Delta I_C}{\Delta V_{CE}} = \frac{1}{r_0}$$

$$r_0 = \frac{\Delta V_{CE}}{\Delta I_C}$$

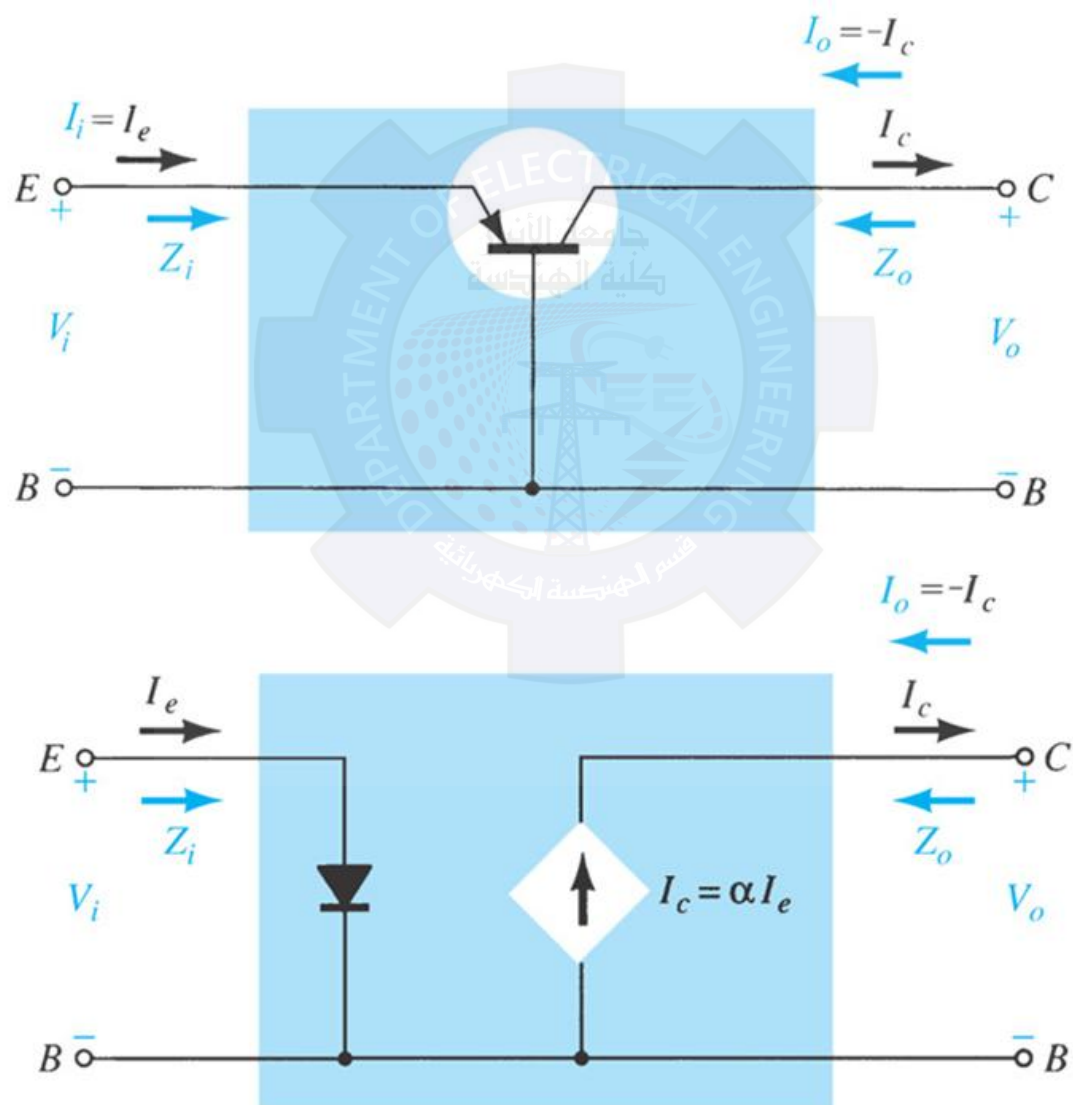
The output resistance  $r$  is typically in the range of 40 k $\Omega$  to 50 k $\Omega$







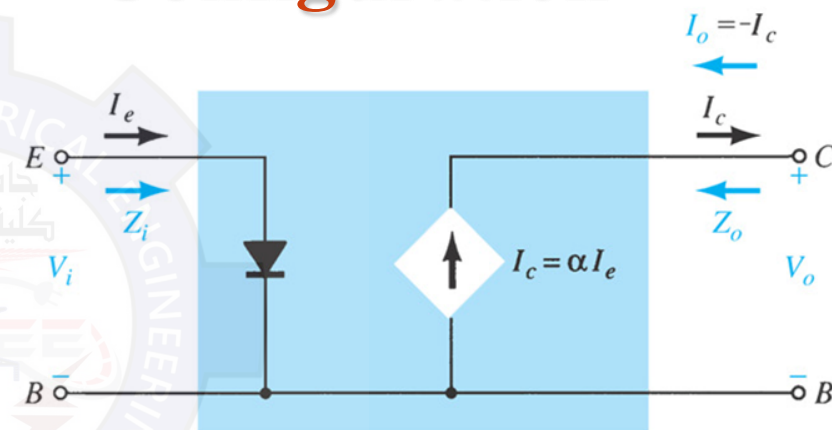
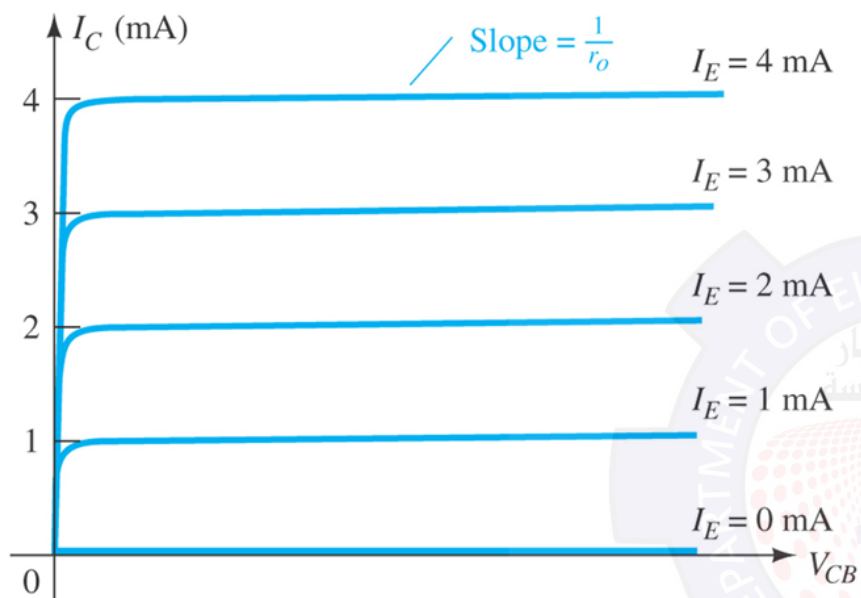
# Common-Base Configuration





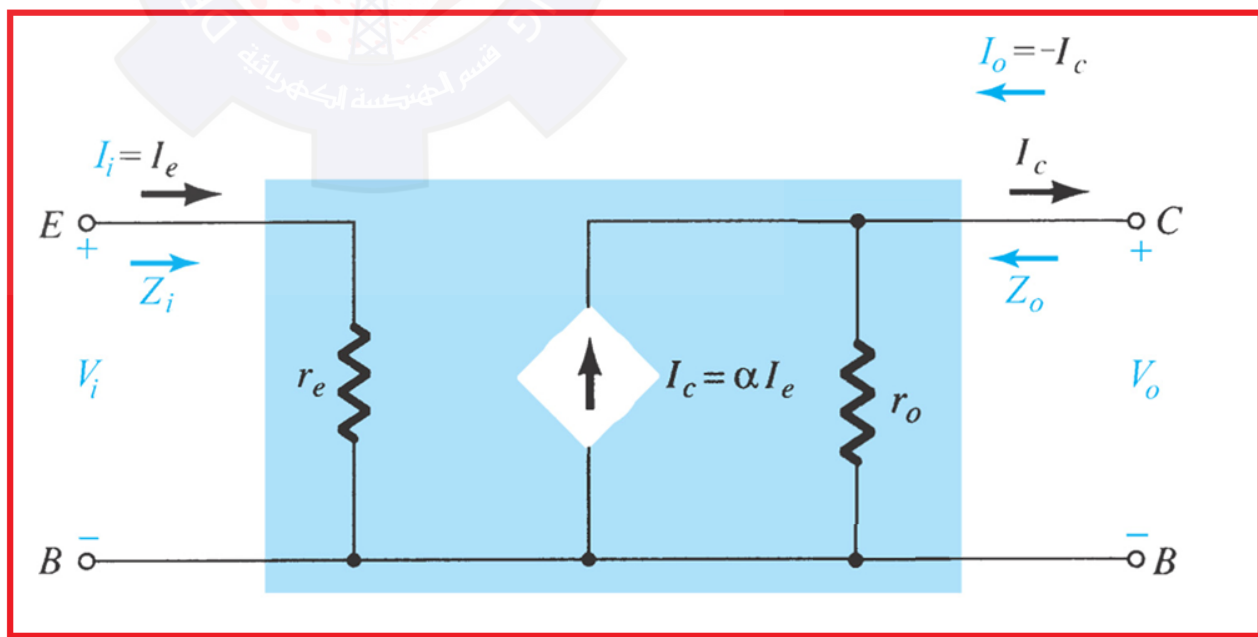


# Common-Base Configuration

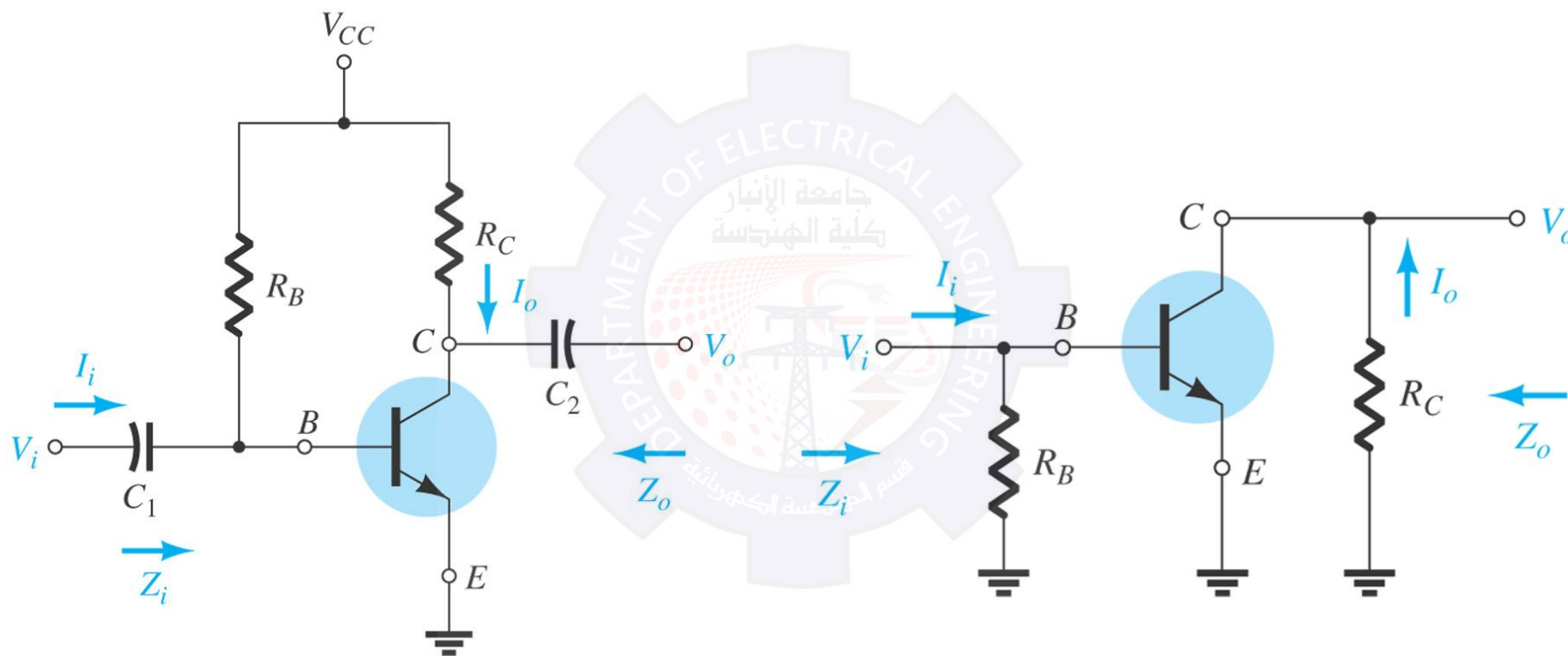


The output resistance  $r_o$  is quite high, typically extend into the megaohm range.

Common Base  $r_e$  equivalent circuit



## Common Emitter Fixed Bias Configuration

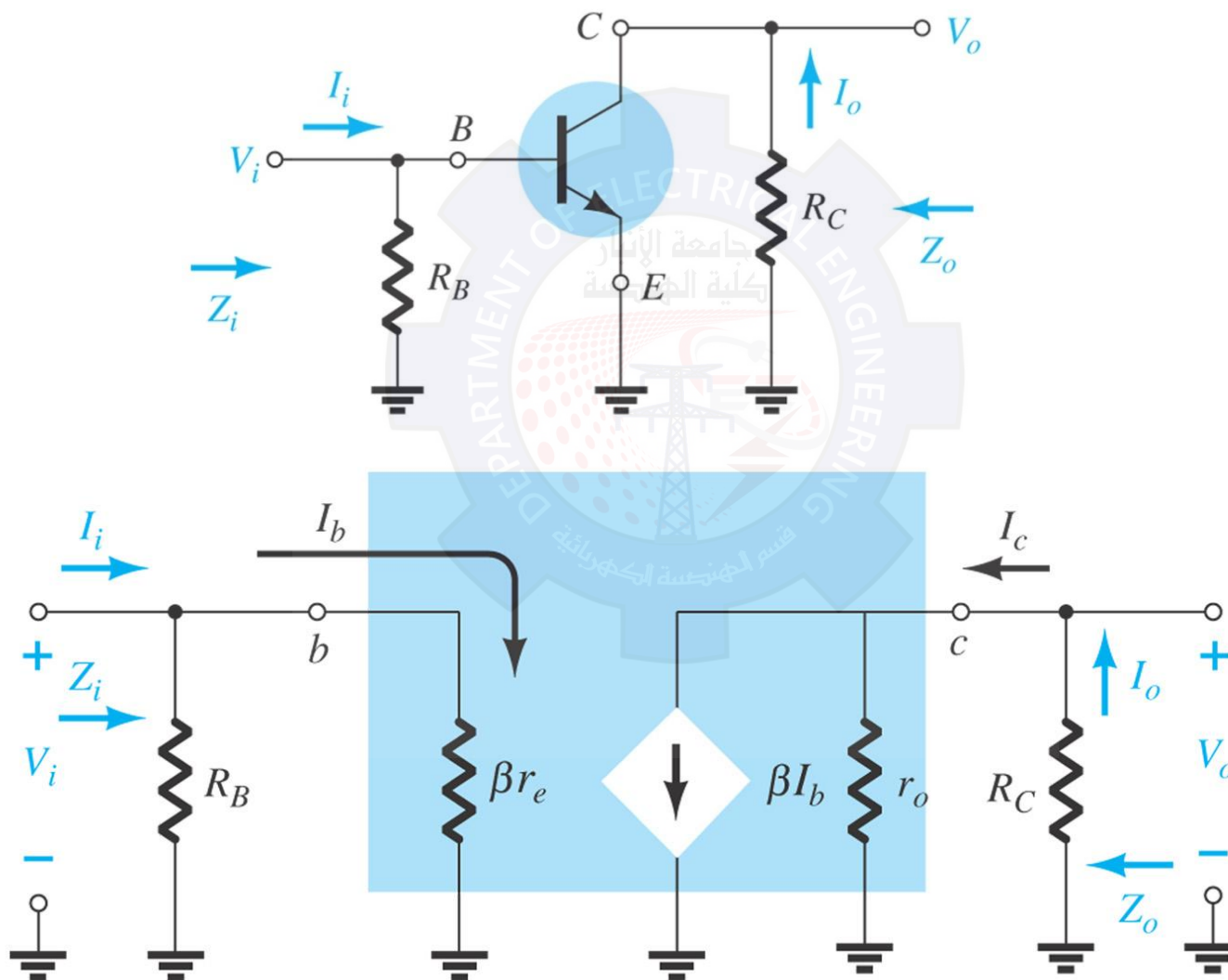


Common-emitter fixed-bias configuration.

Network after the removal of the effects of  $V_{CC}$ ,  $C_1$  and  $C_2$ .



## Common Emitter Fixed Bias Configuration



Substituting the  $r_e$  model into the network.



## Common Emitter Fixed Bias Configuration

### Input impedance:

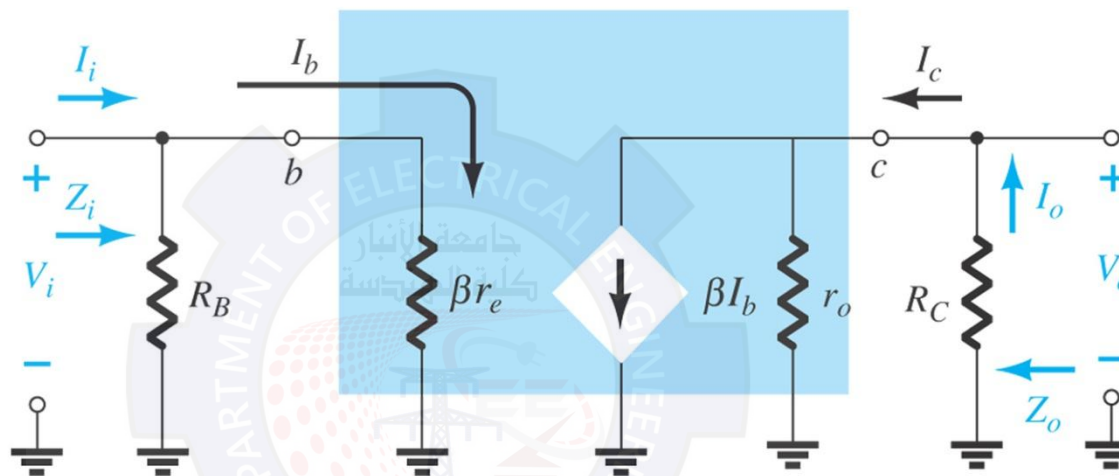
$$Z_i = R_B \parallel \beta r_e$$

$$Z_i \cong \beta r_e \quad | \quad R_E \geq 10\beta r_e$$

### Output impedance:

$$Z_o = R_C \parallel r_o$$

$$Z_o \cong R_C \quad | \quad r_o \geq 10R_C$$



### Voltage gain:

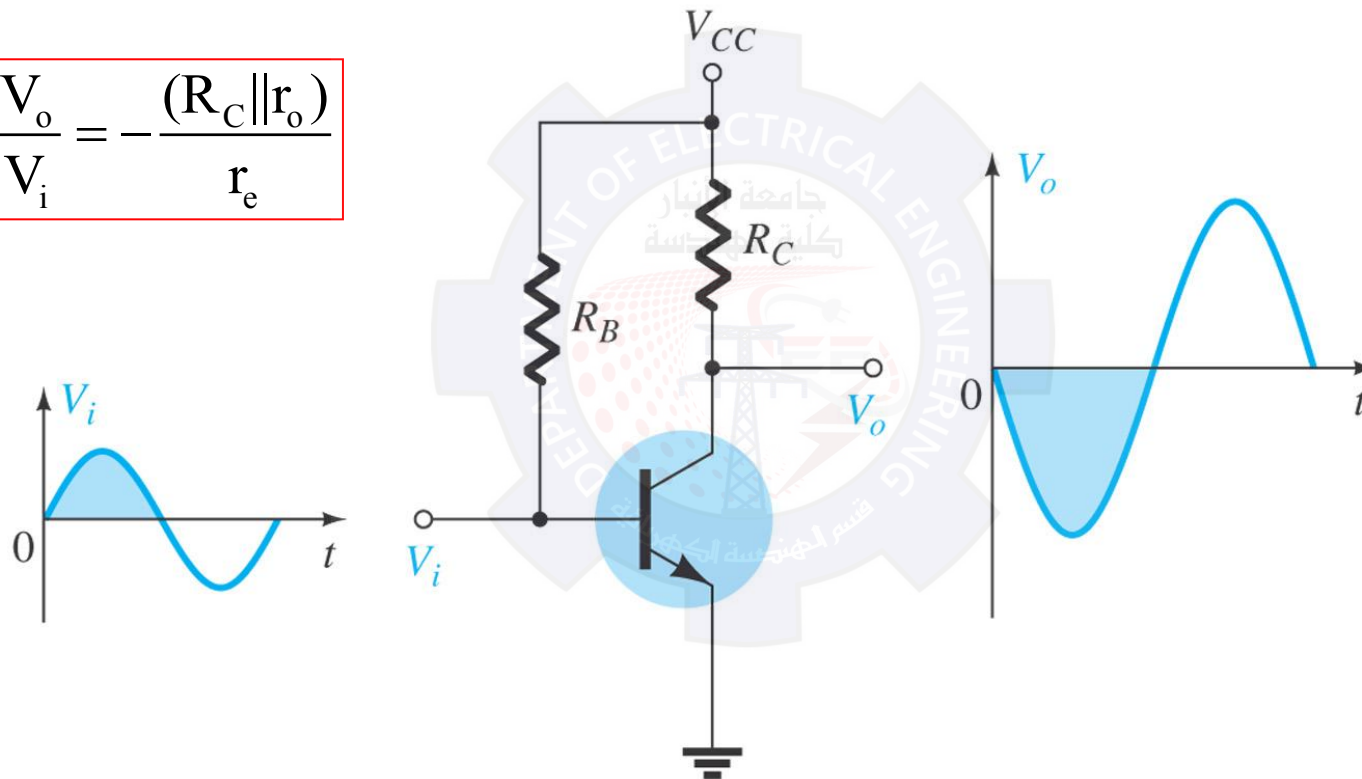
$$V_o = -\beta I_b (R_C \parallel r_o) , \quad I_b = \frac{V_i}{\beta r_e} , \quad V_o = -\beta \left( \frac{V_i}{\beta r_e} \right) (R_C \parallel r_o)$$

$$A_v = \frac{V_o}{V_i} = -\frac{(R_C \parallel r_o)}{r_e} , \quad A_v = -\frac{R_C}{r_e} \quad | \quad r_o \geq 10R_C$$



## Common Emitter Fixed Bias Configuration

$$A_v = \frac{V_o}{V_i} = -\frac{(R_C || r_o)}{r_e}$$



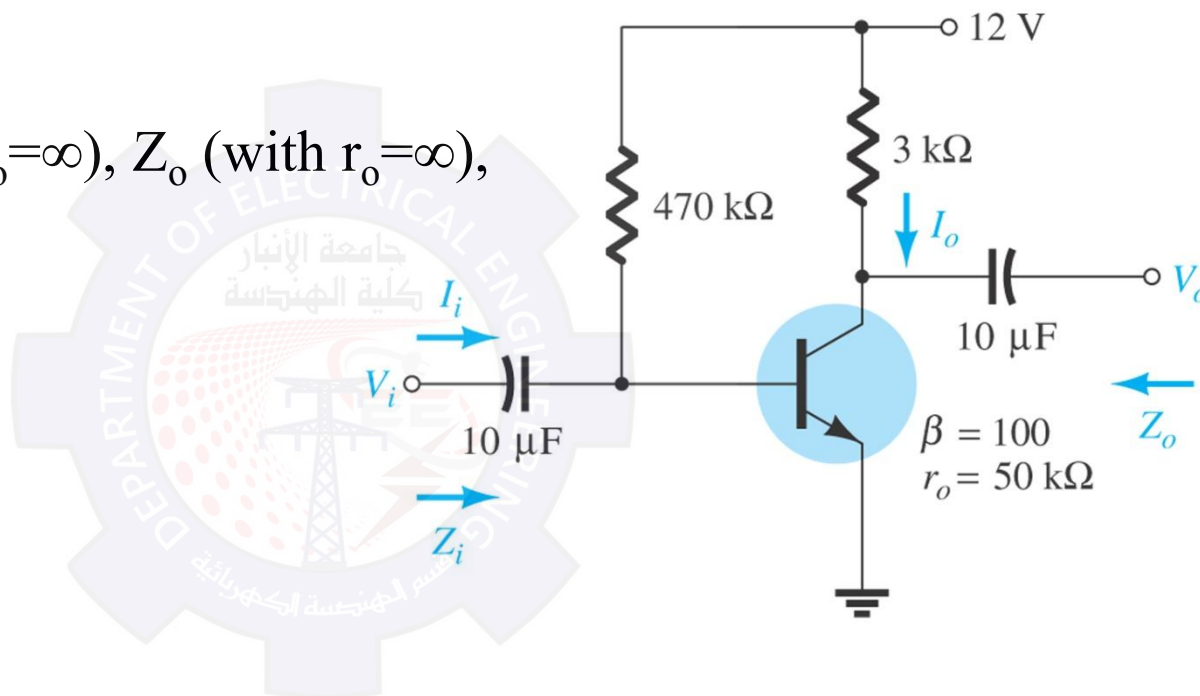
Demonstrating the  $180^\circ$  phase shift between input and output waveforms.



## Example 5.1

Determine  $r_e$ ,  $Z_i$  (with  $r_o = \infty$ ),  $Z_o$  (with  $r_o = \infty$ ),  
 $A_v$  (with  $r_o = \infty$ ).

Repeat with  $r_o = 50 \text{ k}\Omega$ .





## Example 5.1 - Solution

